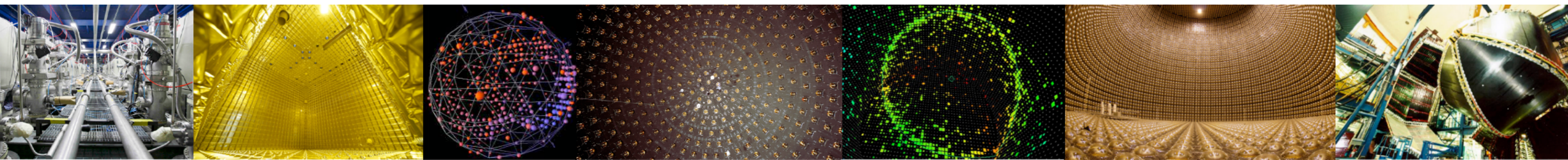
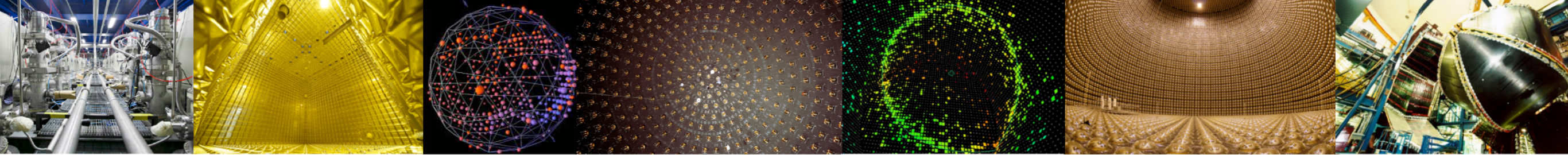


Interface between
BSM Scenarios and
Neutrino Event Generators

William Jay – MIT

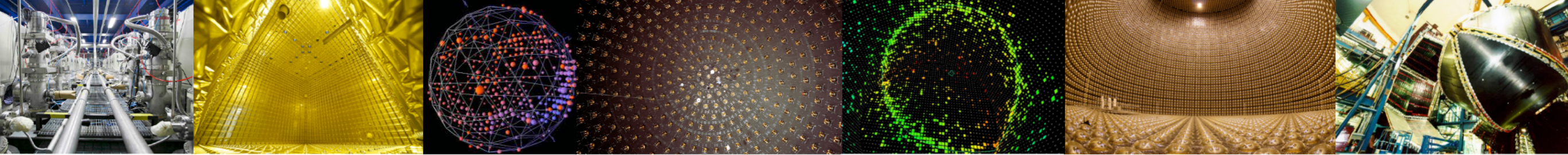
SBN Experiment-Theory Workshop
Santa Fe, New Mexico
2-5 April 2024





Outline

- Simulating the Standard Model
- Simulating beyond the Standard Model
- Examples
- Conclusions



Lepton Event Simulation

The hadronic grand challenge

Want: Mixing parameters, e.g, angle θ

$$P_{\nu_{\mu} \rightarrow \nu_e} \approx \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

$$\Phi_e(E, L) \propto P_{\nu_{\mu} \rightarrow \nu_e}(E, L) \Phi_{\mu}(E, 0)$$

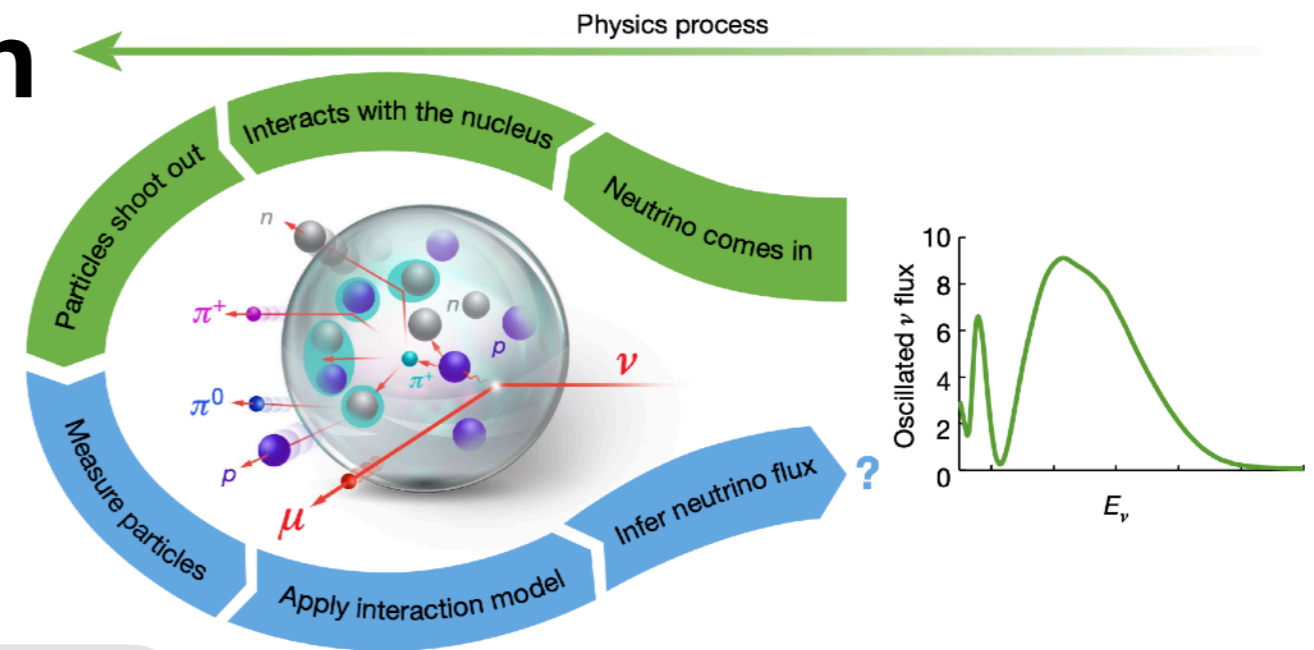
Neutrino fluxes. "Measurable."

$$N_{\alpha}(E_{\text{rec}}, L) \propto \int dE \Phi_{\alpha}(E, L) \sigma(E) f_{\sigma_i}(E, E_{\text{rec}})$$

Event rate

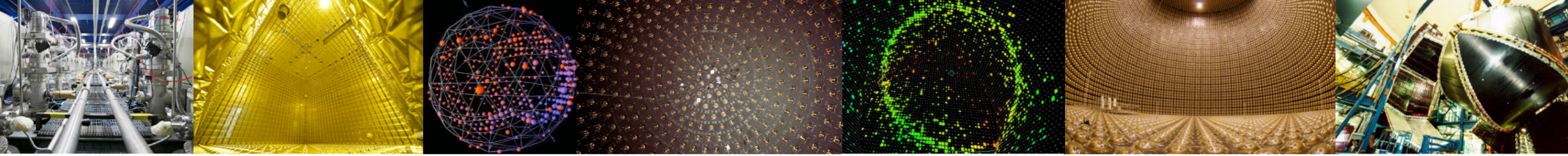
Interaction cross section

"Smearing matrix"
(Experimental + theoretical)

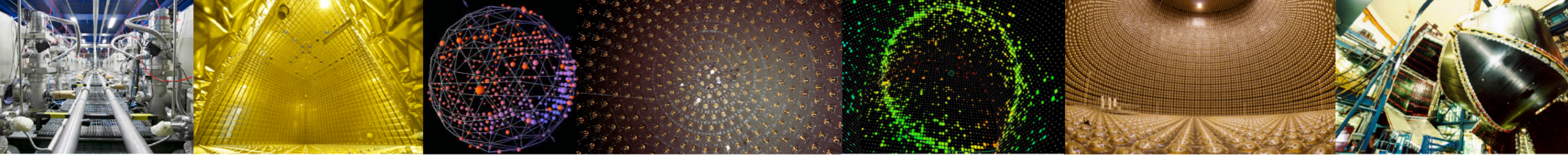


Experimental analysis

Physics process

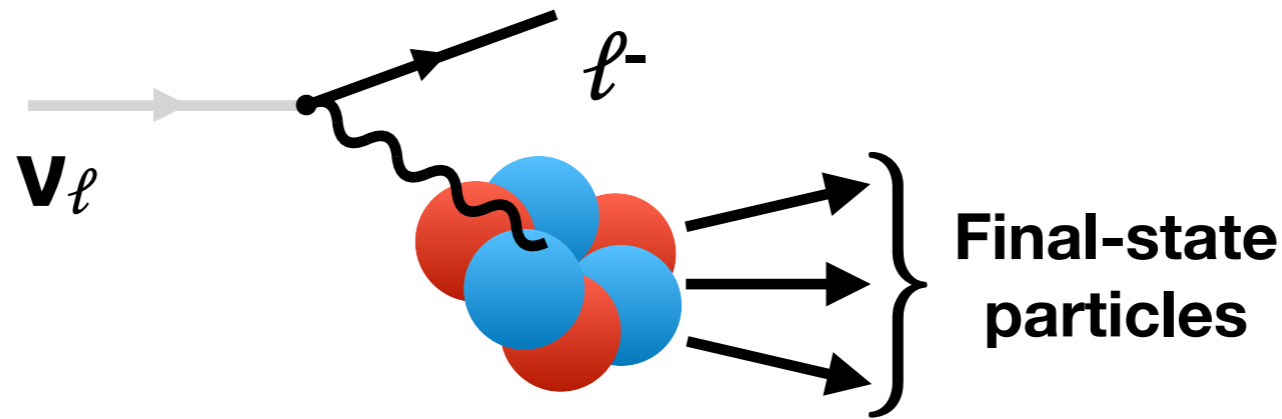


Simulating the Standard Model



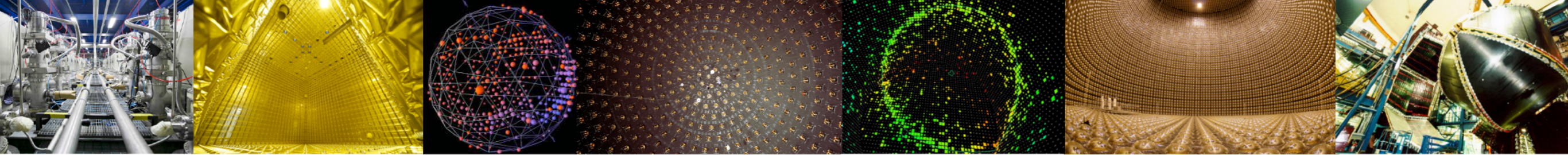
Simulating the Standard Model

Break the problem into well-defined theoretical pieces



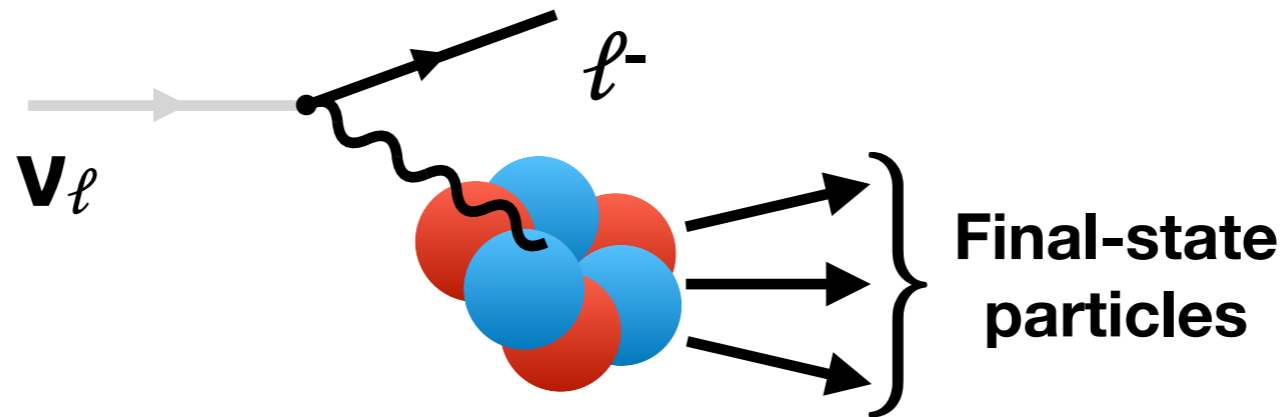
$$d\sigma = \left(\frac{1}{|v_A - v_\ell|} \frac{1}{4E_A^{\text{in}} E_\ell^{\text{in}}} \right) \times |\mathcal{M}|^2 \times \prod_f \frac{d^3 p_f}{(2\pi)^3} (2\pi)^4 \delta^4 \left(k_A + k_\ell - \sum_f p_f \right)$$

$$d\sigma = (\text{flux}) \times (\text{matrix element}) \times (\text{phase space})$$



The Matrix Element

Step 1: Factorization of leptonic and hadronic physics

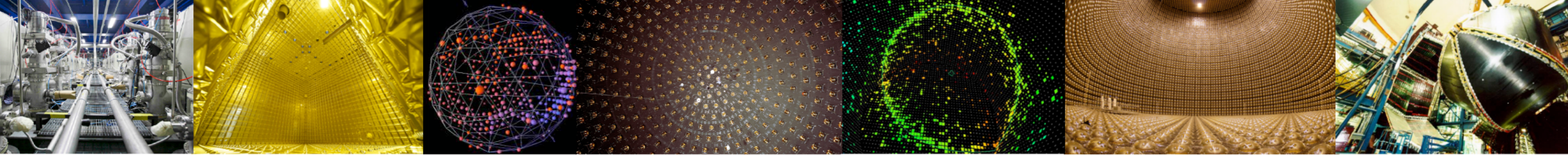


$$|\mathcal{M}|^2 = L_{\mu\nu} \frac{1}{P^2} W^{\mu\nu} \rightarrow \langle \Psi_0 | J_\mu^\dagger(q) | \Psi_f \rangle \langle \Psi_f | J_\nu(q) | \Psi_0 \rangle$$

Leptonic tensor:
 Calculable analytically
 in SM or BSM
 scenario.
 \implies More on this later.

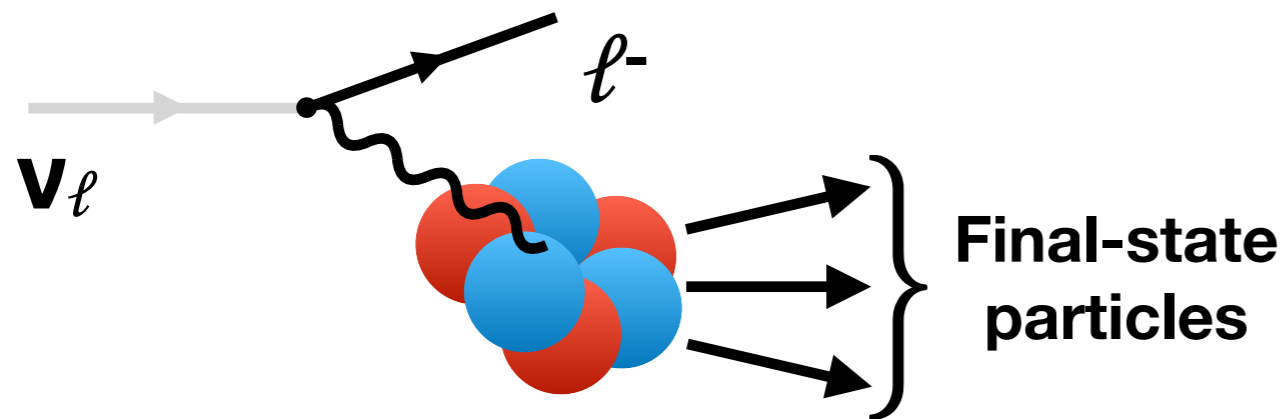
Hadronic tensor:
 Complicated multi-scale
 object, encoding all the
 hadronic/nuclear physics

$|\Psi_0\rangle$: Initial state (say, ^{40}Ar or H_2O)
 $|\Psi_f\rangle$: Final state (nuclear remnant +
 outgoing pions, kaons, etc...)



The Matrix Element

Step 2: Factorization of primary vertex



\mathcal{V} : Primary-interaction vertex

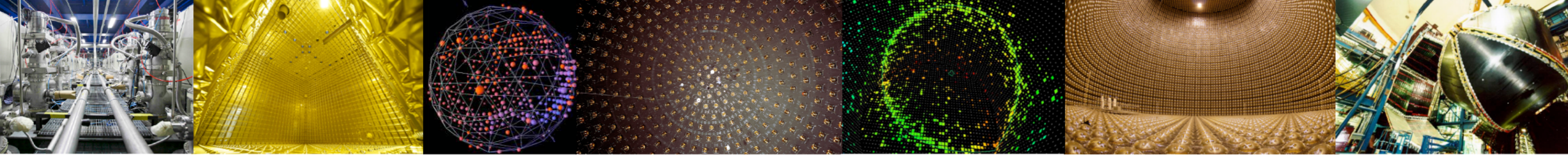
\mathcal{P} : Time evolution to produce observed final states

“Sum coherently over all possible intermediate states p' .”
-Quantum mechanics

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 = \left| \sum_{p'} \mathcal{V}(\{k\} \rightarrow \{p'\}) \times \mathcal{P}(\{p'\} \rightarrow \{p\}) \right|^2$$

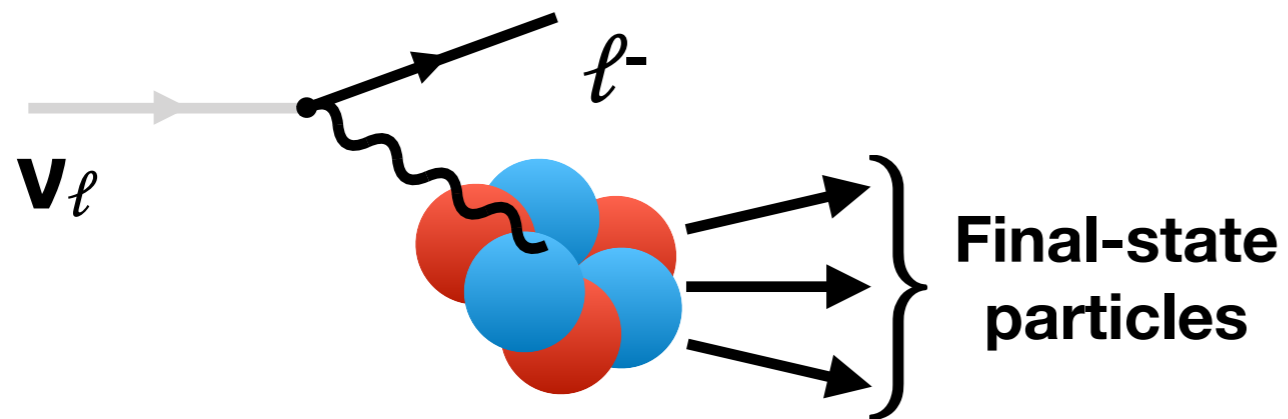
This is exact, but quite complex.

\implies Factorize the problem.



The Matrix Element

Step 2: Factorization of primary vertex



\mathcal{V} : Primary-interaction vertex

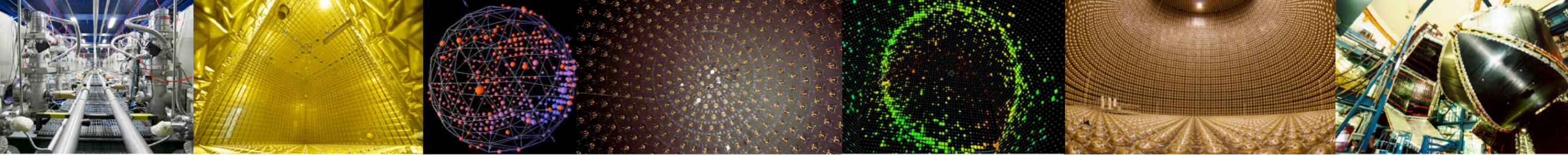
\mathcal{P} : Time evolution to produce observed final states

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

Treat the sum incoherently.

Handle constituents with theoretical care.

(Analogy to physics at LHC: similar to dressing hard-scattering cross sections with parton showers)

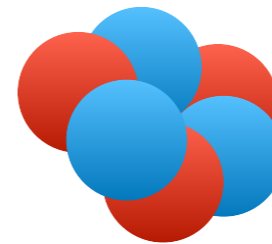


The Primary-interaction Vertex

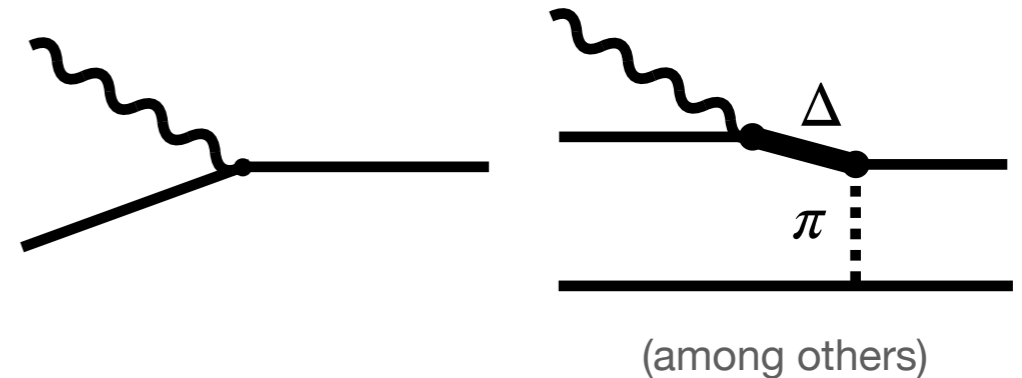
Step 3: Choose factorization scheme and DOF

- Take nucleons as initial-state DOF
- Take electroweak currents from nuclear EFT:

$$J^\mu(q) = \sum_i j_i^\mu(q) + \sum_{i<j} j_{ij}^\mu(q) + \dots$$



Spatial distribution from nuclear many-body theory: QMC. Quasi-exact.



- Choose a factorization scheme: the *impulse approximation*

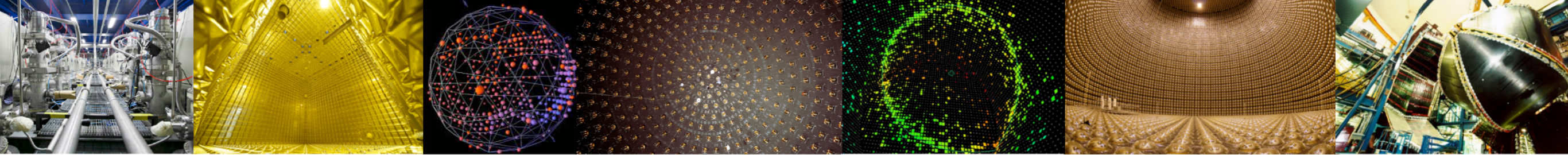
$$|\Psi_f\rangle = |\mathbf{p}\rangle \otimes |\Psi_f^{A-1}\rangle$$

“For momentum transfer $|\mathbf{q}| \gtrsim 400$ MeV, external probes resolve individual nucleons.”

Z. Tabrizi
EFT approach to
vA interactions
T15:00

N. Steinberg
Quasielastic, 2-body currents
within many-body approaches
R11:00

K. Niewczas
Single- and N-nucleon knockout
within many-body approaches
F9:00

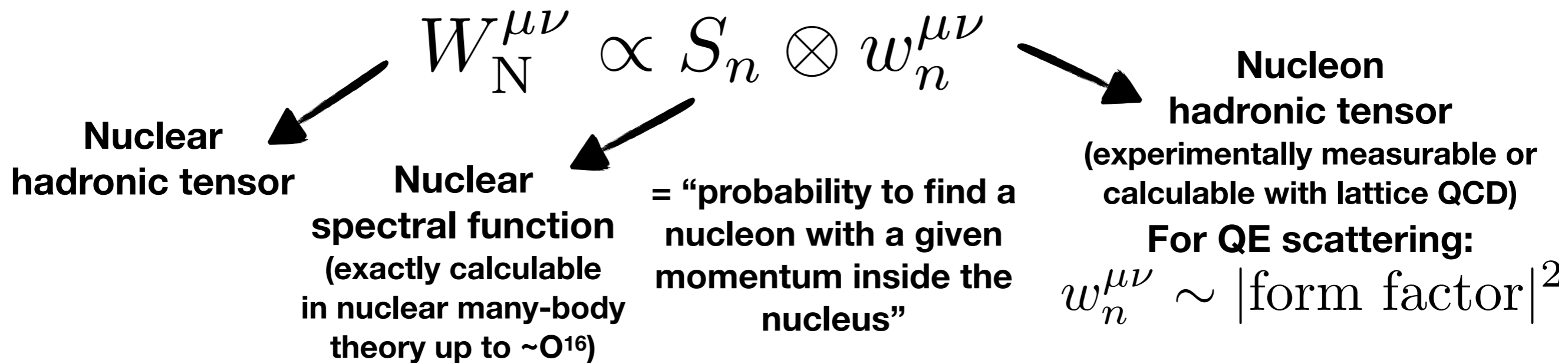


The Primary-interaction Vertex

Step 3: Choose factorization scheme and DOF

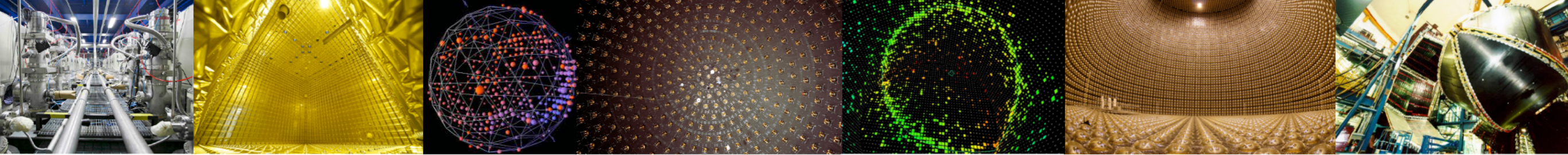
$$W_N^{\mu\nu} = \langle \Psi_0 | J^{\mu\dagger}(q) | \Psi_f \rangle \langle \Psi_f | J^\nu(q) | \Psi_0 \rangle$$

With the *impulse approximation* $|\Psi_f\rangle = |\mathbf{p}\rangle \otimes |\Psi_f^{A-1}\rangle$,



M. Wagman
Theory Uncertainties
in νA interactions
W12:00

R. Gupta
Axial form factors
from LQCD
Th9:00

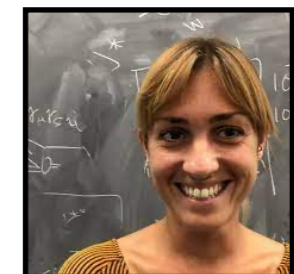
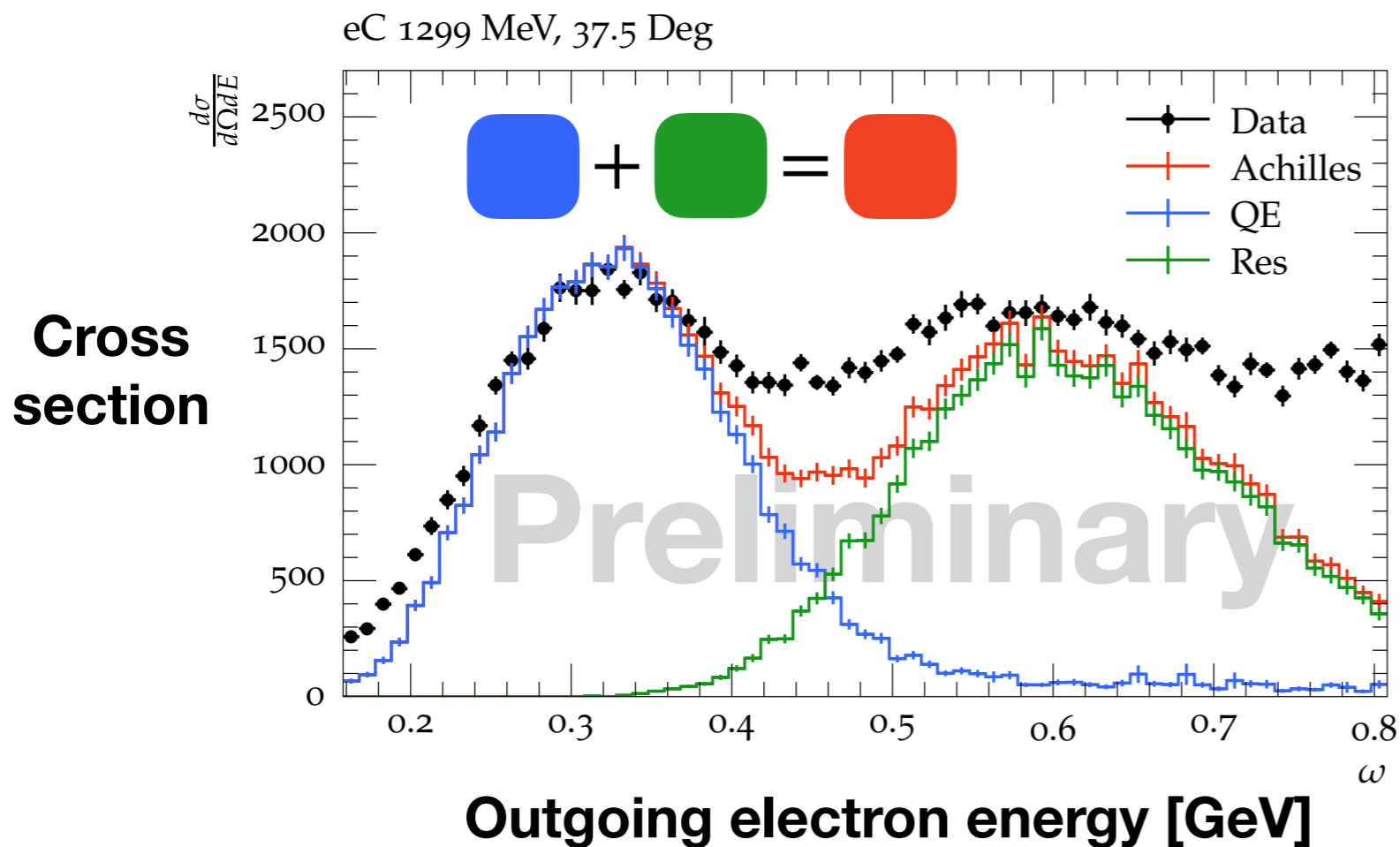
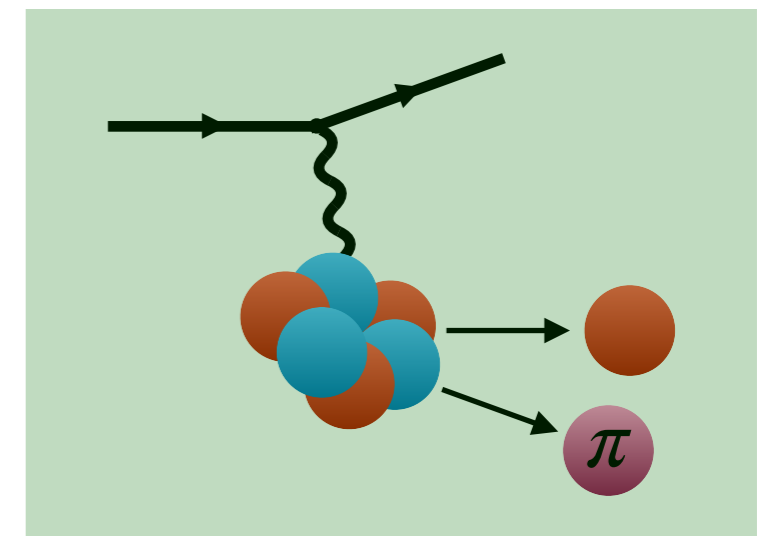
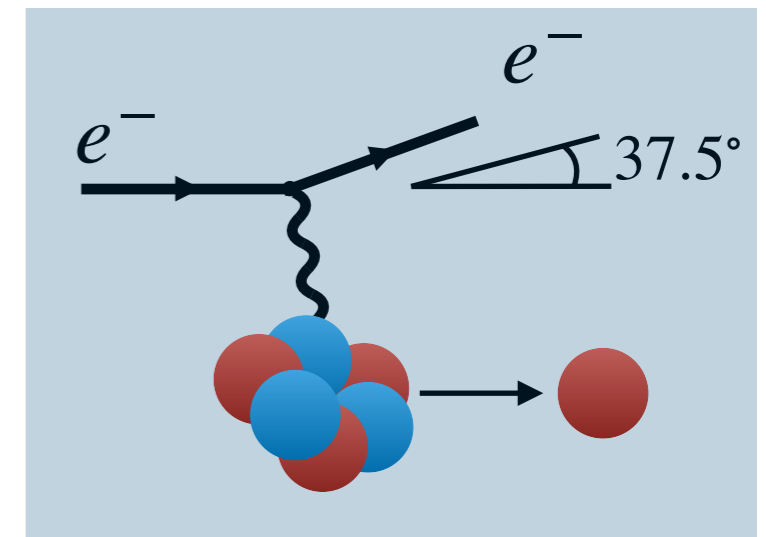


Hardonic Validation: eA-scattering

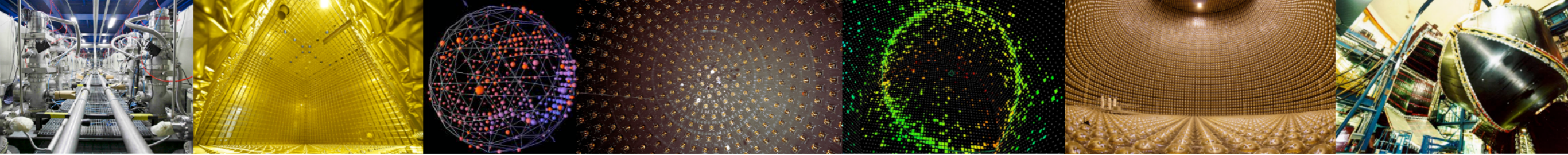
Constraining hadronic uncertainties with electron scattering

- Experimental data: $e^{12}\text{C}$ scattering at 1299 MeV, e' fixed angle 37.5°
- **New:** Achilles now includes resonance production in dynamical coupled channel (DCC) model

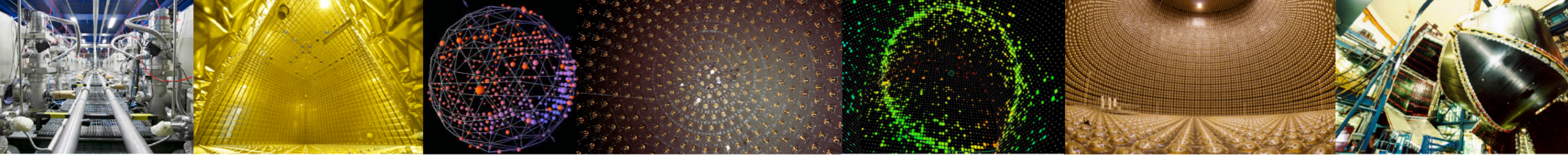
R.M. Sealock et al
Electroexcitation of the $\Delta(1232)$ in nuclei
PRL 62 (1989) 1350-1353



Noah Steinberg
Postdoc @ FNAL



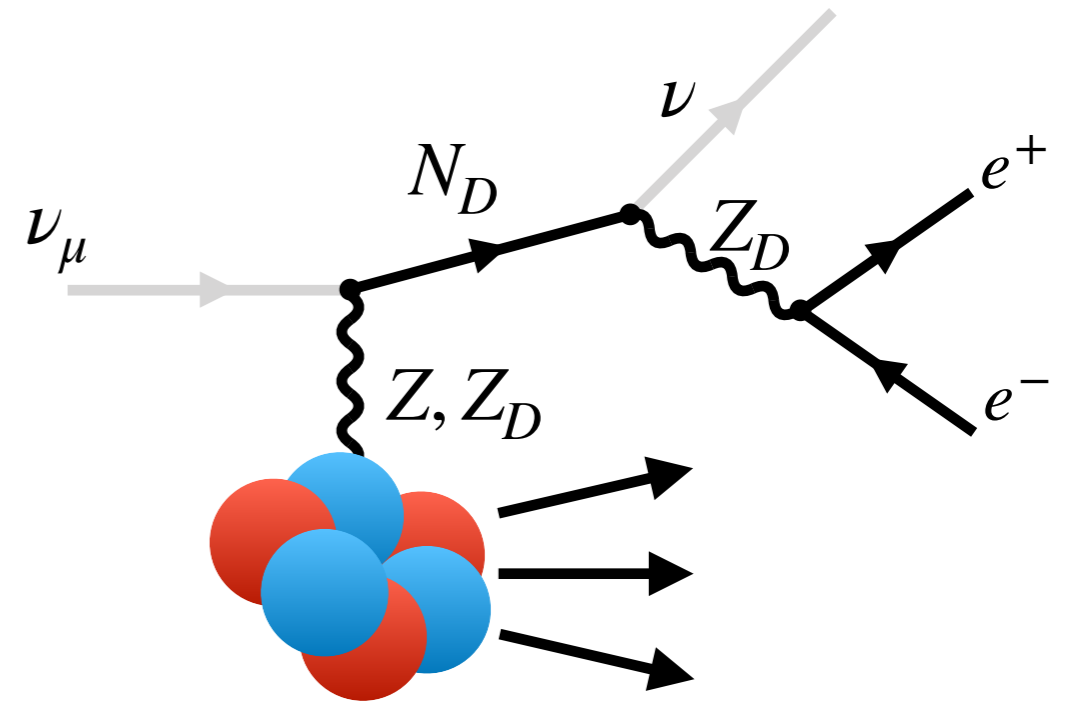
Simulating beyond the Standard Model



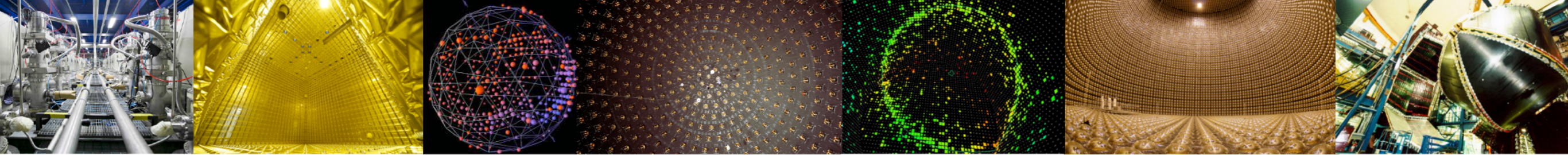
What might BSM mean?

For example, dark neutrino portal

- Suppose the existence of a
 - Dark neutrino N_D
 - Dark vector boson Z_D
- Suppose $m_{N_D} > m_{Z_D}$ so that $N_D \rightarrow Z_D + \nu_i$ is possible
- Suppose $m_{Z_D} < 2m_\mu$ so that Z_D decays to electrons, light neutrinos
- This setup can lead to excess low-energy electrons, e.g., in MiniBoone



Simulating these theories is important to SBN program and beyond

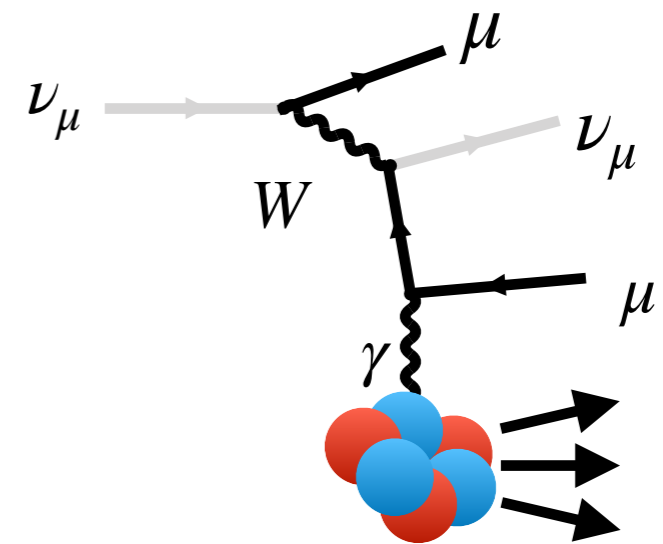
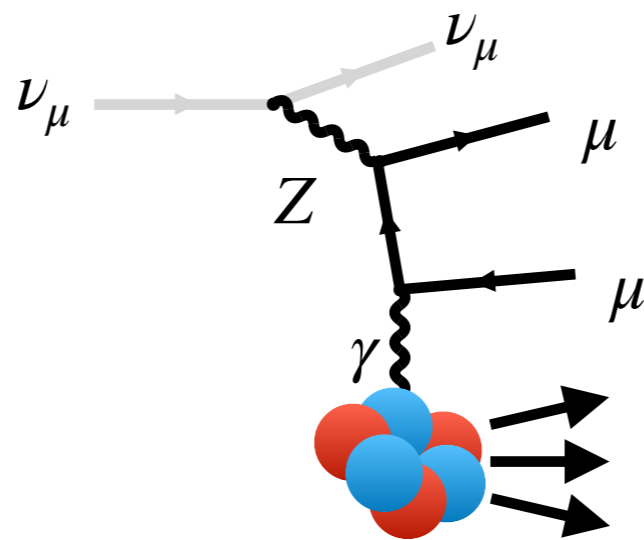


Leptonic Currents

In the SM and Beyond

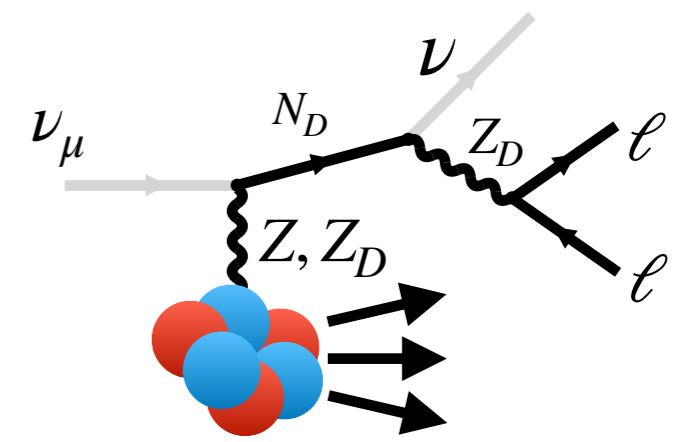
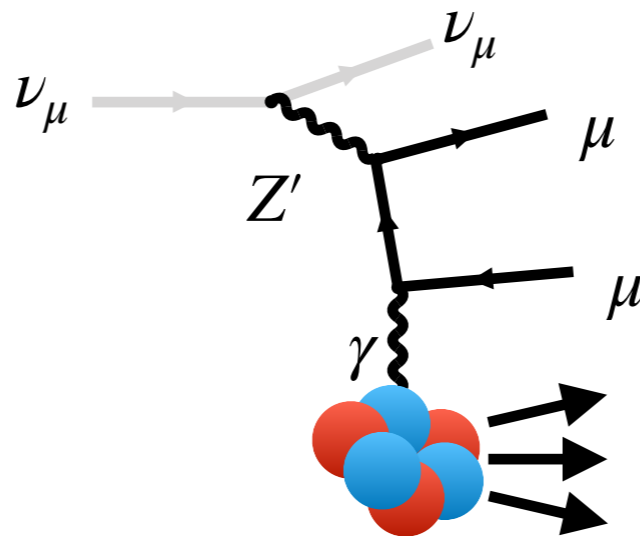
SM Tridents

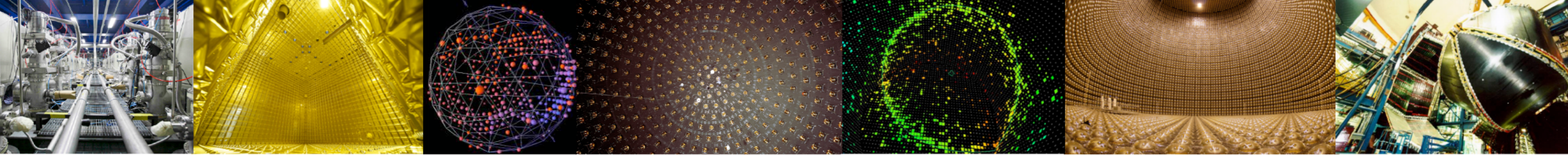
ν -induced lepton pair production



BSM Scenarios

Z' , dark neutrino portal, etc...

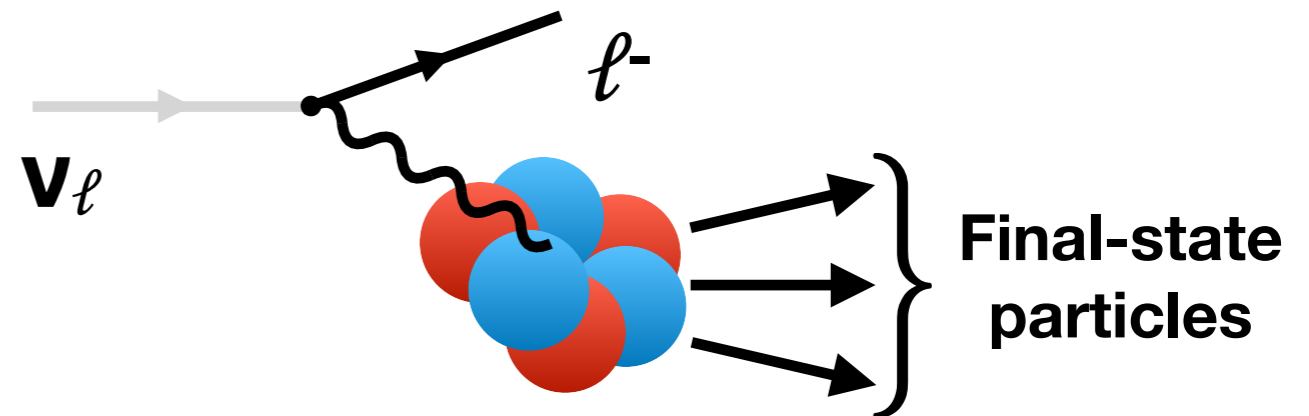




Leptonic Currents

In the SM and Beyond

$$|\mathcal{M}|^2 \propto L_{\mu\nu} \frac{1}{P^2} W^{\mu\nu}$$

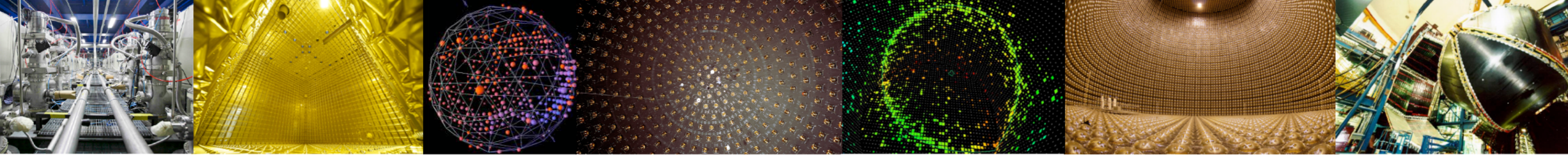


**Ex: Charged-current scattering
(unpolarized nucleus) in SM**

$$L_{\mu\nu} = 2 \left(p'_\mu p_\nu + p_\mu p'_\nu - p' \cdot p g_{\mu\nu} - i\epsilon_{\mu\nu\rho\alpha} p'^\alpha p^\beta \right)$$

Factorization of $|\mathcal{M}|^2$ becomes unwieldy for several gauge bosons (γ, Z, Z')

$$d\sigma = L_{\mu\nu}^{(\gamma\gamma)} W^{(\gamma\gamma)\mu\nu} + L_{\mu\nu}^{(\gamma Z)} W^{(\gamma Z)\mu\nu} + L_{\mu\nu}^{(Z\gamma)} W^{(Z\gamma)\mu\nu} + \dots$$



Automatic Amplitudes

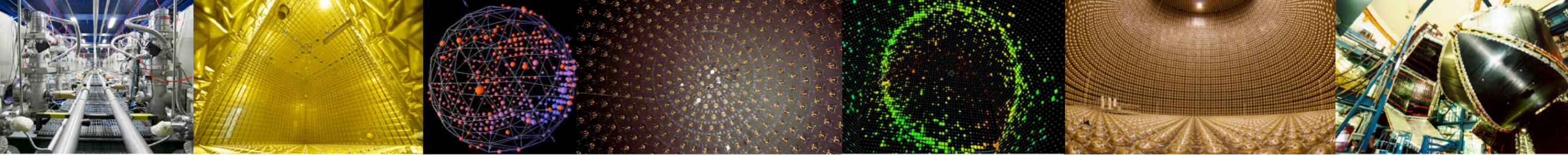
In the SM and Beyond

- Factorize the amplitude into products of currents

$$\mathcal{M} = \sum_i L_\mu^{(i)} W^{(i)\mu}$$

- Automate construction of the leptonic current in SM, BSM
- Build cross section from amplitudes

$$d\sigma \sim \left| \sum_i L_\mu^{(i)} W^{(i)\mu} \right|^2$$



Automatic Amplitudes

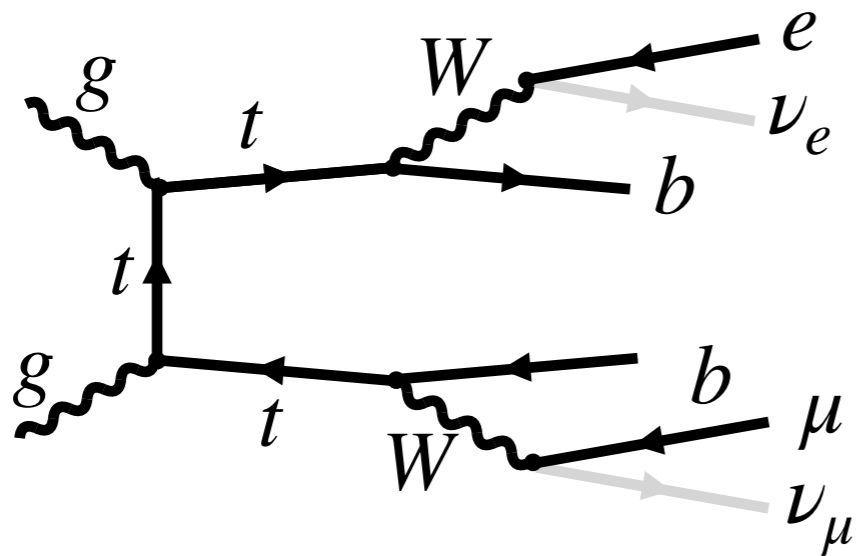
In the SM and Beyond

Berends and Giele
Nucl.Phys.B 306 (1988) 759-808

S. Höche et al.
Eur.Phys.J.C 75 (2015)
 [arXiv:1412.6478]

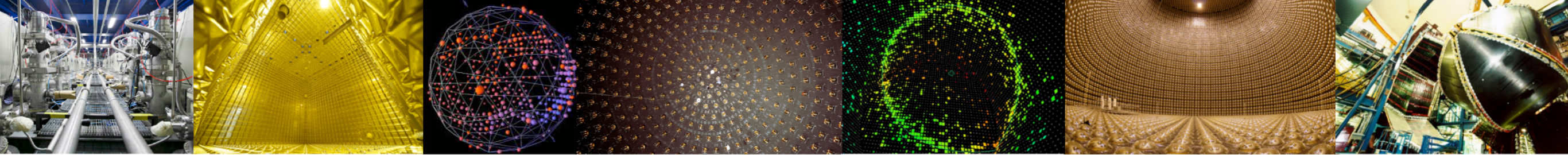
Context: $t\bar{t}$ production at LHC

$$gg \rightarrow t\bar{t} \rightarrow b\bar{b}e\nu_e\mu\nu_\mu$$



Keys for success

1. Automatic generation of tree-level amplitudes
2. Preservation of spin correlations in heavy decay cascades
3. Automatic generation of n-body phase space



Automatic Leptonic Currents

In the SM and Beyond

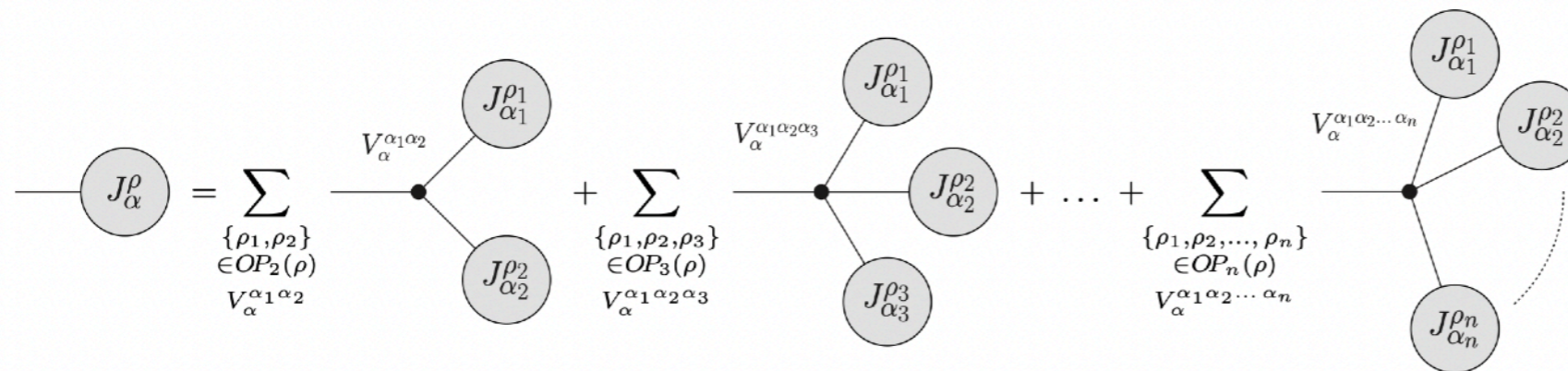
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Eur.Phys.J.C 75 (2015)
[arXiv:1412.6478]

J. Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]

- Recursive definition for (off-shell) currents:

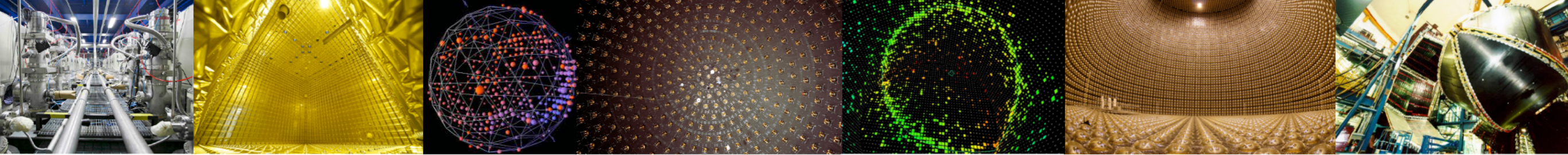
- (current) = (propagator) \times \sum (vertex) \times (sub-currents)



- Example:

$$(\gamma^\mu)_{ab} \bar{\psi}_a \psi_b = \mu \text{---} \left(\gamma^\mu \right) \text{---} \psi$$





Automatic Leptonic Currents

Leptonic limitations (current Achilles implementation)

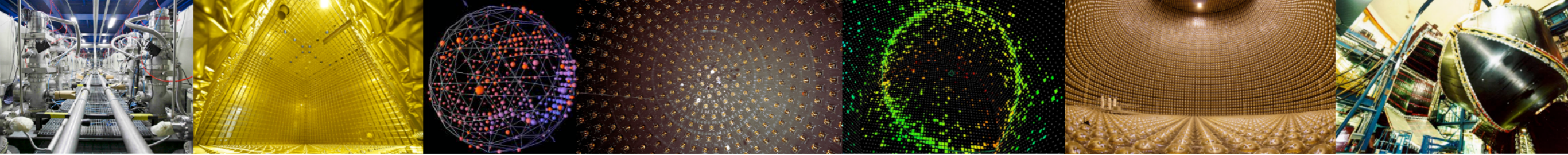
- ▶ Scalar, spin-1/2, or spin-1 particles
 - Spin $> 1 \implies$ Write down/implement relevant external states and propagators
- ▶ Spin-1 probes of nucleus
 - Spin $\neq 1 \implies$ Expand nuclear model with relevant form factors
- ▶ Color-singlet particles
 - Color-charged particles: breaks assumed description via hadronic DOF at low energies
 - Most (all?) realistic BSM models are neutral under QCD

Berends and Giele
Nucl.Phys.B 306 (1988) 759-808

S. Höche et al.
Eur.Phys.J.C 75 (2015)
[arXiv:1412.6478]

J. Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]





Preserving spin correlations

In the SM and Beyond

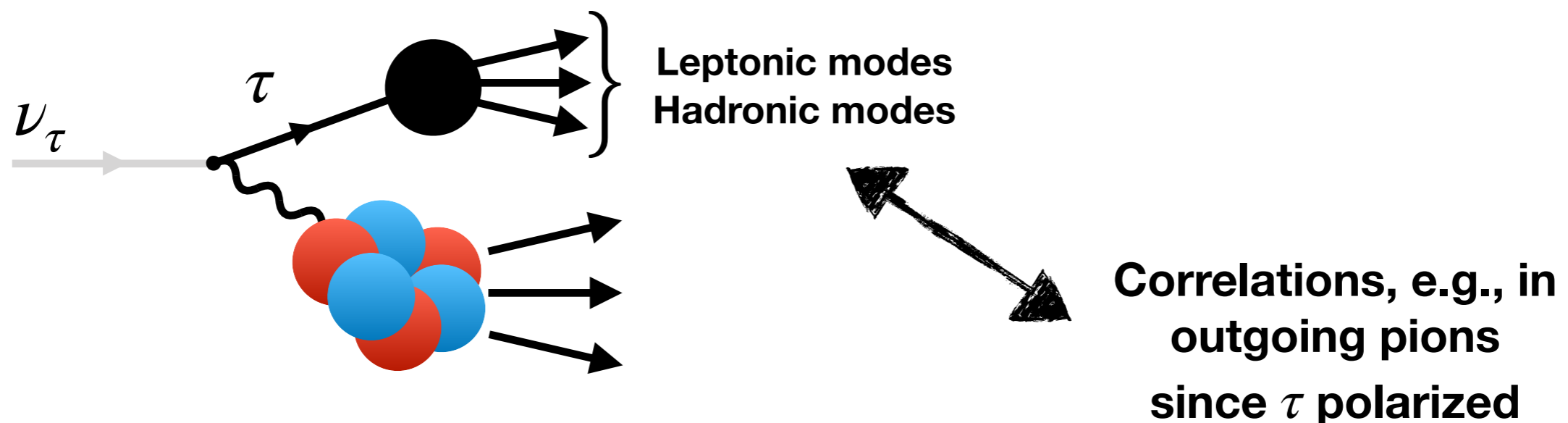
- Examples:
 - Top-quark decays in LHC physics
 - τ decays in neutrino scattering

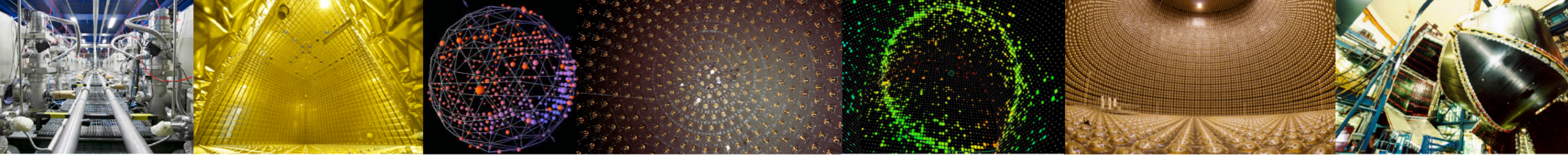
J. Collins
Nucl.Phys.B 304 (1988)794-804

S. Höche et al.
Eur.Phys.J.C 75 (2015)
[arXiv:1412.6478]

P. Richardson
JHEP 11 (2001) 029
[arXiv:hep-ph/0110108]

J. Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]





Preserving spin correlations

In the SM and Beyond

- Big idea: Momenta are generated according to

$$\left(\rho_{\kappa_1 \kappa_1'}^1 \rho_{\kappa_2 \kappa_2'}^2 \right) \times \left(\mathcal{M}_{\kappa_1 \kappa_2; \lambda_1 \dots \lambda_n} \mathcal{M}_{\kappa_1' \kappa_2'; \lambda_1' \dots \lambda_n'}^* \right) \times \prod_i D_{\lambda_i, \lambda_i'}^i$$

Incoming spin-density matrices

(Amplitude)²

Outgoing-particle decay matrix

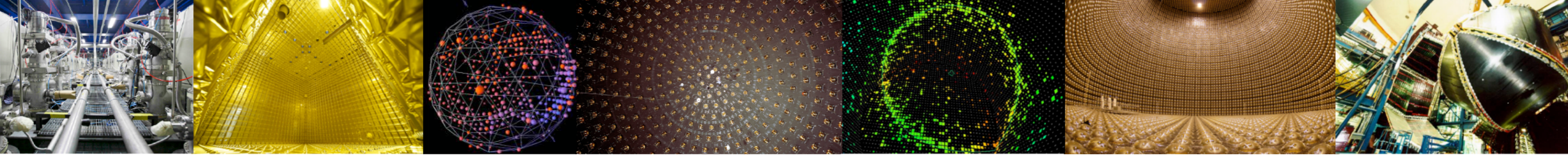
- Decay unstable particles randomly
- Develop chain of decays until final particles are stable
- Recursively determine outgoing-particle decay matrix, constrained by conservation of probability

J. Collins
Nucl.Phys.B 304 (1988)794-804

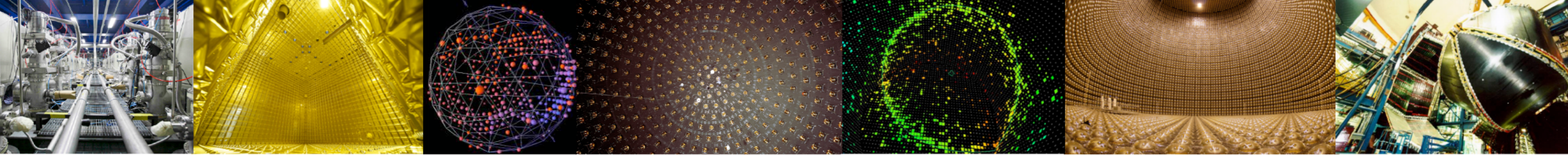
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P. Richardson
JHEP 11 (2001) 029
[arXiv:hep-ph/0110108]

J. Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]



Examples



Neutrino tridents $\nu_{\mu} {}^{12}\text{C} \rightarrow \nu_{\mu} e^{+} e^{-} X$

Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]

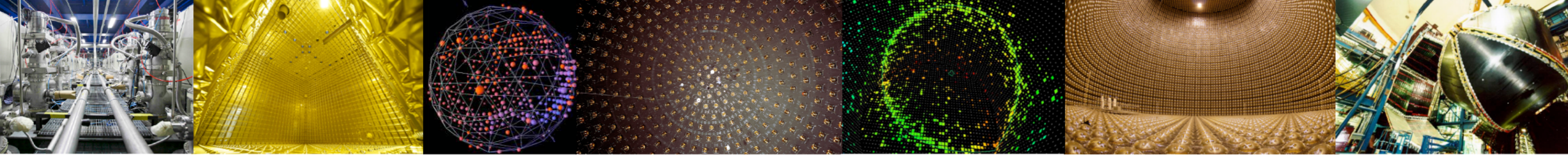
Example of the pipeline using Achilles

Motivation:

- Proof-of-concept involving interference between interactions with γ , Z .
- Proof-of-concept for generic BSM interface
- Important background for BSM explanations of the MiniBooNE excess.
- Demonstrate uses of tools developed by LHC event generation community: Sherpa, Comix, FeynRules, UFO files

Results

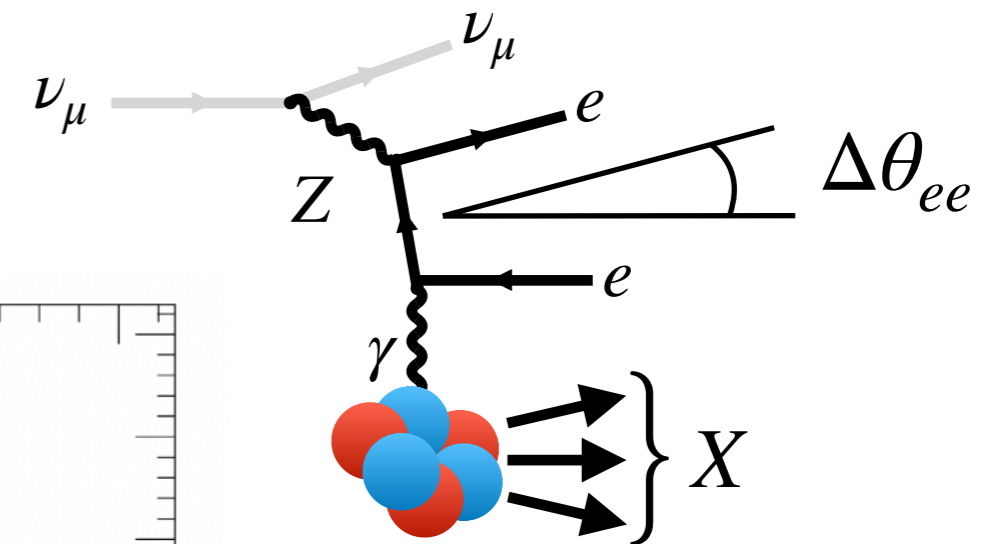
- First fully differential results for trident production in the quasielastic region



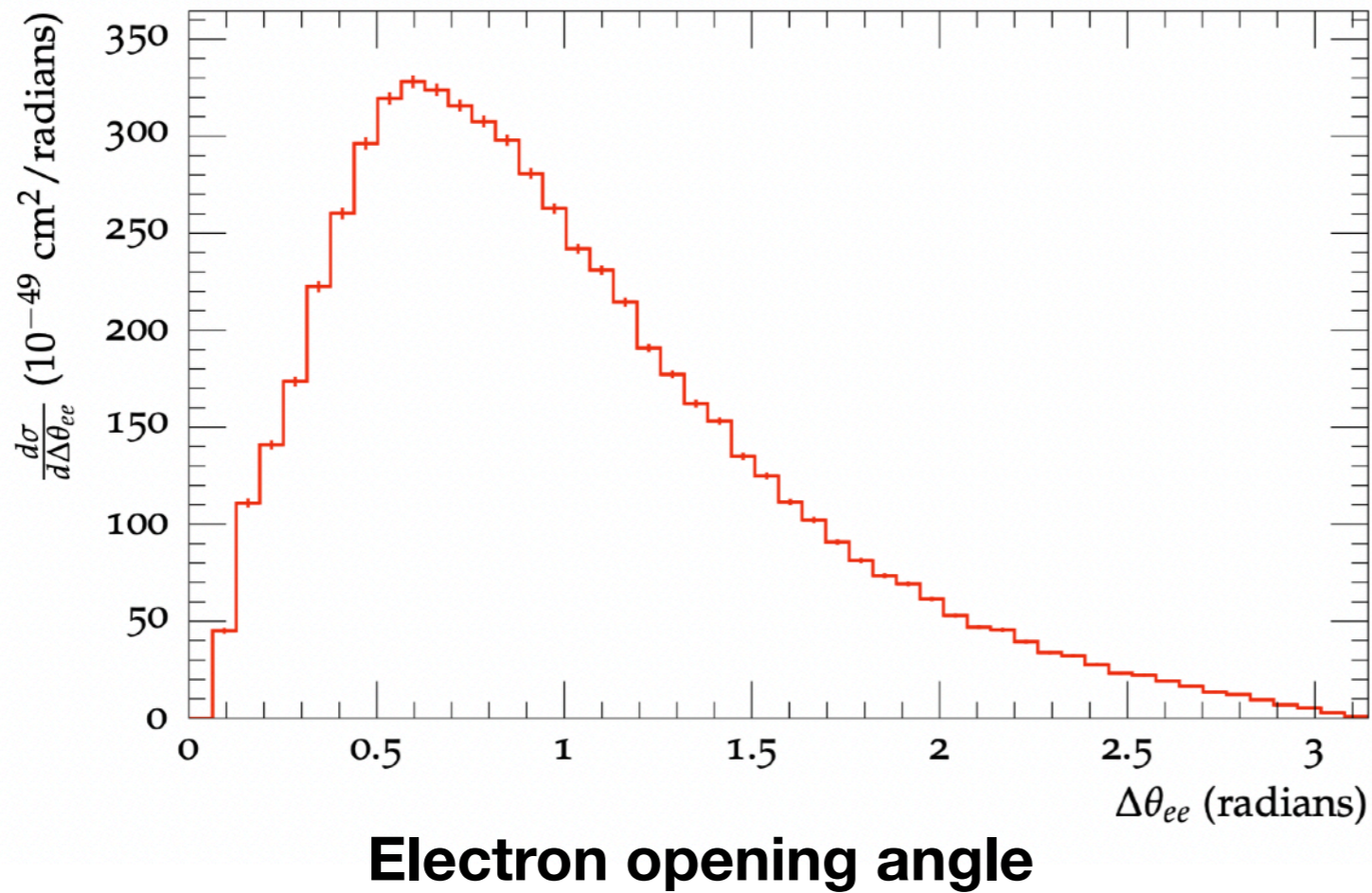
Neutrino tridents $\nu_{\mu} {}^{12}\text{C} \rightarrow \nu_{\mu} e^{+} e^{-} X$

Isaacson et al.
PRD 105 (2022) 9, 096006
[arXiv:2110.15319]

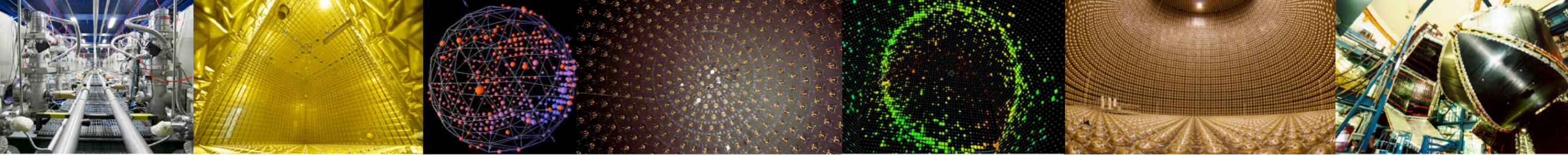
Example of the pipeline using Achilles



Cross section



Paper also reports energy distributions for outgoing electrons



Correlated τ decays

Example of the pipeline using Achilles

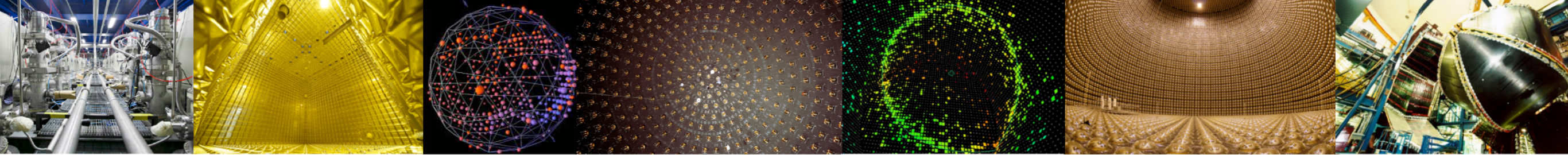
Isaacson et al.
PRD 108 (2023) 9, 093004
[arXiv:2303.08104]

Motivation:

- DUNE: $\mathcal{O}(100s)$ ν_τ events / year
- Polarized $\tau \implies$ final-state correlations
- Standard Model predicts:
 - τ polarization perpendicular to the lepton-scattering plane *vanishes*
 - τ polarization components within the lepton-scattering plane do not vanish
- Other generators have often treated ν_τ interactions as for $\nu_e, \nu_\mu \rightarrow$ “outgoing τ as LH only”

Results

- First fully differential predictions for ν_τ scattering at DUNE energies, including all spin correlations and all τ decay channels
- Calculated using generic interface between Achilles and Sherpa
- Correlations between production and decay are *automatically* maintained



Correlated τ decays

Isaacson et al.
PRD 108 (2023) 9, 093004
[arXiv:2303.08104]

Example of the pipeline using Achilles

Momentum Fraction Distributions

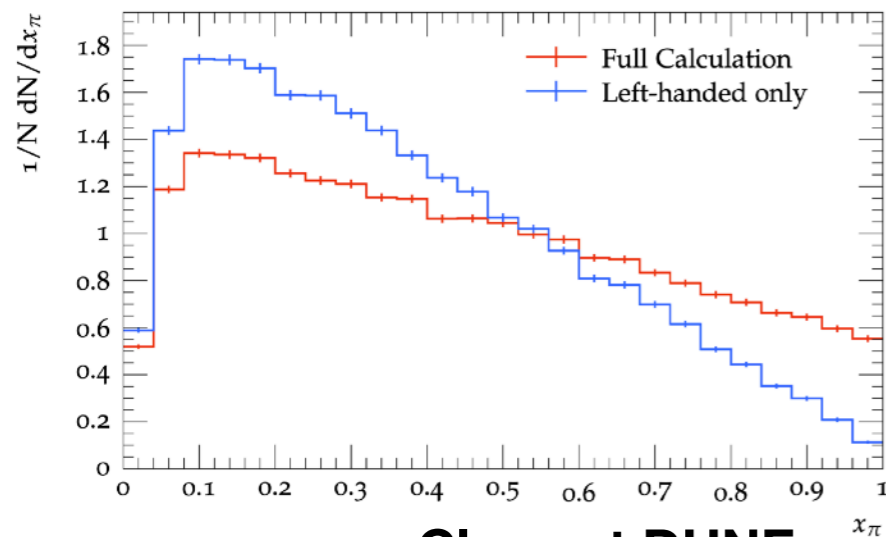
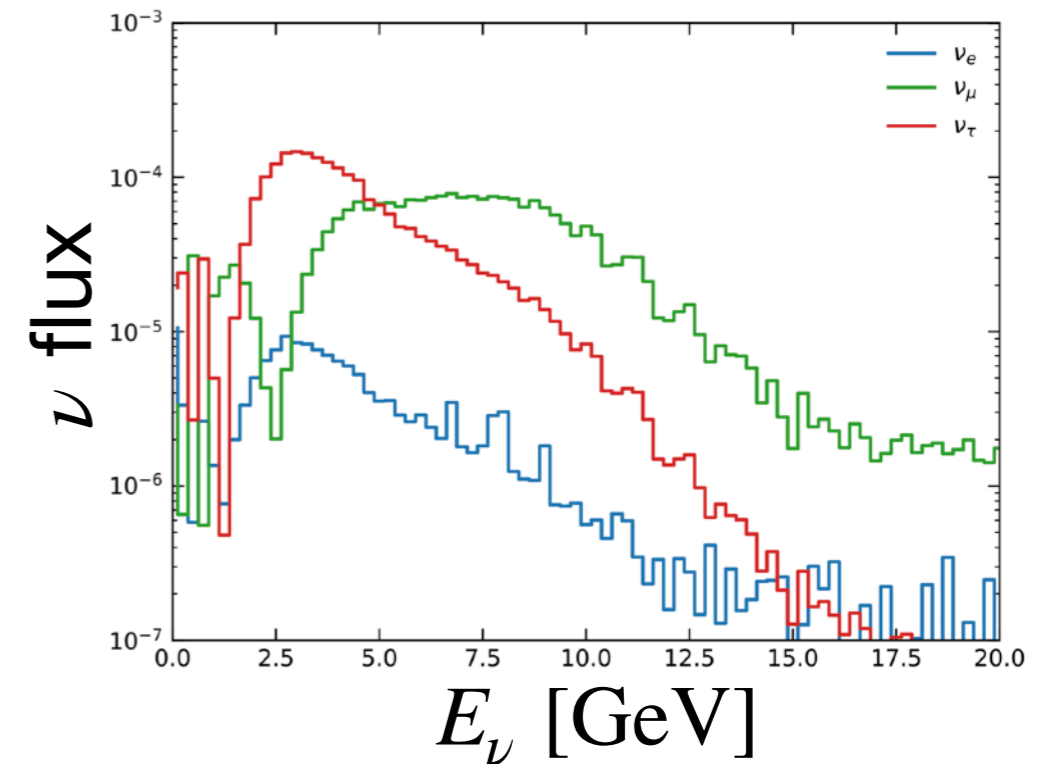
- Benchmarking done against analytic results in collinear ($p_\tau \rightarrow \infty$) limit, monochromatic beams
- Final results calculated using realistic DUNE fluxes

$$\frac{1}{N} \frac{dN}{dx_i}$$



Momentum fraction

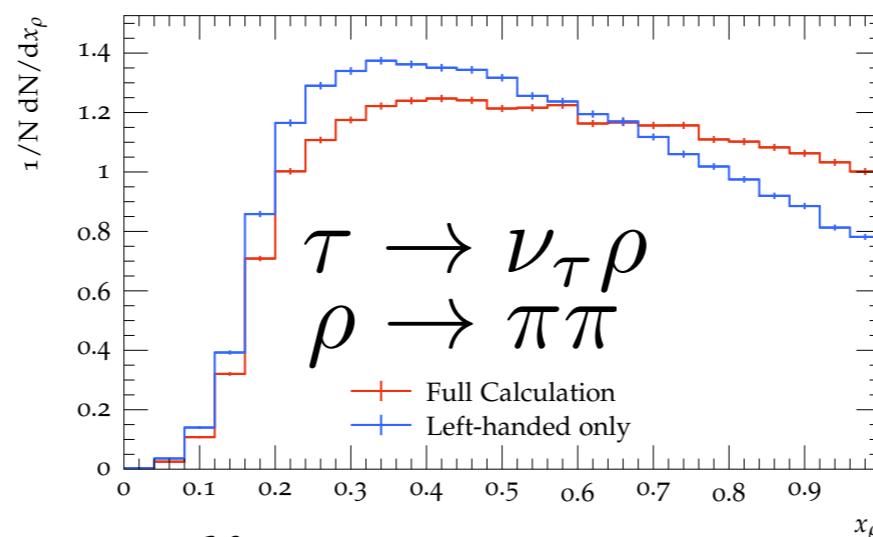
$$x_i = E_i/E_\tau$$



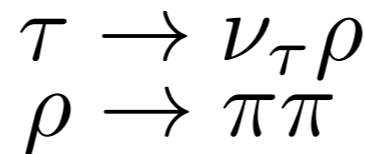
x_π

Clean at DUNE

$\mathcal{B}(1\pi) \sim 10\%$

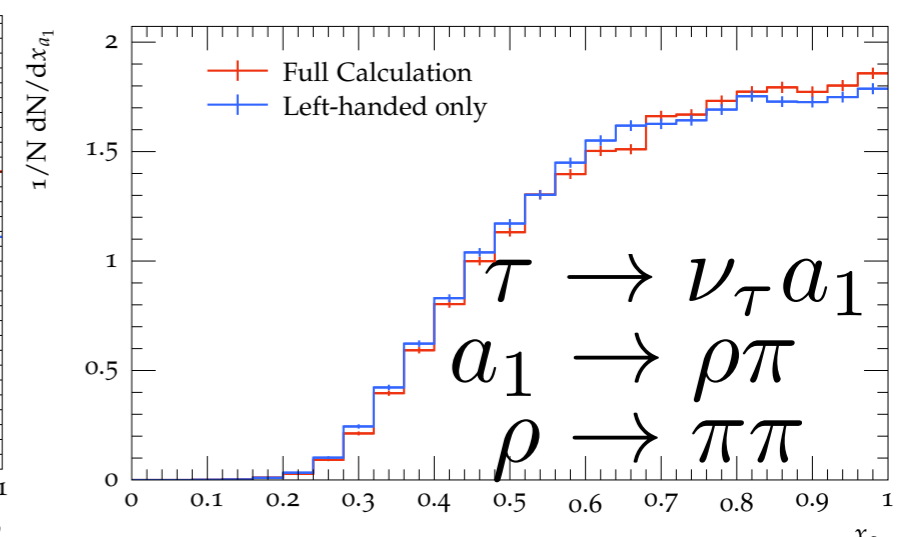


x_ρ

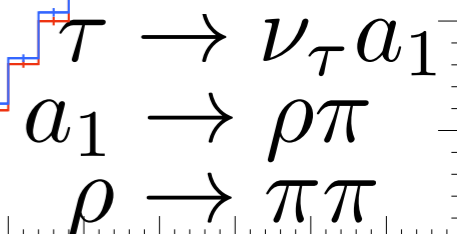


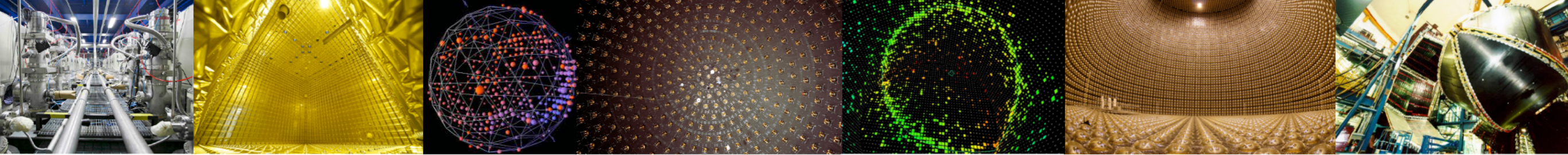
Full Calculation
Left-handed only

$\mathcal{B}(2\pi) \sim 25\%$



x_{a_1}





Neutrino Dark Sector

Example of the pipeline using Achilles

- Simulation of full phase space including spin correlations
- Allows for separation of Dirac and Majorana cases

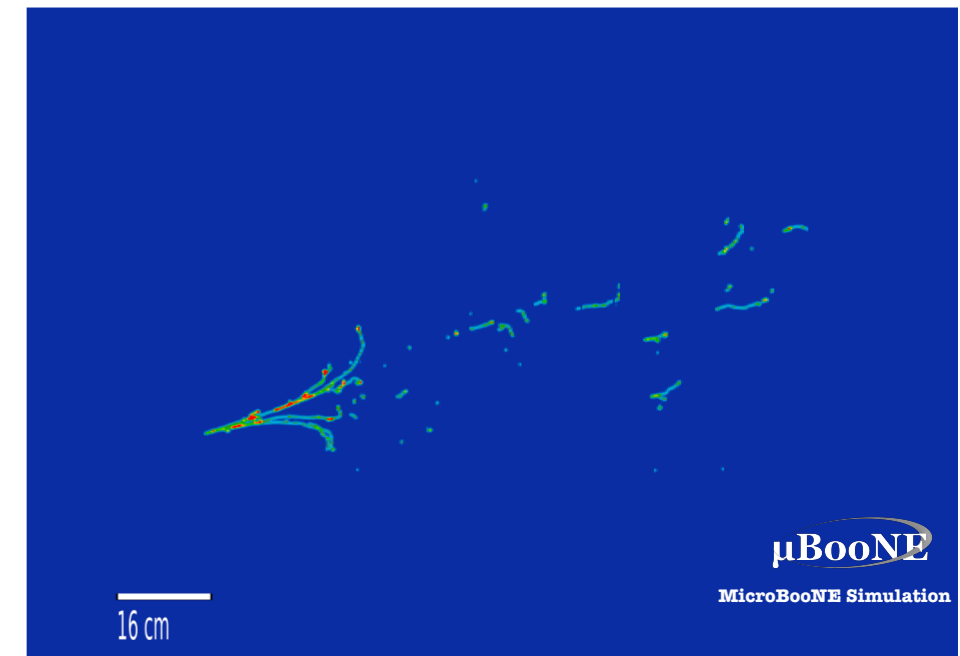
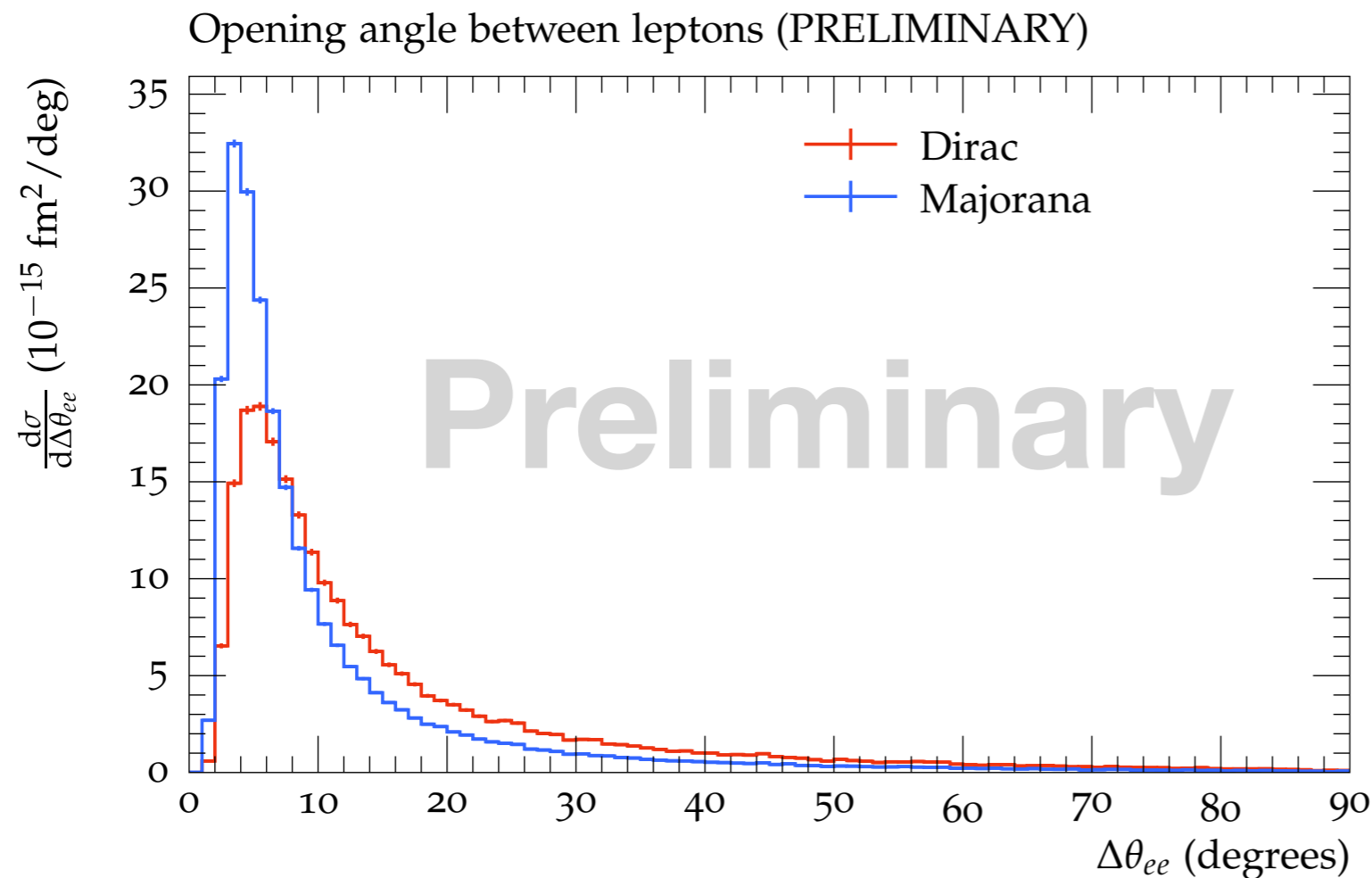
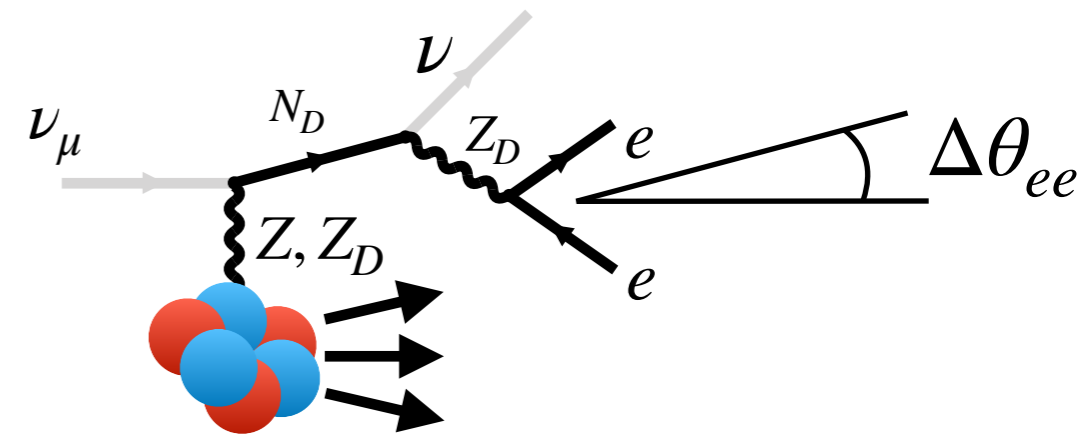
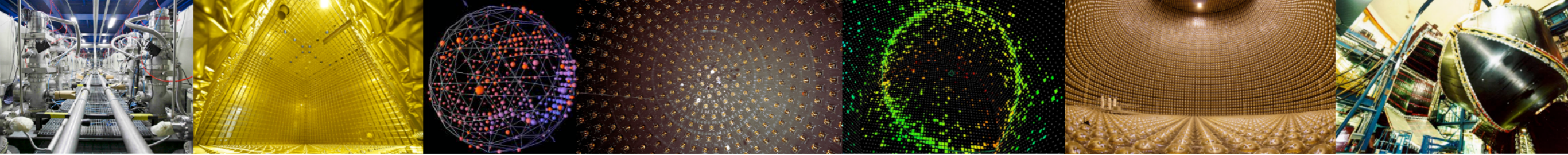


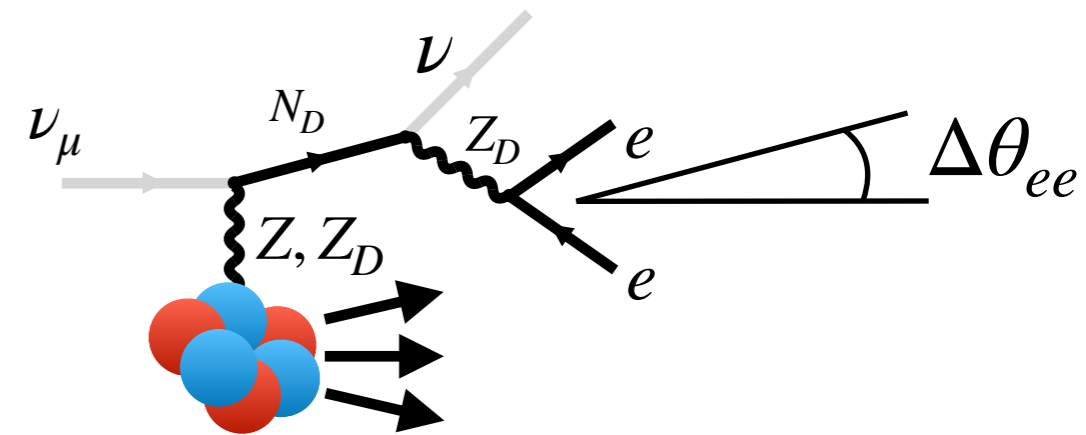
Image courtesy MicroBooNE using Achilles



Neutrino Dark Sector

Example of the pipeline using Achilles

- Simulation of full phase space including spin correlations
- Allows for separation of Dirac and Majorana cases



Energy of leading lepton (PRELIMINARY)

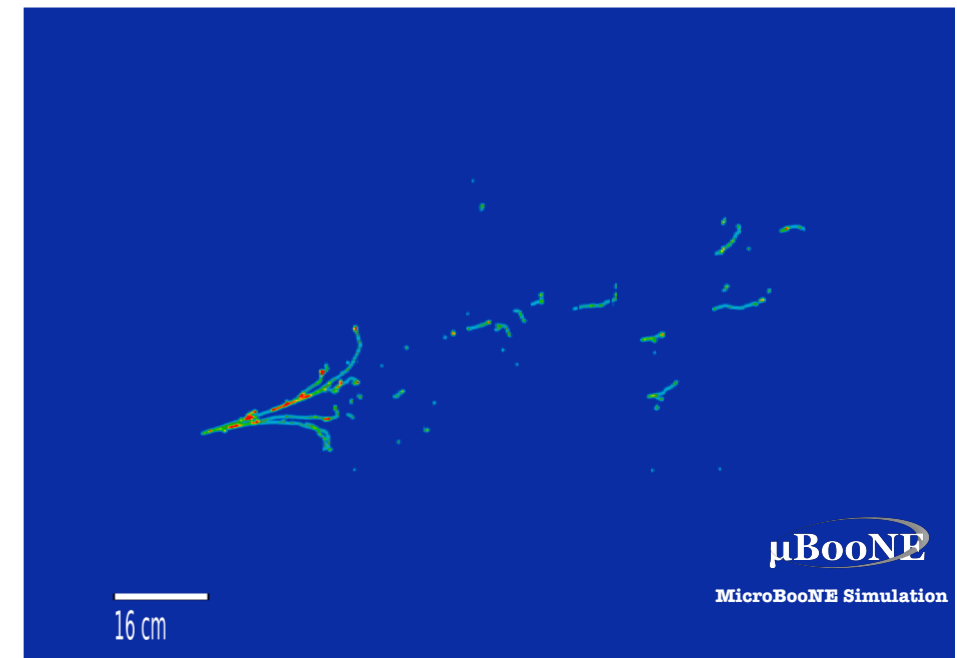
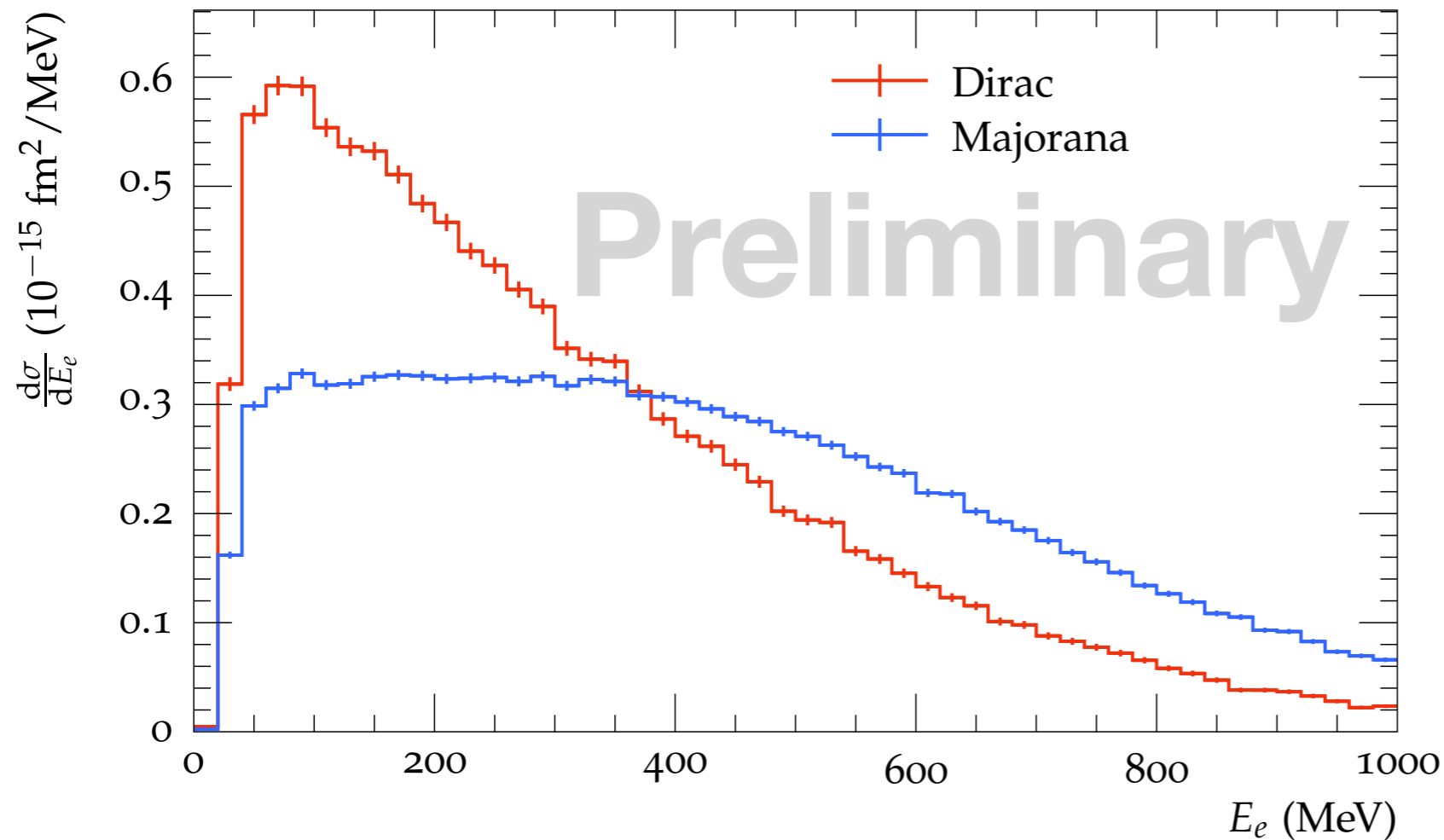
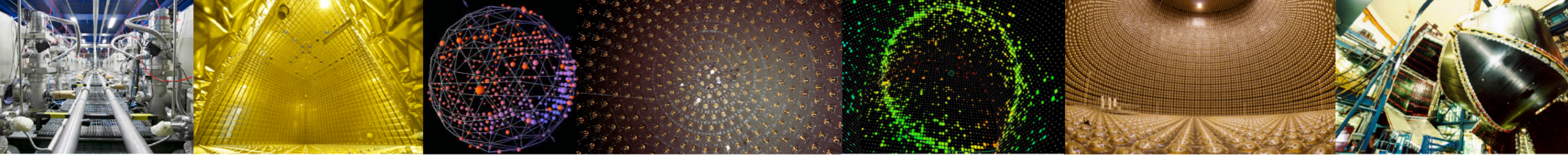


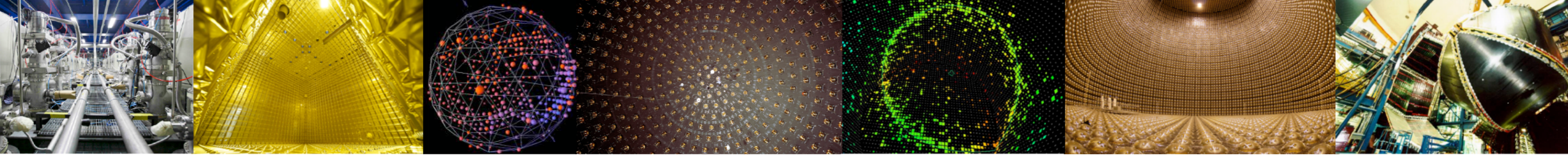
Image courtesy MicroBooNE using Achilles



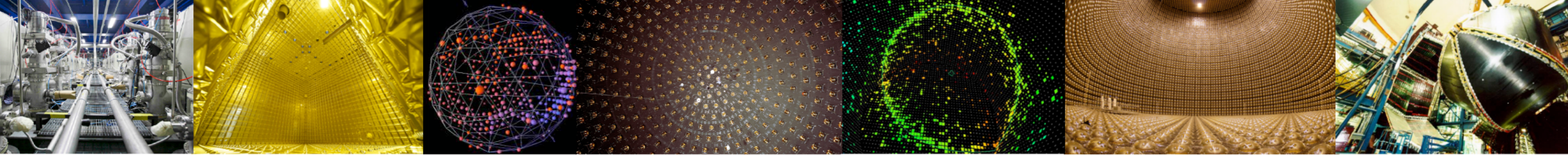
Summary / Conclusions

Standardizing for Success

- **Leptonic currents**
 - SM and BSM models have many interactions
 - Leverage existing implementations (e.g., Sherpa, Comix)
 - Ensures common definition (e.g., of a BSM model) across generators
- **Hadronic currents**
 - νA scattering involves many hadronic/nuclear inputs
 - Desirable to constrain as many “moving pieces” as possible using LQCD, *ab initio* nuclear many-body theory
- **Hadronic modeling inevitable in some areas**
 - Must be able to quantify uncertainty from “reasonable” variations
 - E.g., in situ parameter variation for uncertainty in primary-interaction vertex
 - Mention connections to vector of weights in NuHepMC standard
- **Goal:** rapid iteration of comparisons between predictions from different generators



Backup



Hadronic currents

From *ab initio* nuclear theory and lattice QCD

$$W^\mu = \langle \psi_f^A | J^\mu(q) | \psi_0^A \rangle$$

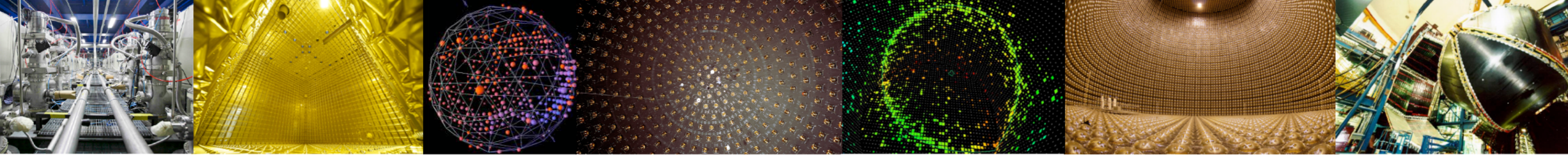
$$\rightarrow \sum_{k,i} \left[\langle \psi_f^{A-1} | \otimes \langle k | \right] | \psi_0^A \rangle \times \langle p + q | j_i^\mu(q) | k \rangle$$

Overlap with final nuclear state in impulse approximation

- Spectral function
 $\sim |\text{overlap}|^2$
- Calculable in *ab initio* nuclear many-body theory

Single-nucleon form factor

- Calculable in LQCD
- LQCD calculations are quickly approaching full systematic control



Achilles: Comparison to experiment

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

J. S. O'Connell *et al.*, *Phys. Rev. C* **35**, 1063 (1987).
 R. M. Sealock *et al.*, *Phys. Rev. Lett.* **62**, 1350 (1989).
 D. Zeller, Investigation of the structure of the C-12 nucleus by high-energy electron scattering, Other thesis, Karlsruhe University, 1973.

**Inclusive eC
hadronic cross
section**

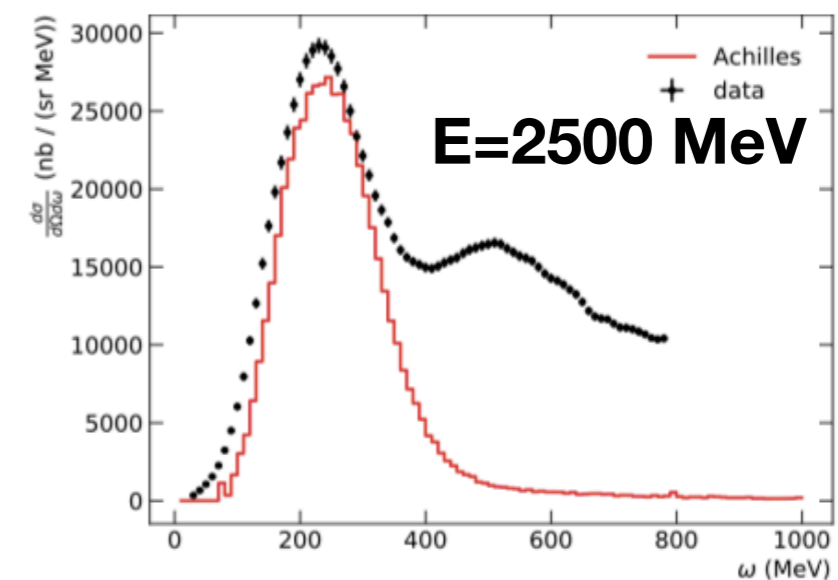
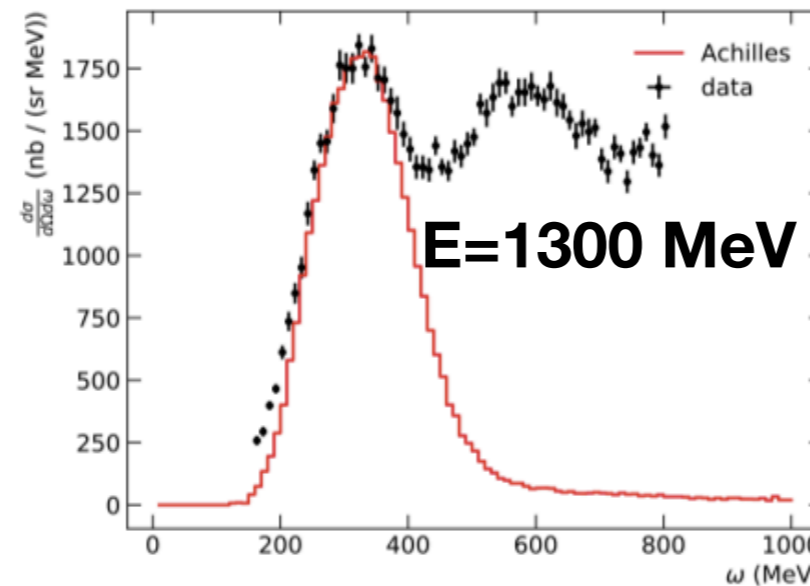
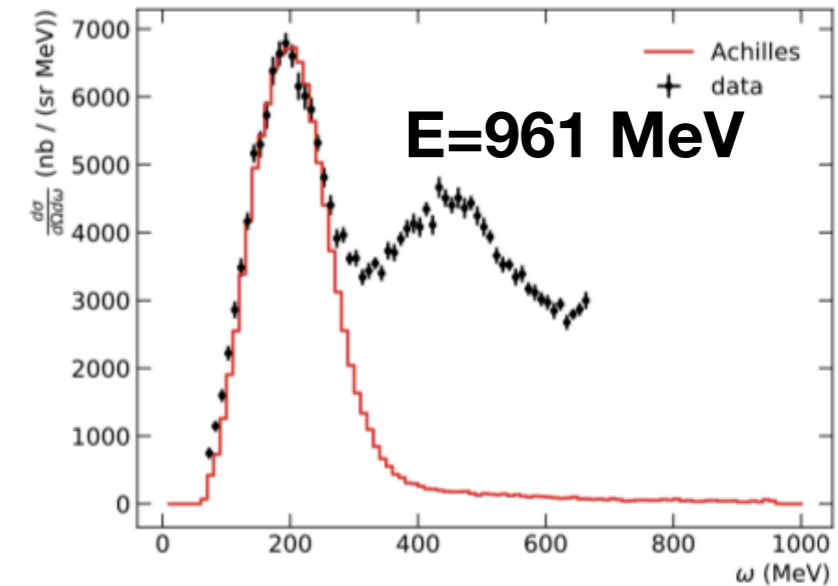
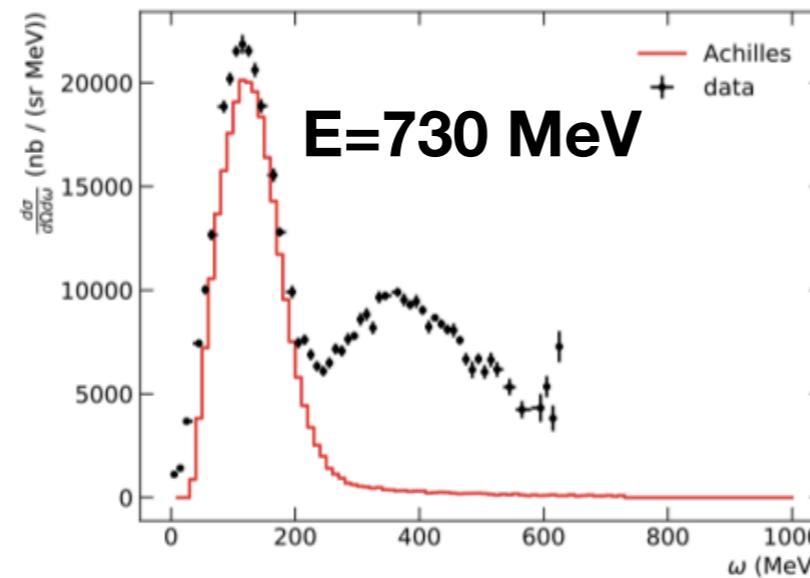
$$\frac{d\sigma}{d\Omega d\omega}$$

**Fixed outgoing
electron angle**

$\theta = 37^\circ$ to

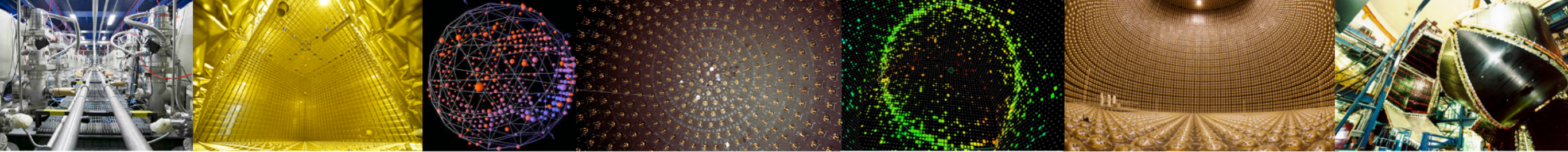
**match
experimental
settings**

**Differential in
outgoing electron
energy ω**



Beyond firsts peak: Neglected MEC and resonance contributions

Good agreement = Validation of initial model for QE interaction



Achilles: Comparison to experiment

CLAS and $e4\nu$ collaborations
Nature 599 (2021) 7886, 565-570

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

- Inclusive e-C hadronic cross section
- Analysis by $e4\nu$ to mimic kinematic setup for QE νA scattering

$$E_{QE} = \frac{2m_N \epsilon + 2m_N E_\ell - m_\ell^2}{2(m_N - E_\ell + p_\ell \cos \theta_\ell)}$$

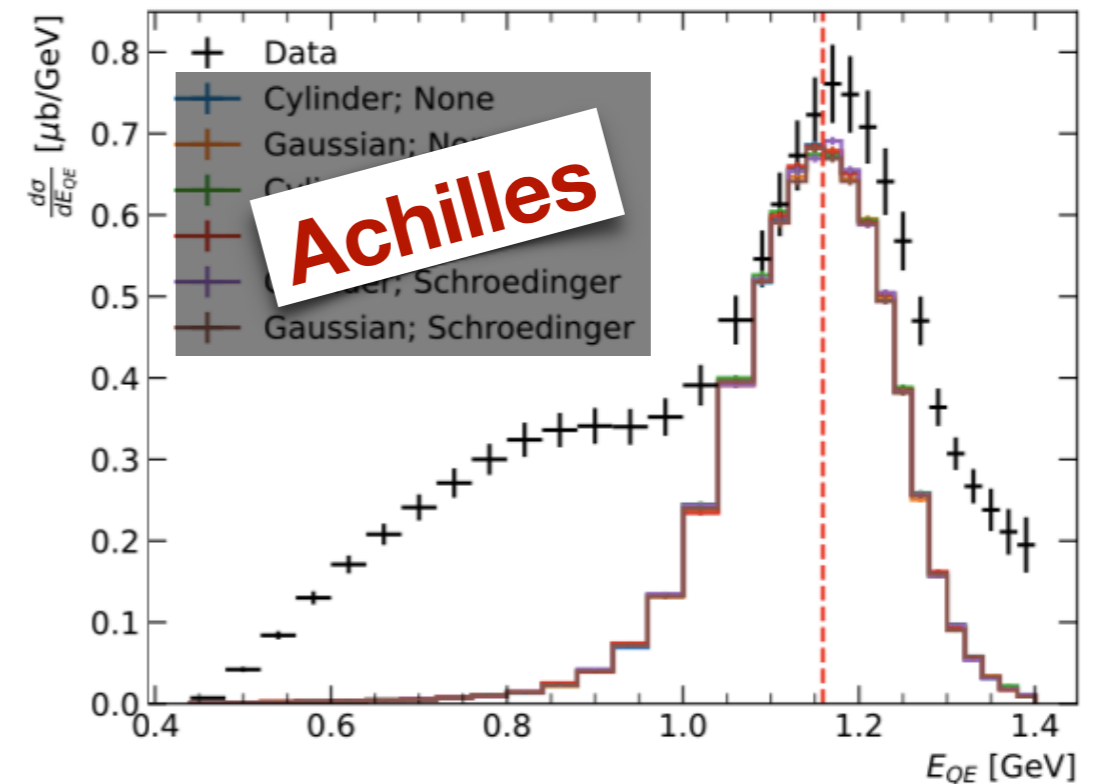
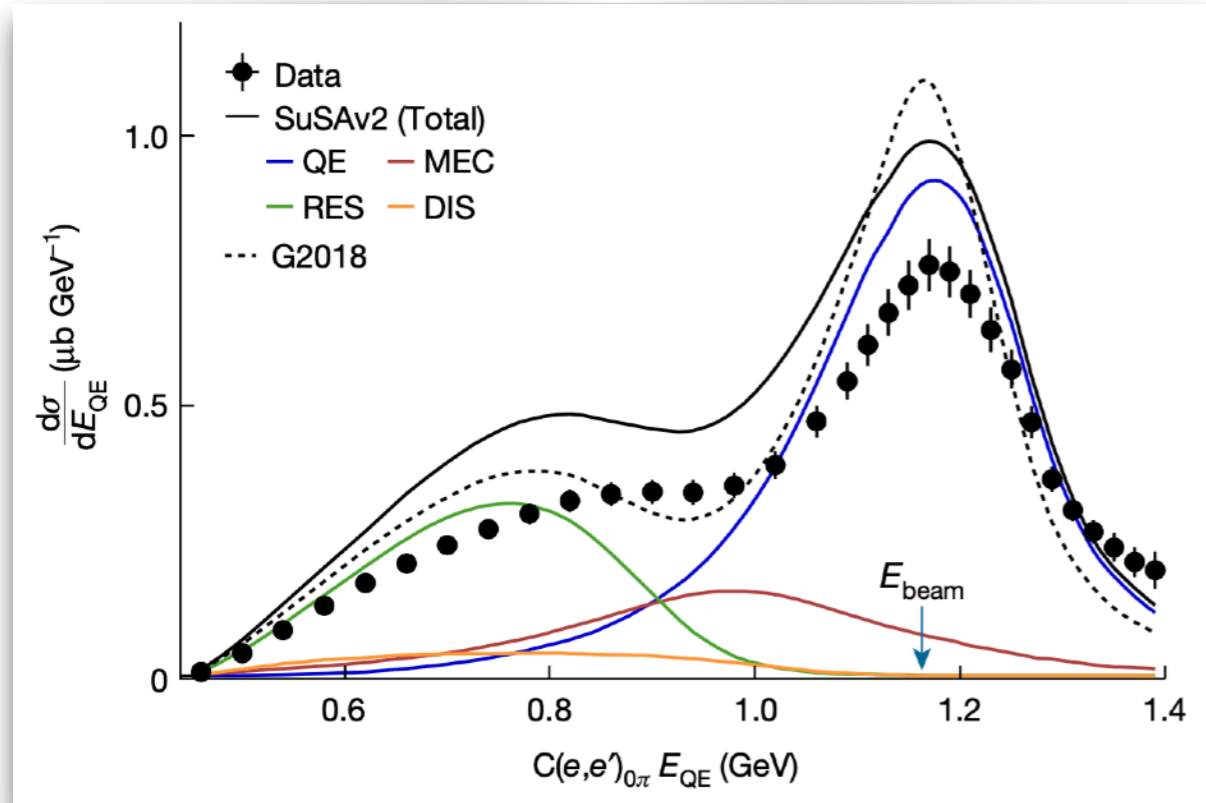
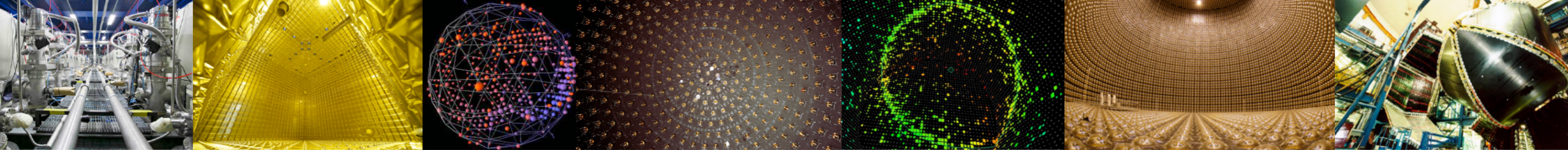


FIG. 4: Comparison of the quasielastic energy reconstructed for an electron beam of 1159 MeV. Data is taken from Ref. [69]. The definition of E_{QE} can be found in Eq. 31. The red dashed vertical line marks the true beam energy.

- Low E_{QE} : MEC and resonance contributions
- High E_{QE} : interference effects (neglected)



Achilles: Comparison to experiment

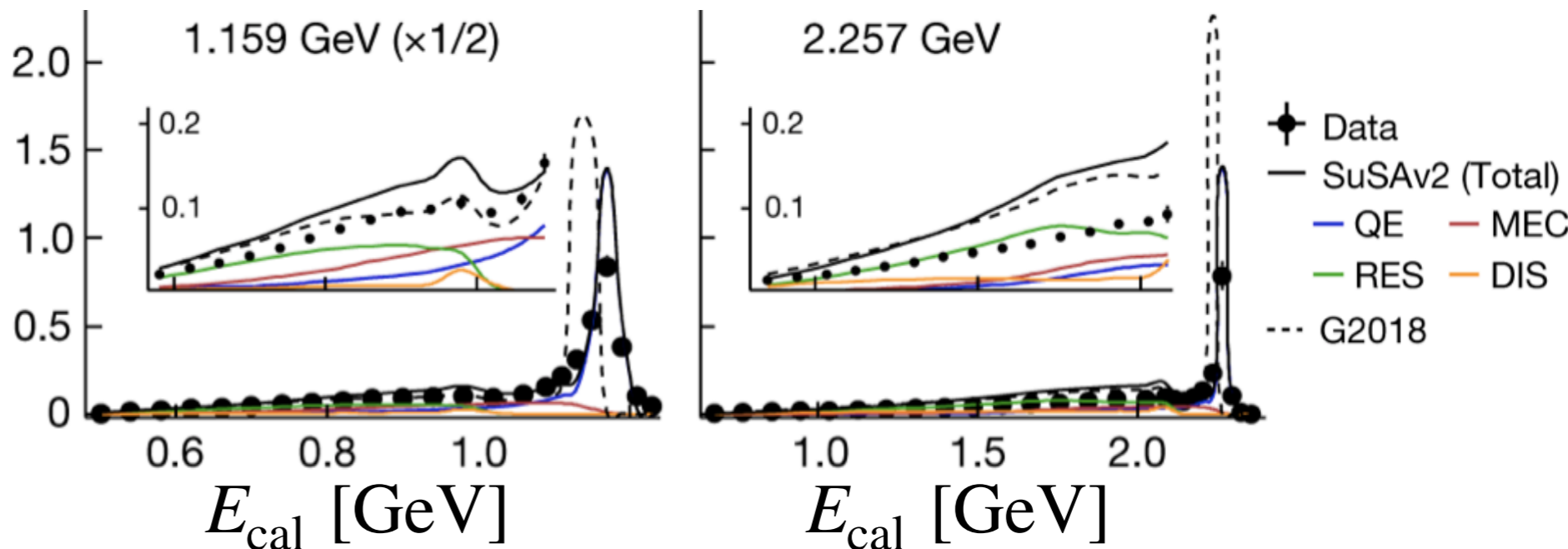
CLAS and $e4\nu$ collaborations
 Nature 599 (2021) 7886, 565-570

PRD 107 (2023) 3, 033007 [arXiv:2205.06378]

E_{cal} = “Calorimetric energy” = “sum of final-state energies”

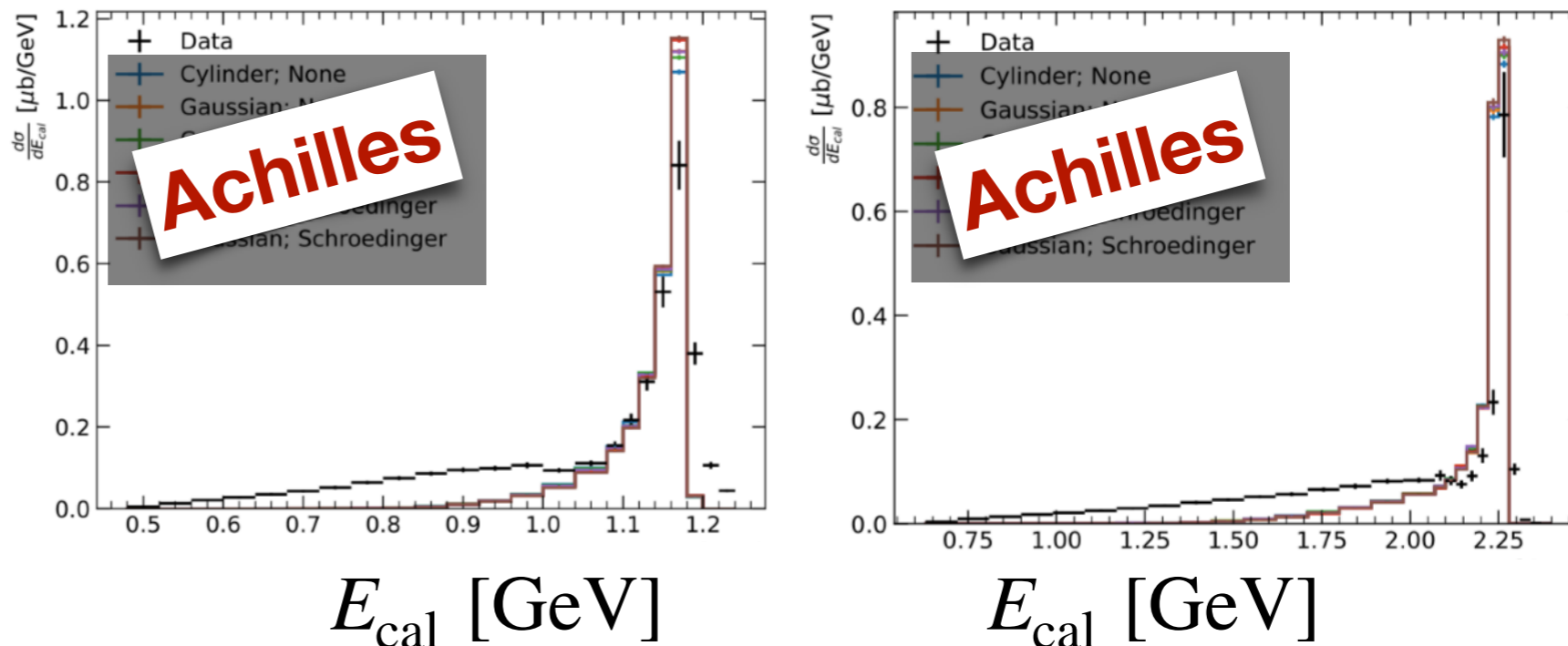
Data + simulation
 from $e4\nu$ paper

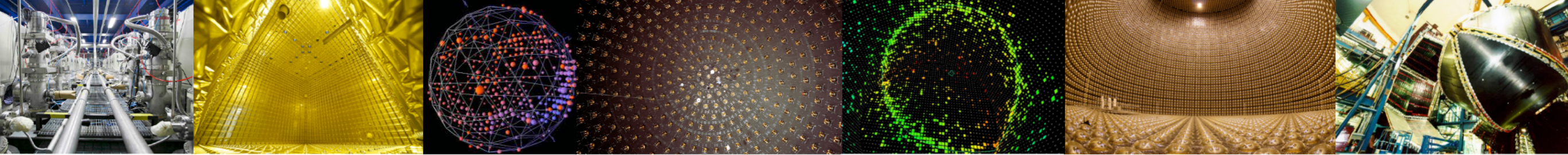
$$\frac{d\sigma}{dE_{\text{cal}}}$$



Same $e4\nu$ data
 vs Achilles

$$\frac{d\sigma}{dE_{\text{cal}}}$$



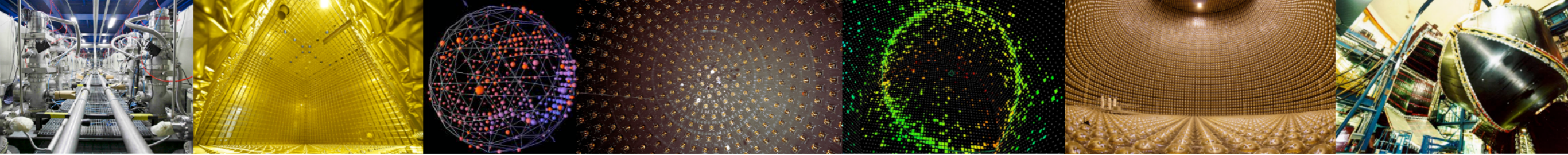


Achilles Intranuclear Cascade (INC)

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

The quantum mechanical scattering model:

- Utilizes measured NN cross sections, e.g., from SAID database with GEANT4 or NASA parameterization
- Scatters probabilistically according to the impact parameter: $P(b) = \exp(-\pi b^2 / \sigma)$
 - ☑ $\lambda^{-1} = \rho\sigma$ for the mean free path λ
 - ☑ Total probability integrates to the cross section σ
- Incorporates Pauli blocking and formation zone to constrain possible scatterings



Achilles Intranuclear Cascade (INC)

$$|\mathcal{M}(\{k\} \rightarrow \{p\})|^2 \simeq \sum_{p'} |\mathcal{V}(\{k\} \rightarrow \{p'\})|^2 \times |\mathcal{P}(\{p'\} \rightarrow \{p\})|^2$$

Classical propagation in the background nucleus creates an effective optical potential which induces two effects:

1. Short-distance: $\frac{d\sigma}{d\Omega} \longrightarrow \left(\frac{d\sigma}{d\Omega} \right)_{\text{in medium}}$

(In-medium corrections to NN interactions)

2. Long-distance: $\dot{\mathbf{p}} = -\partial_{\mathbf{q}} H \quad \dot{\mathbf{q}} = +\partial_{\mathbf{p}} H$

(Classical evolution in background potential)