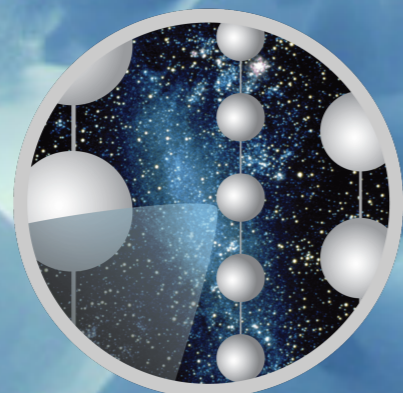


# Recent Results on the 3+1 Model from IceCube

Nicholas Kamp for the IceCube collaboration  
Santa Fe, NM; 2 April 2024

2nd Short-Baseline Experiment-Theory Workshop

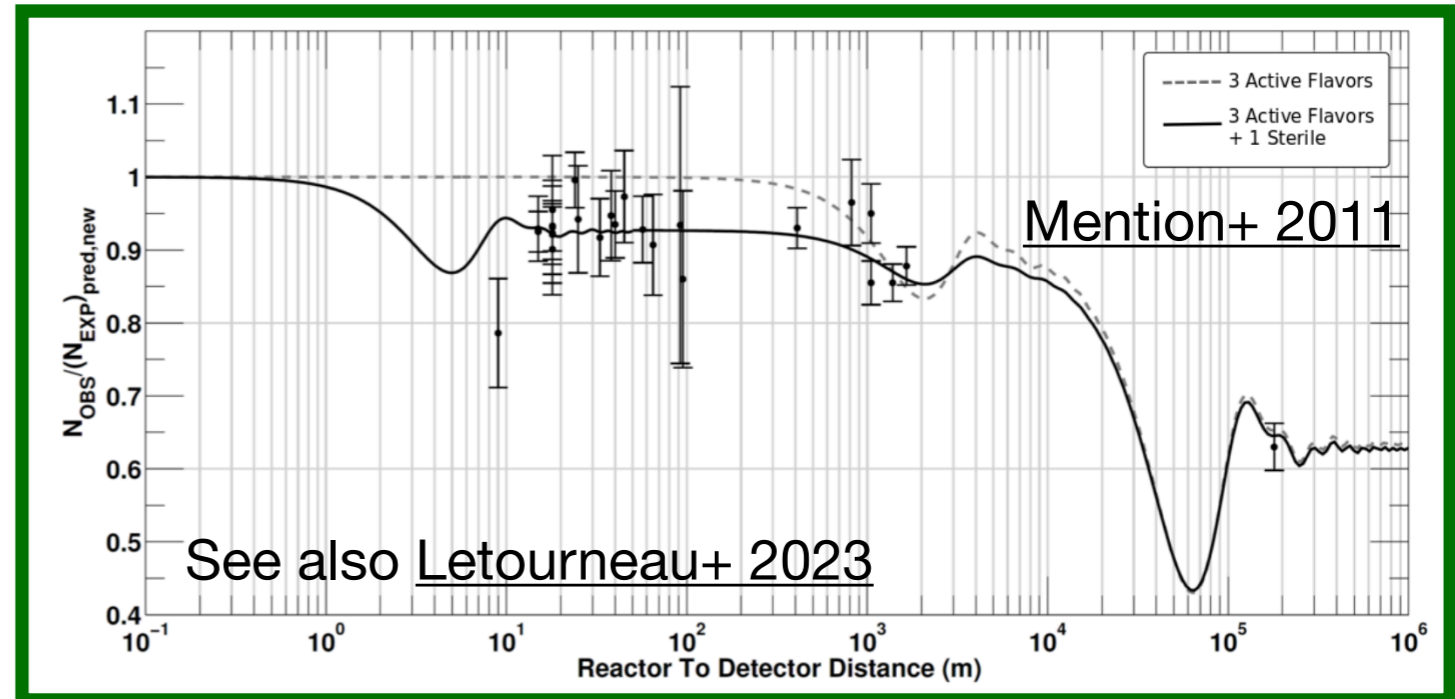
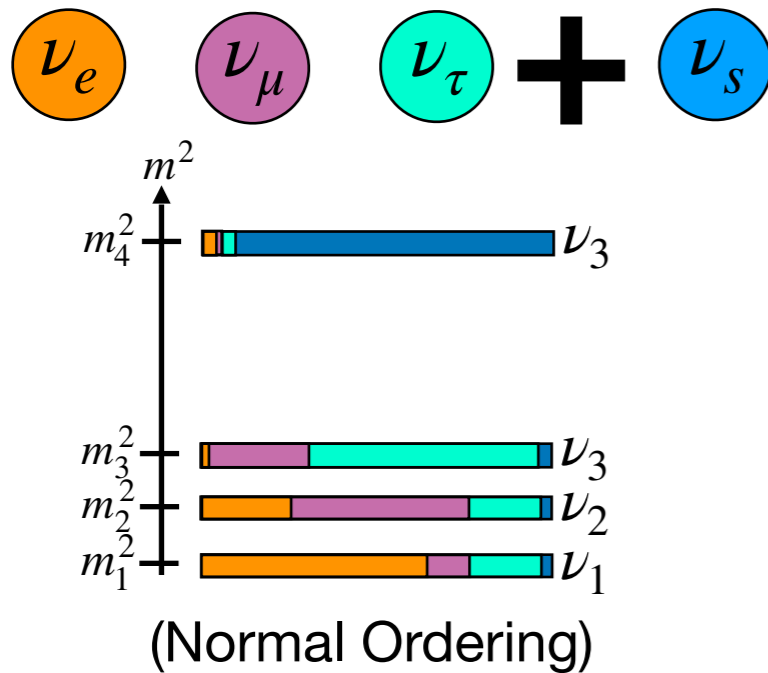


ICECUBE

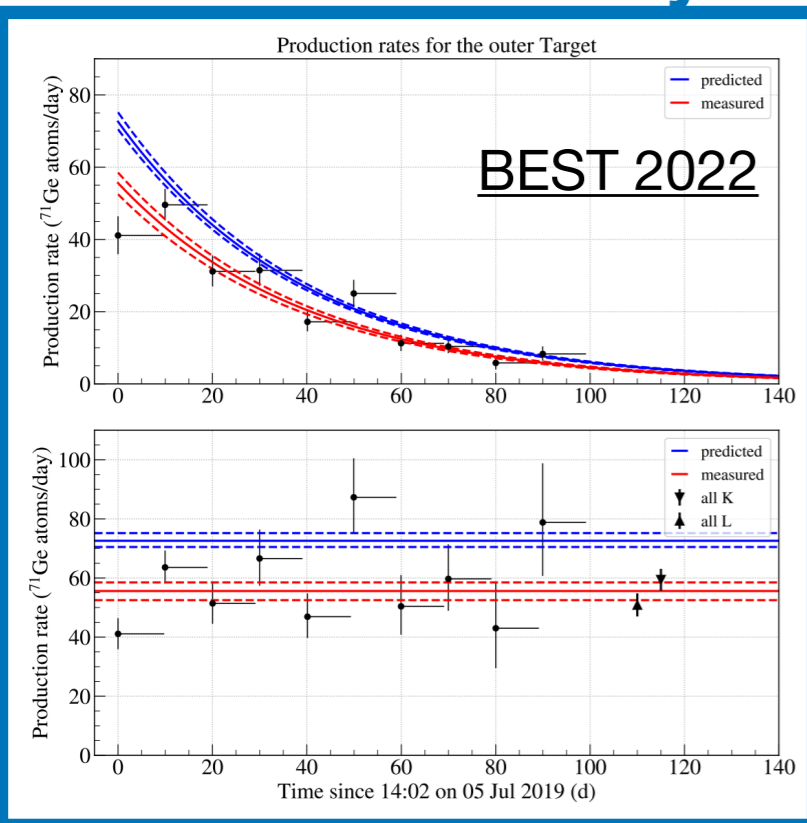


# Many Anomalies Hinting at 3+1

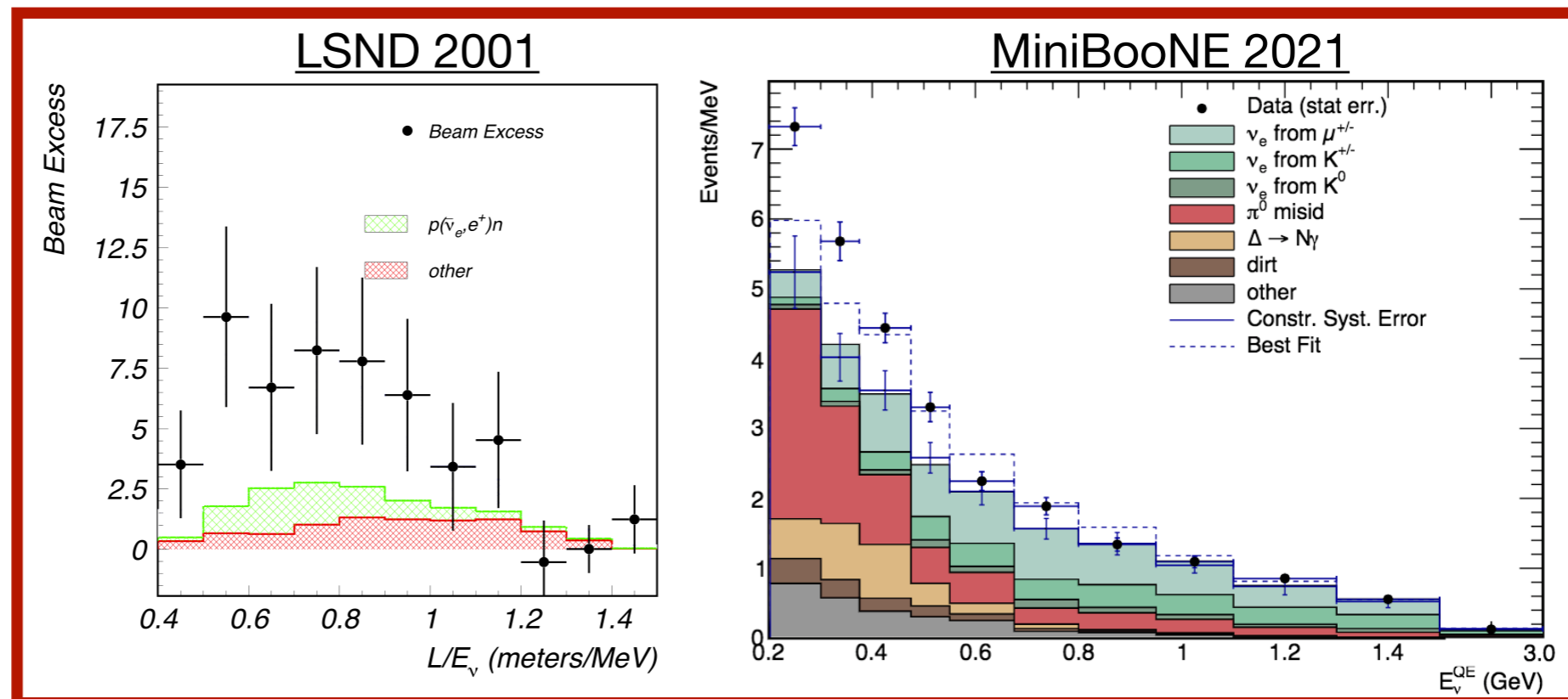
## Reactor Antineutrino Anomaly



## Gallium Anomaly



## Short Baseline Accelerator Anomalies



# “Typical” 3+1 Experiment



Human-made  
neutrino source (e.g.  
accelerator, reactor,  
radioactive)



# “Typical” 3+1 Experiment



**Human-made  
neutrino source (e.g.  
accelerator, reactor,  
radioactive)**



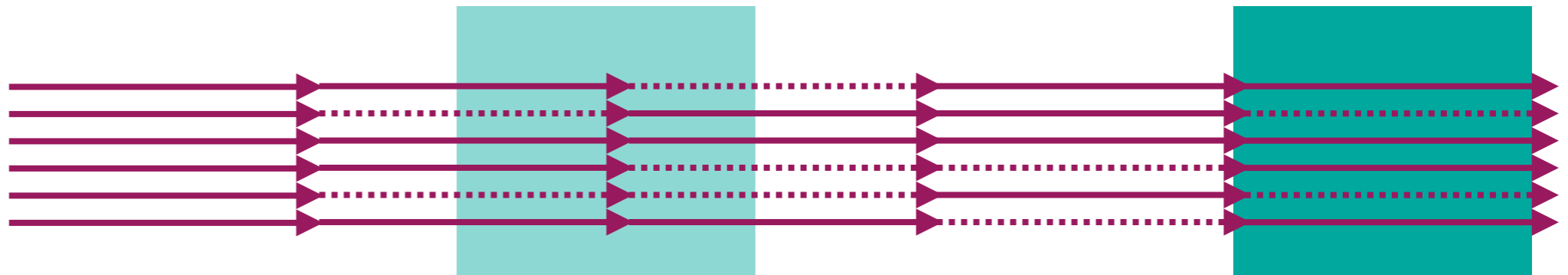
**Observe neutrino  
interactions in one  
or two ton-scale  
detectors with  
fixed baseline**



# “Typical” 3+1 Experiment



Human-made neutrino source (e.g. accelerator, reactor, radioactive)



Search for anomalous (dis)appearance via vacuum oscillations induced by the new mass eigenstate

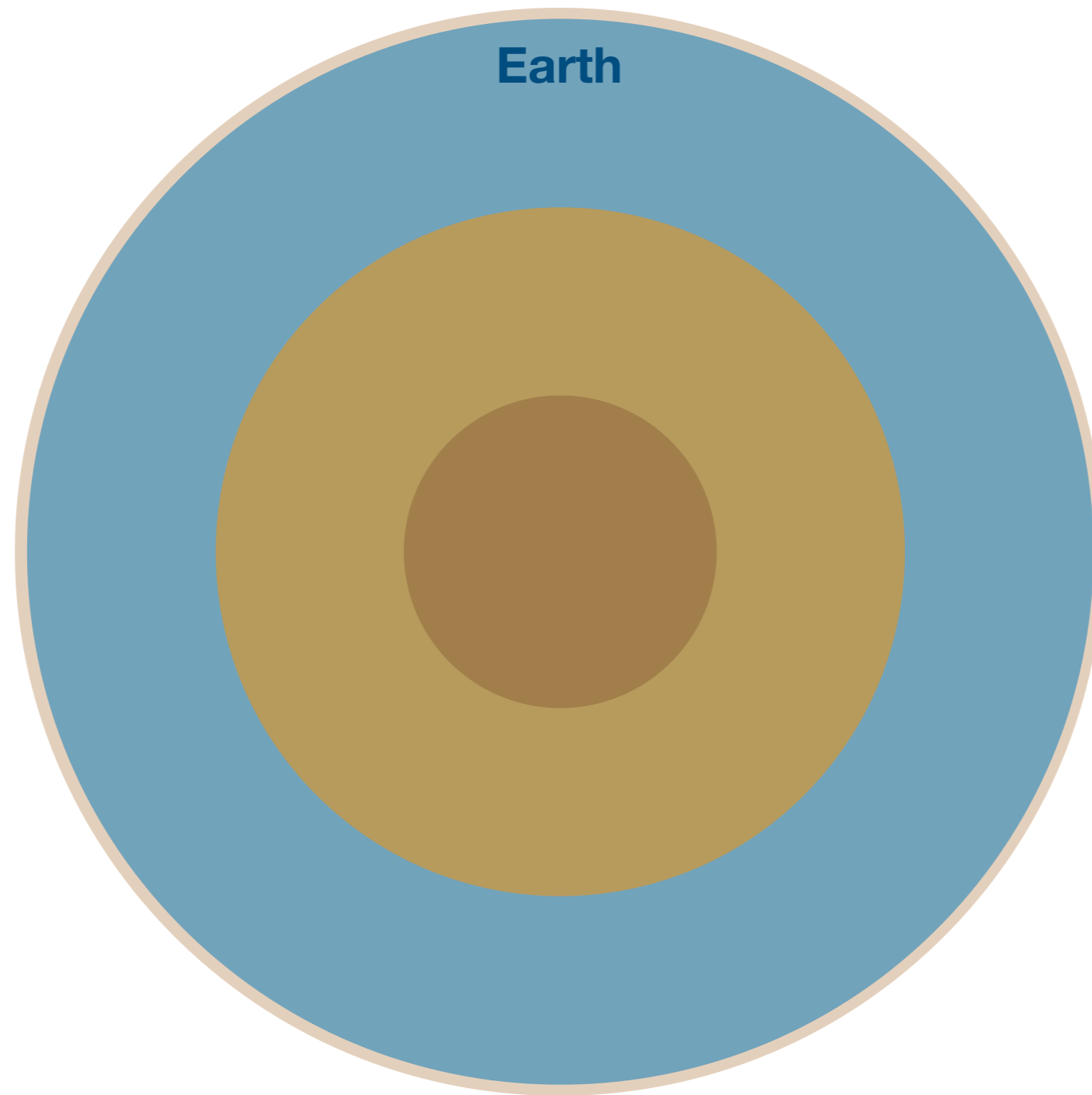
Observe neutrino interactions in one or two ton-scale detectors with fixed baseline

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2(2\theta_{\mu e}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

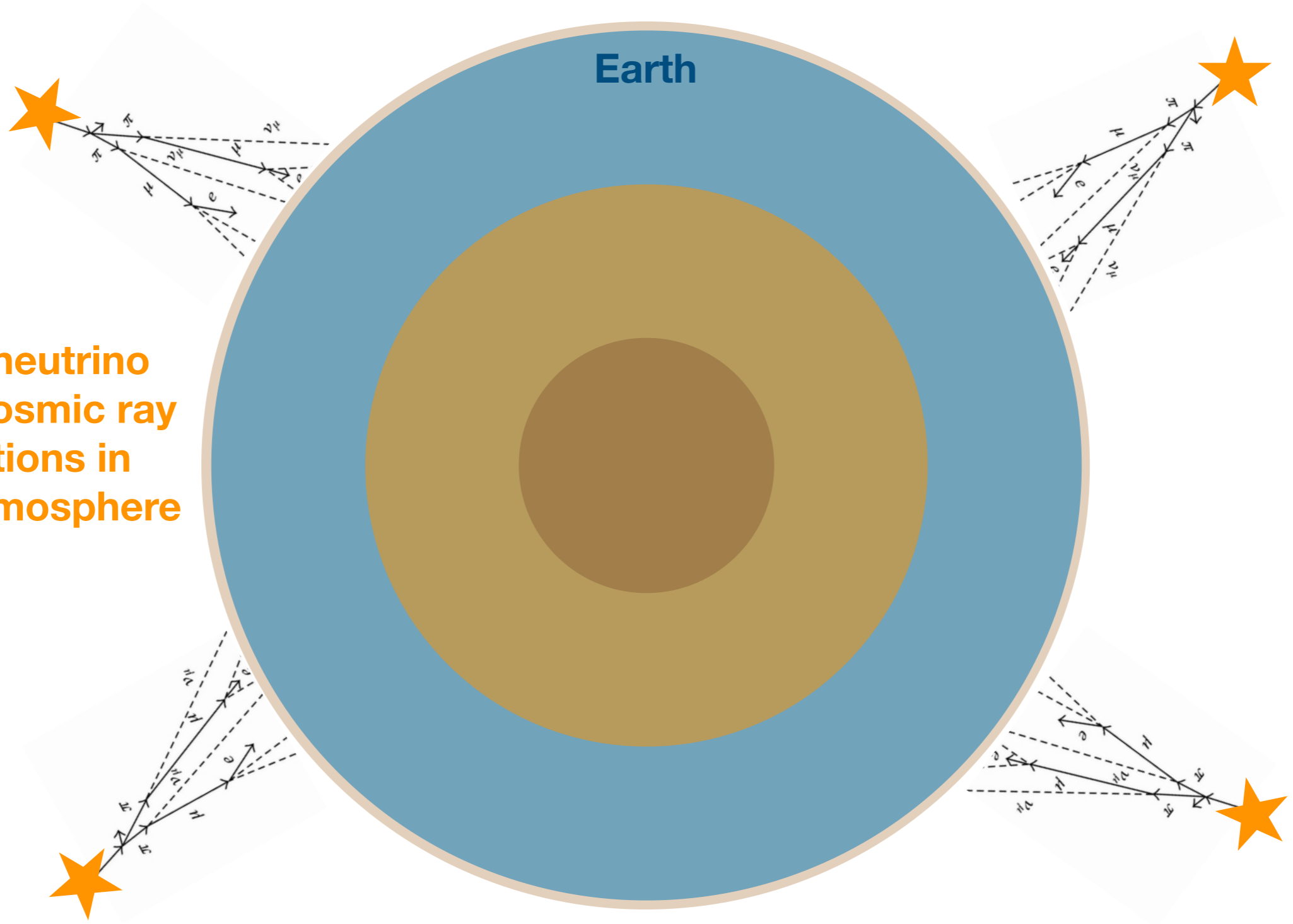
$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2(2\theta_{ee}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta_{\mu\mu}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

# 3+1 in IceCube



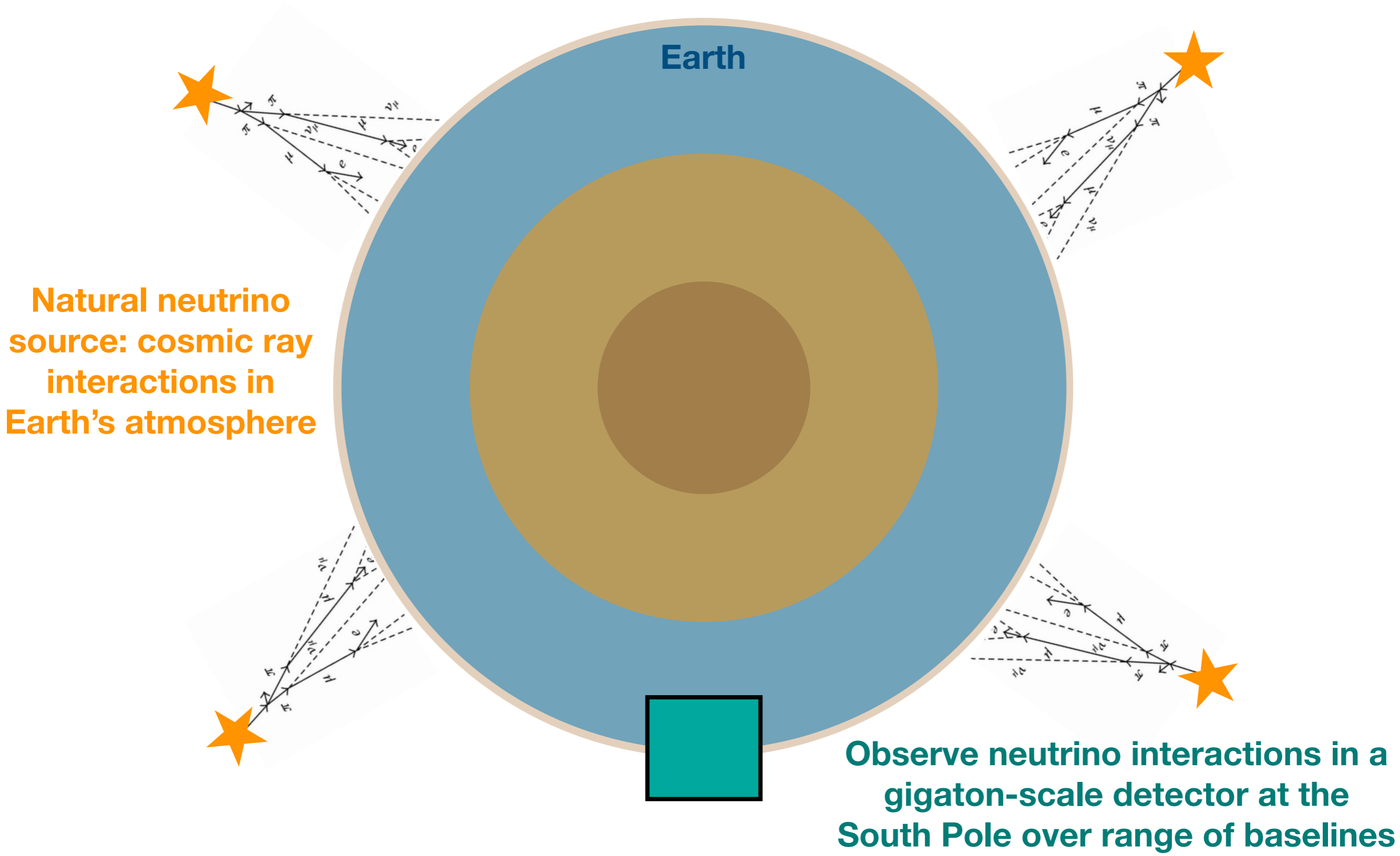
# 3+1 in IceCube



Natural neutrino source: cosmic ray interactions in Earth's atmosphere



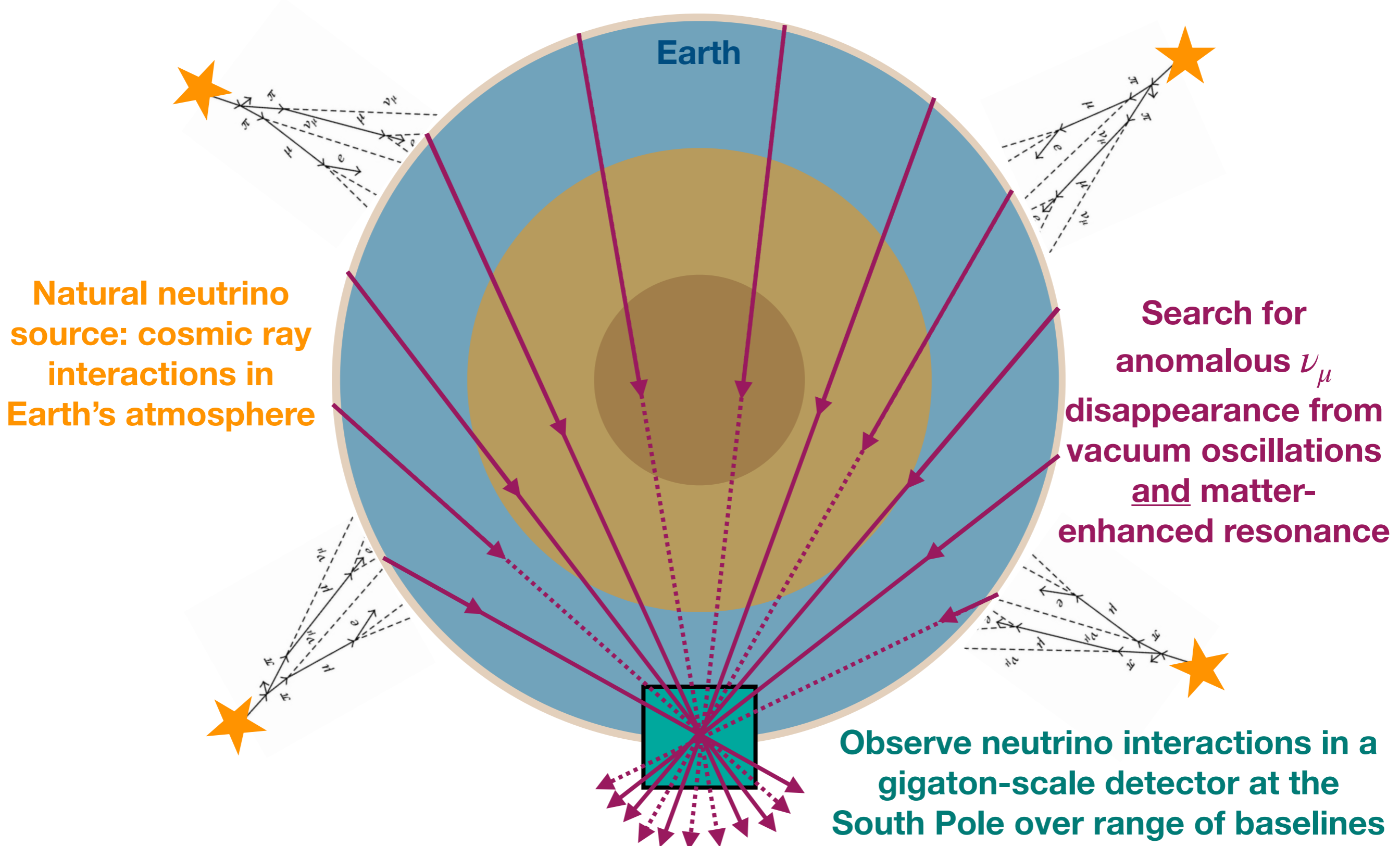
# 3+1 in IceCube

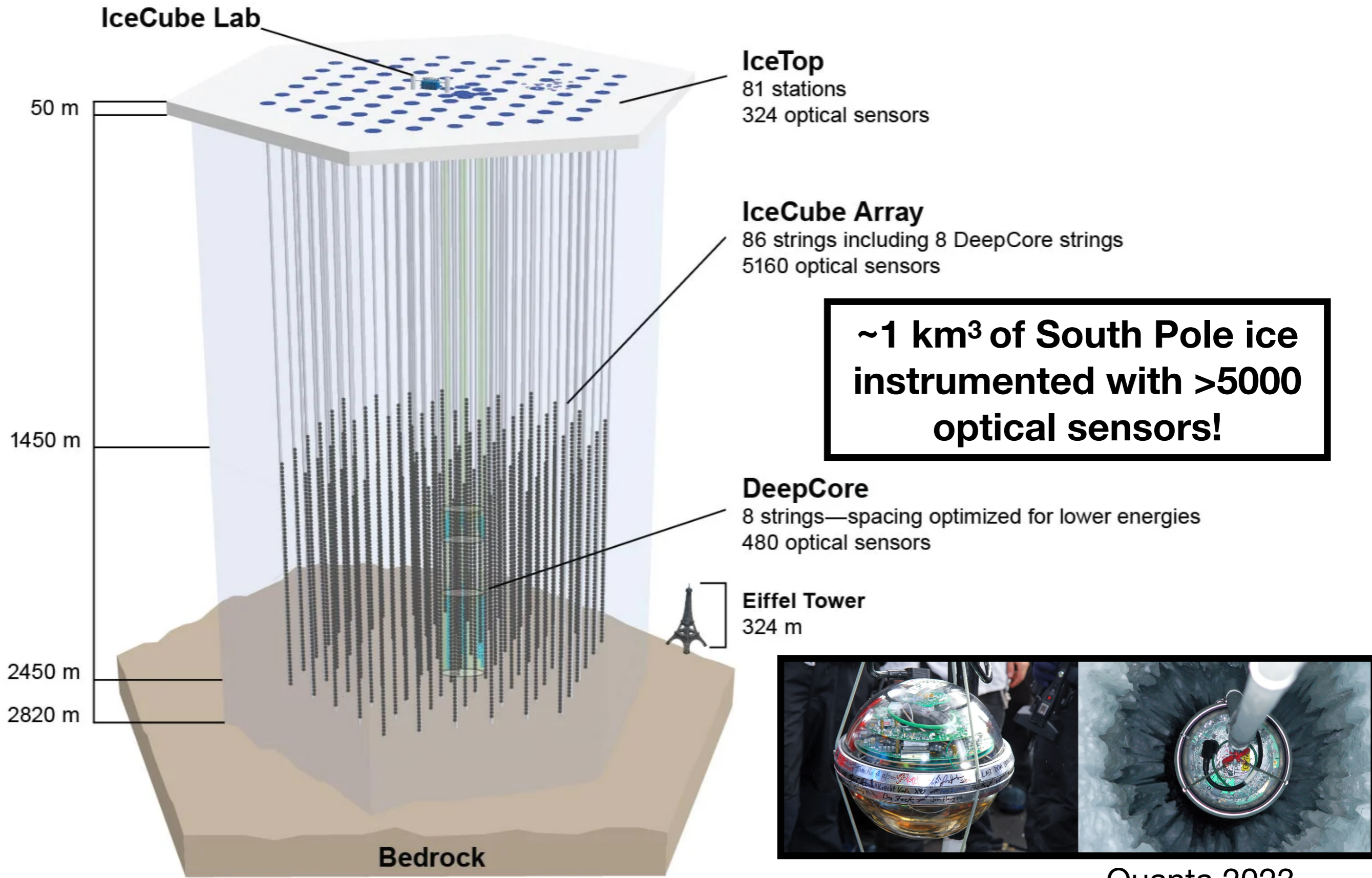


Natural neutrino source: cosmic ray interactions in Earth's atmosphere

Observe neutrino interactions in a gigaton-scale detector at the South Pole over range of baselines

# 3+1 in IceCube

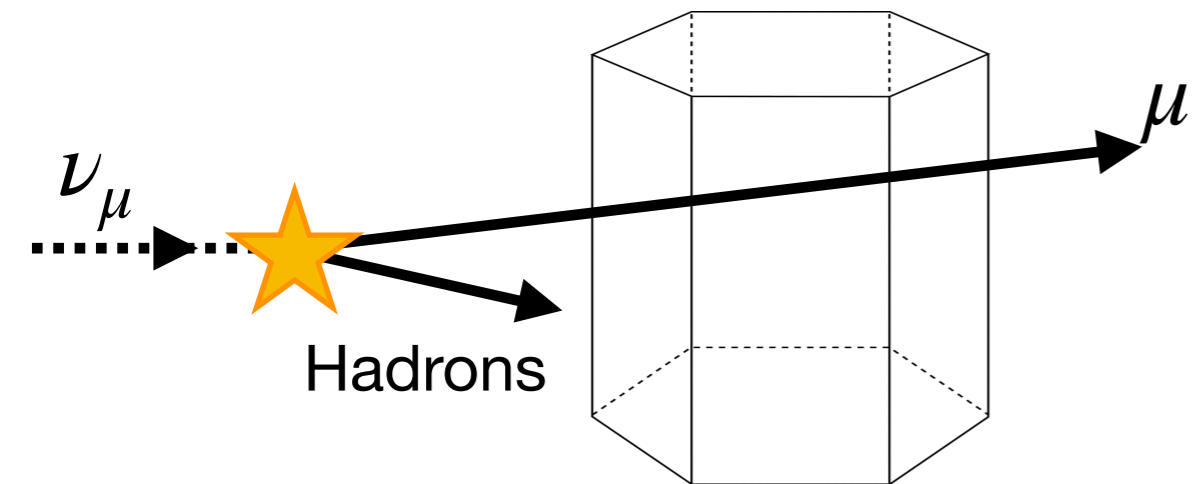




Quanta 2023

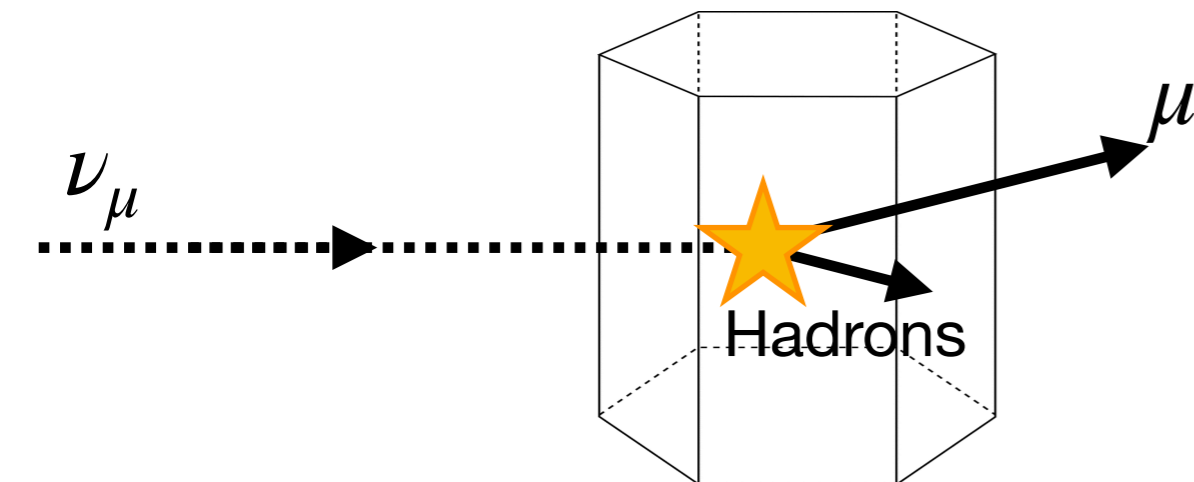


# IceCube Event Types



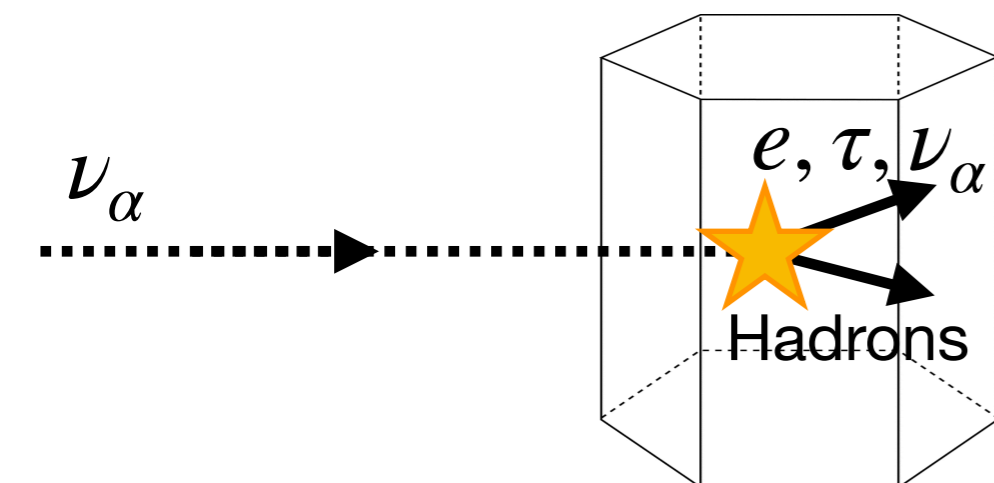
## “Through-going track”

$\nu_\mu$  charged-current DIS outside the active volume



## “Starting track”

$\nu_\mu$  charged-current DIS inside the active volume



## “Cascade”

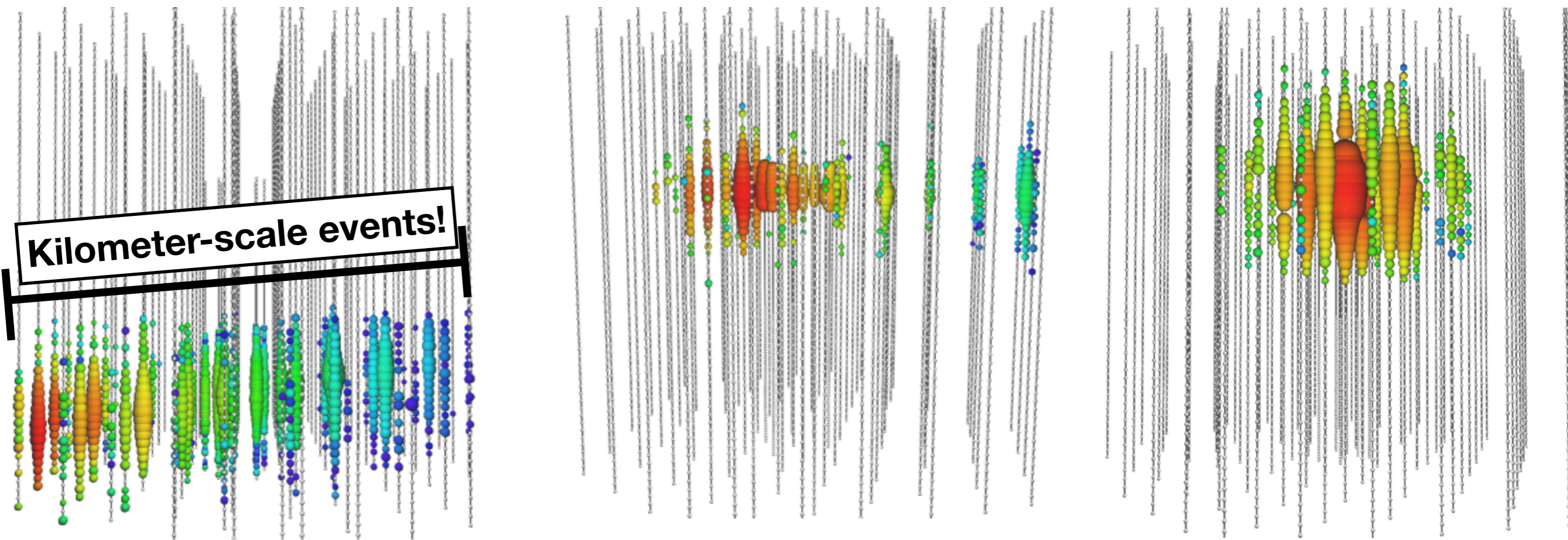
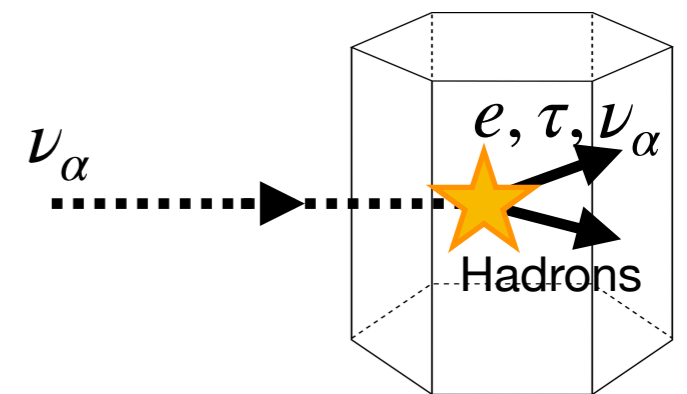
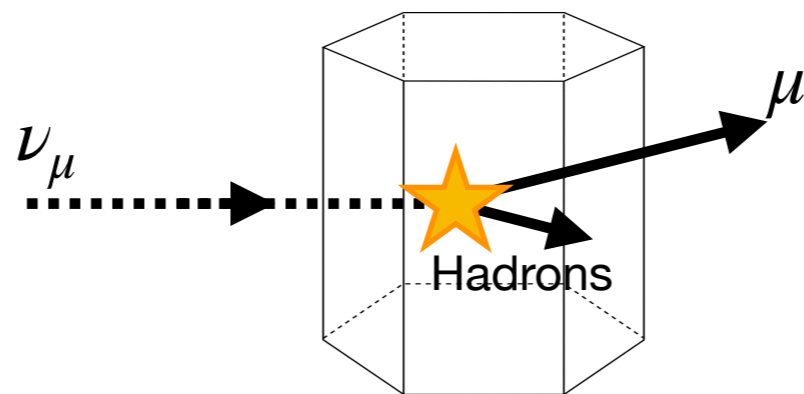
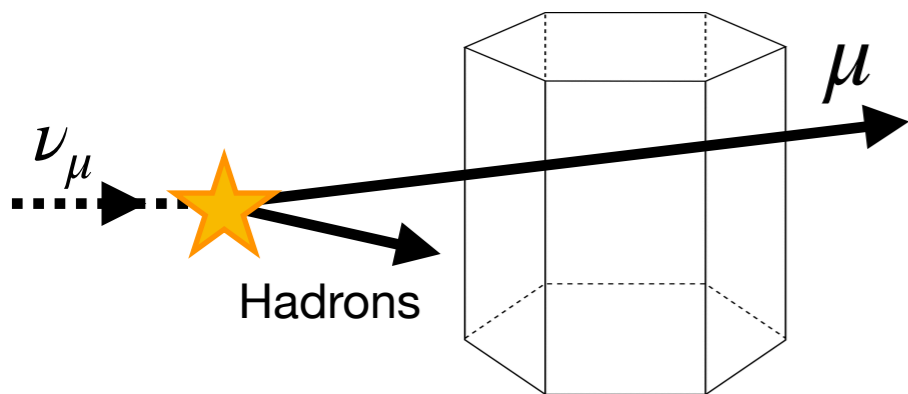
$\nu_{e,\tau}$  charged-current DIS or  $\nu_\alpha$  neutral-current DIS inside the active volume

# IceCube Event Types

## Through-going track

## Starting track

## Cascade



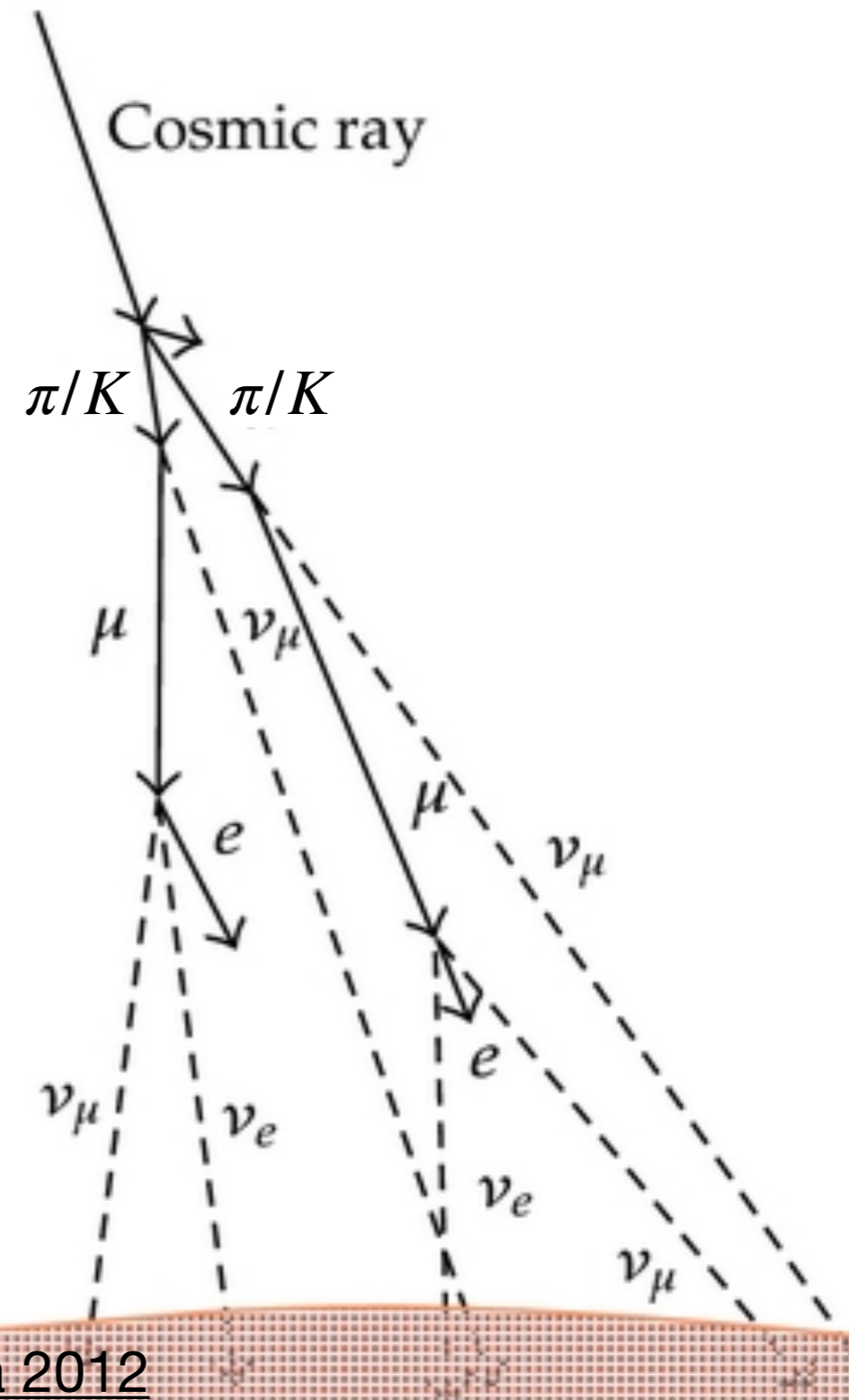
Earliest photons



Latest photons

# Atmospheric Neutrino Flux

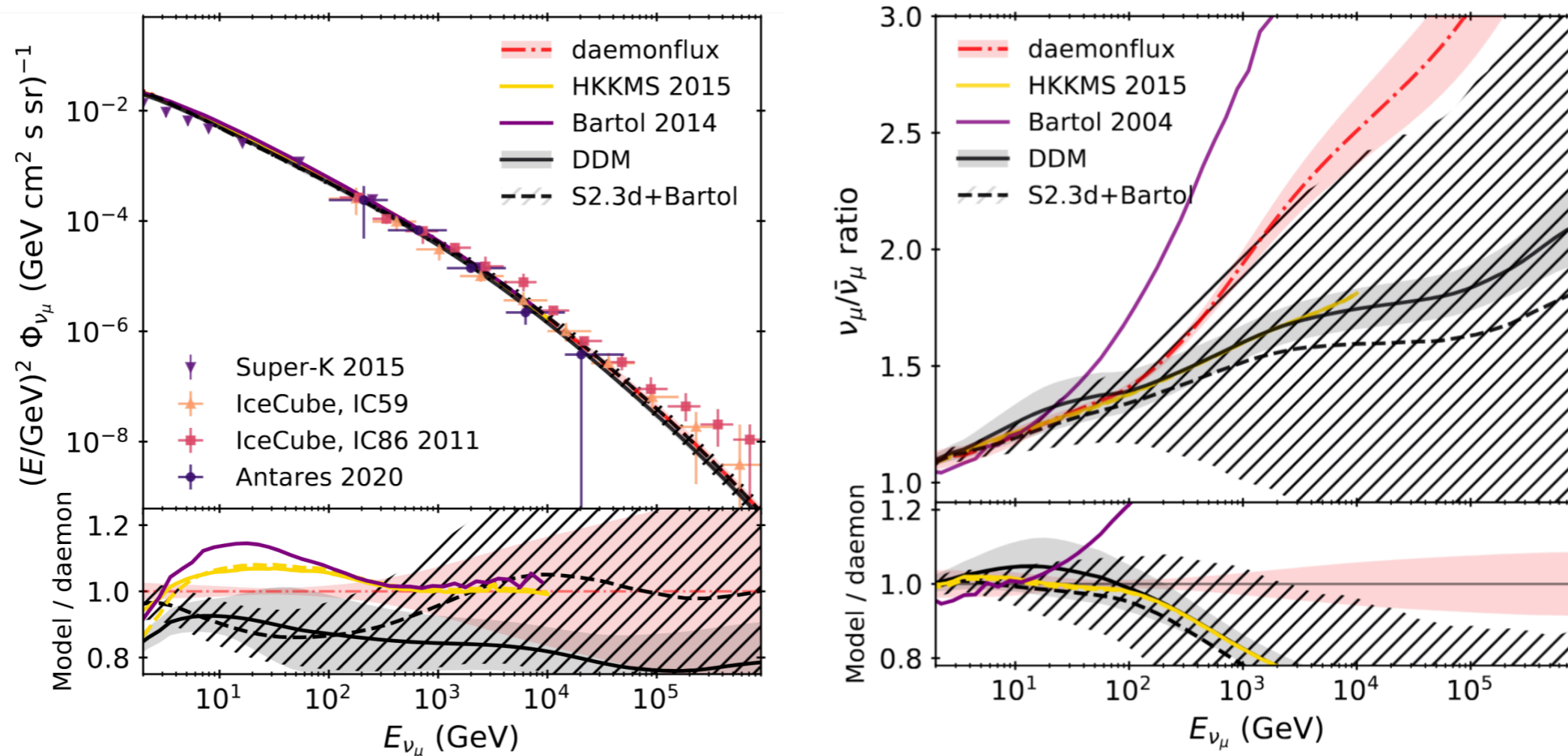
- We use the atmospheric neutrino flux as our  $\nu_\mu/\bar{\nu}_\mu$  source
- Like accelerator neutrino sources, neutrinos generated by the decay of hadrons produced proton-nuclear collisions
- Unlike accelerator neutrino sources, flux predictions don't require modeling of complicated target hall geometry or magnetic fields of focusing horns



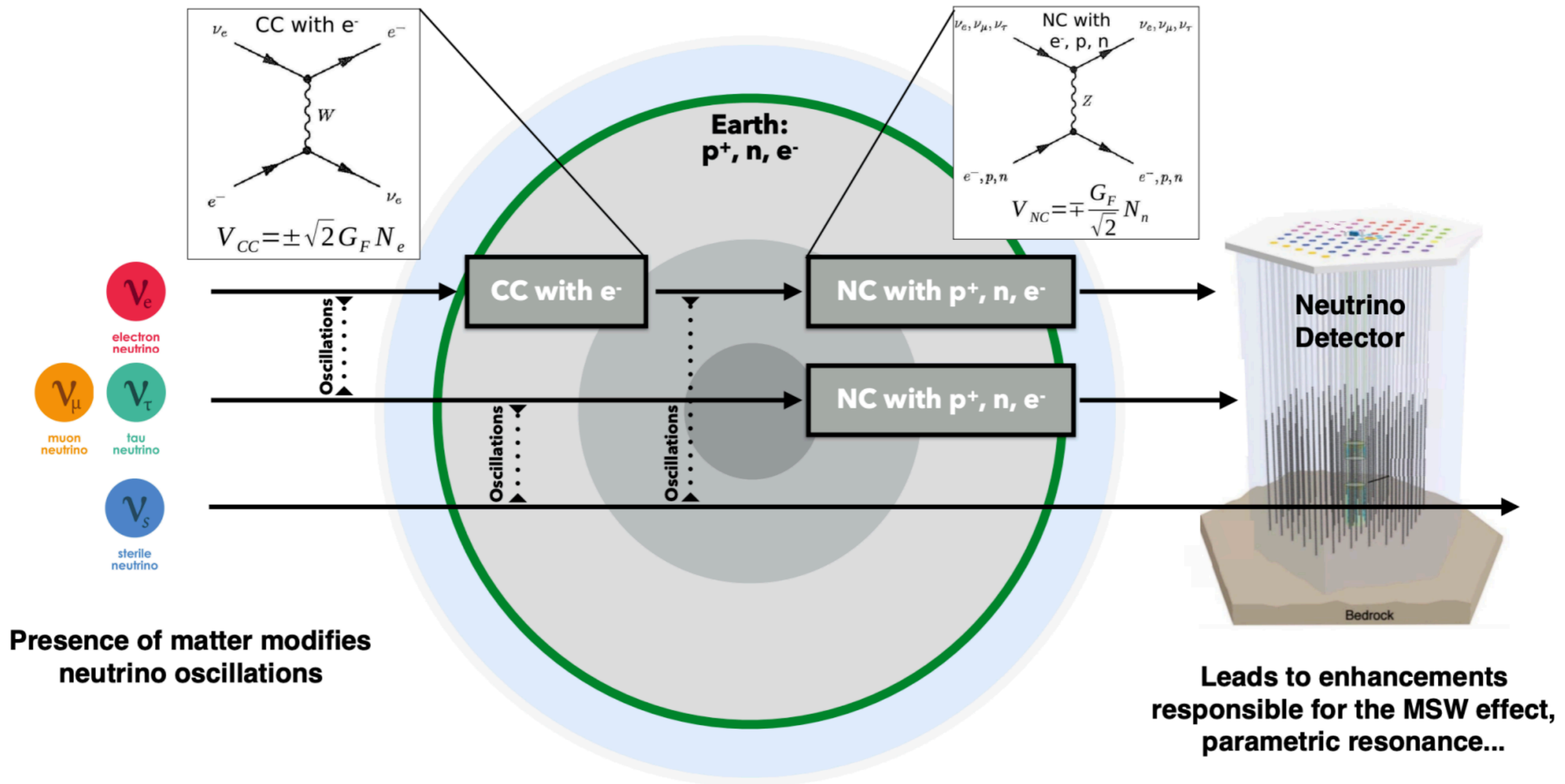


# Atmospheric Neutrino Flux

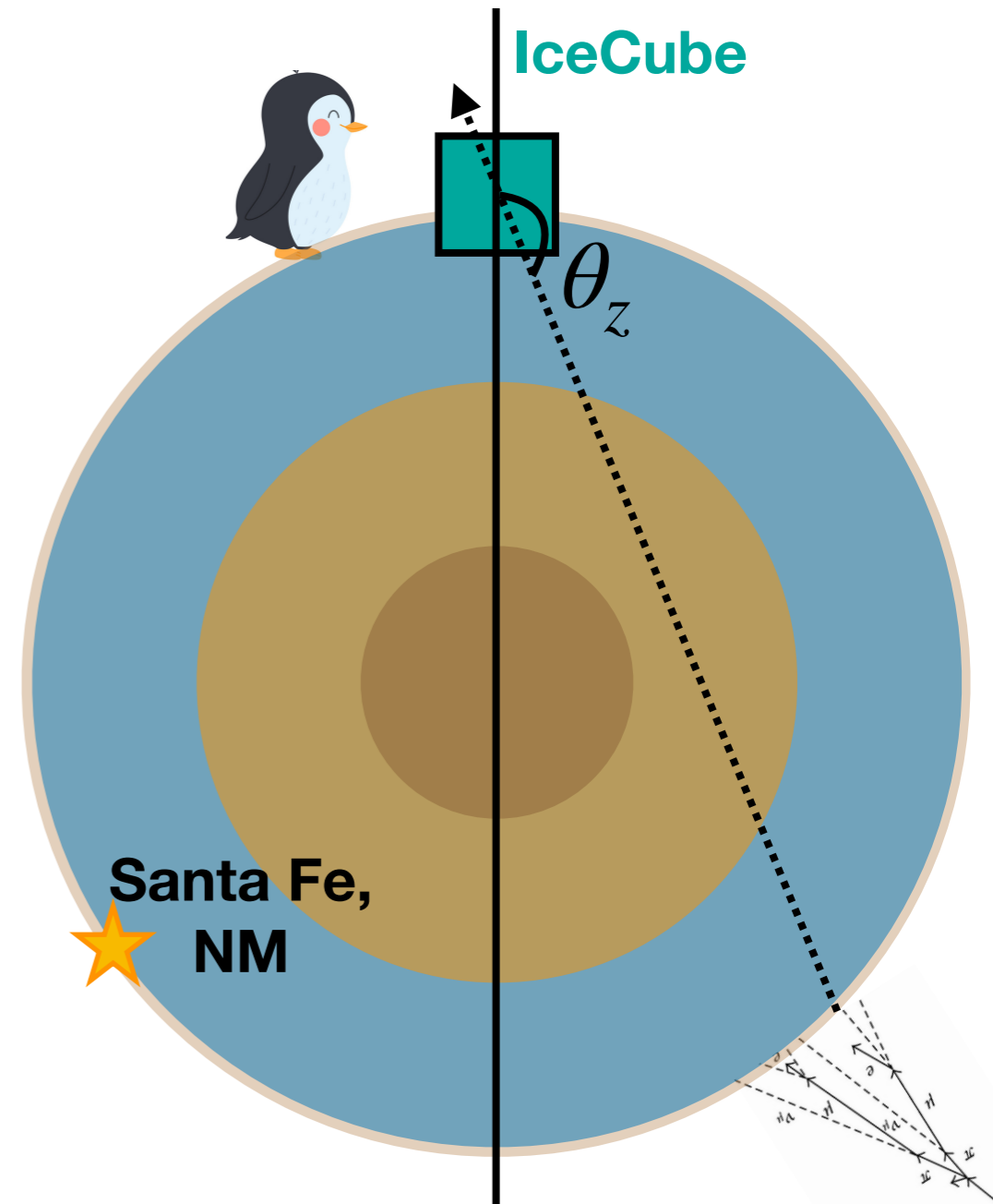
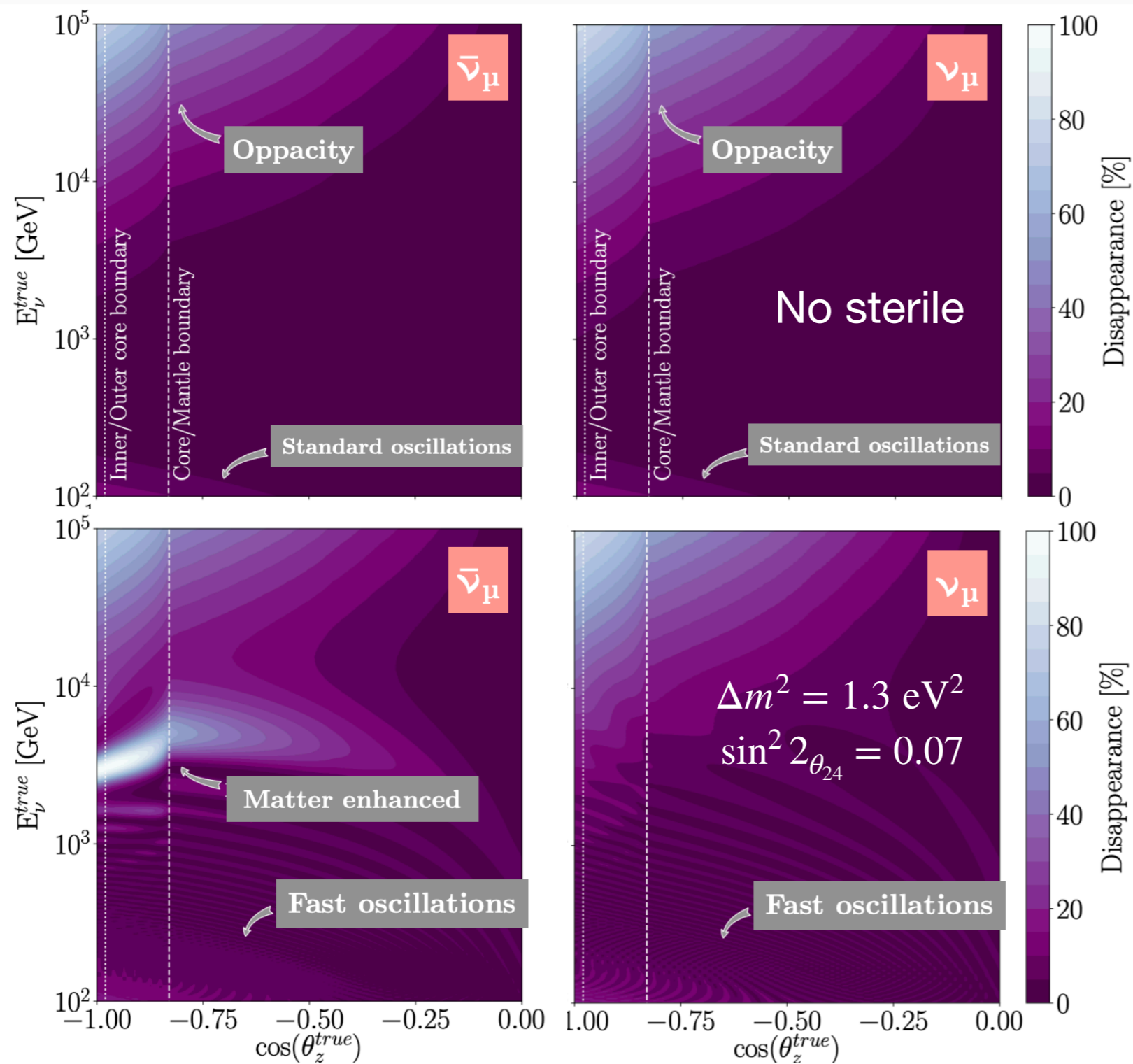
- We use the updated DAEMONFLUX model ([Yañez+ 2023](#))
- Based on measurements of cosmic muon fluxes and charge ratios as well as fixed target hadron cross sections
- Uncertainties account for cosmic ray nucleon flux, meson production cross sections, and detector-specific systematics



# Sterile neutrinos in IceCube



# Sterile neutrinos in IceCube

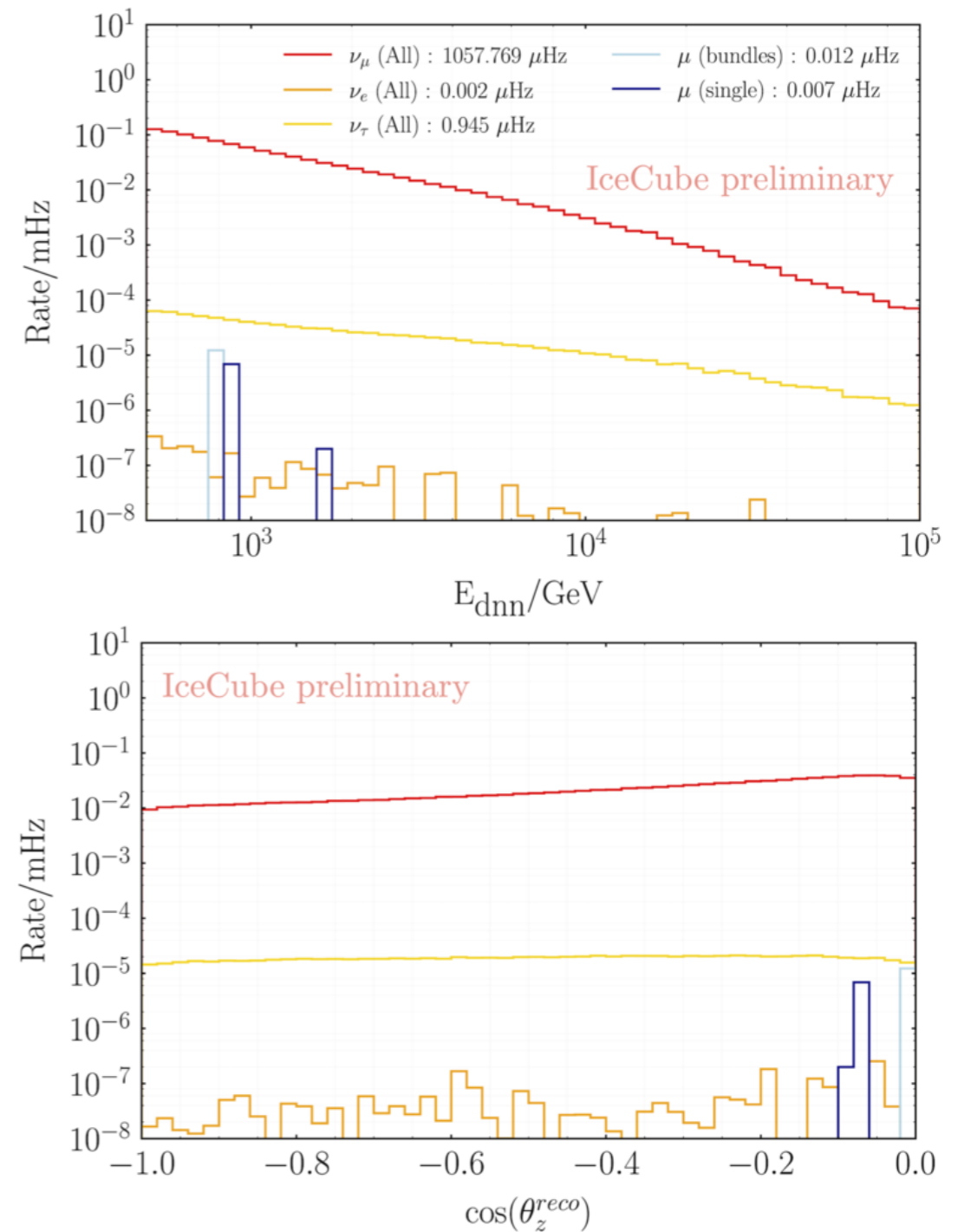
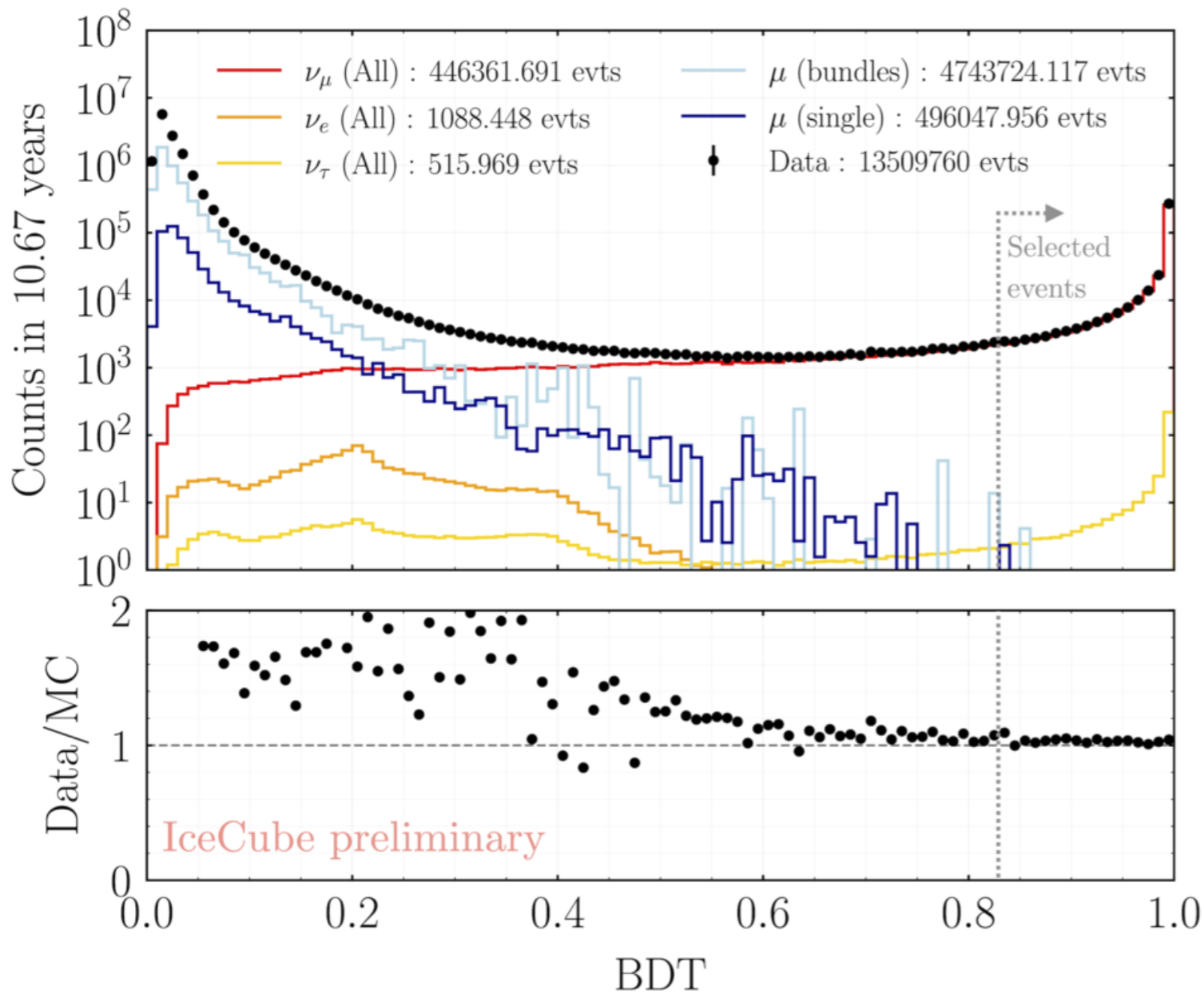


**Simultaneous measurement of oscillated and un-oscillated component of neutrino flux**



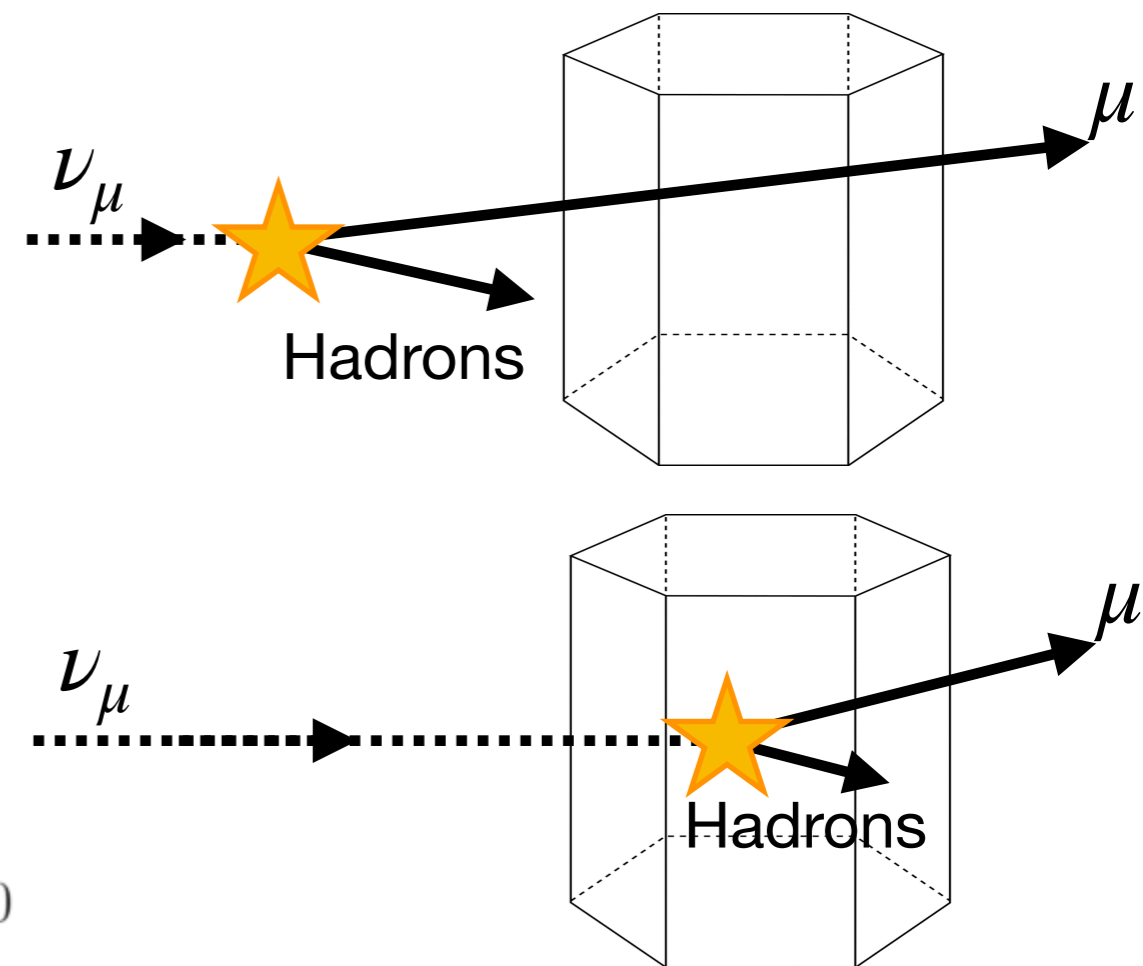
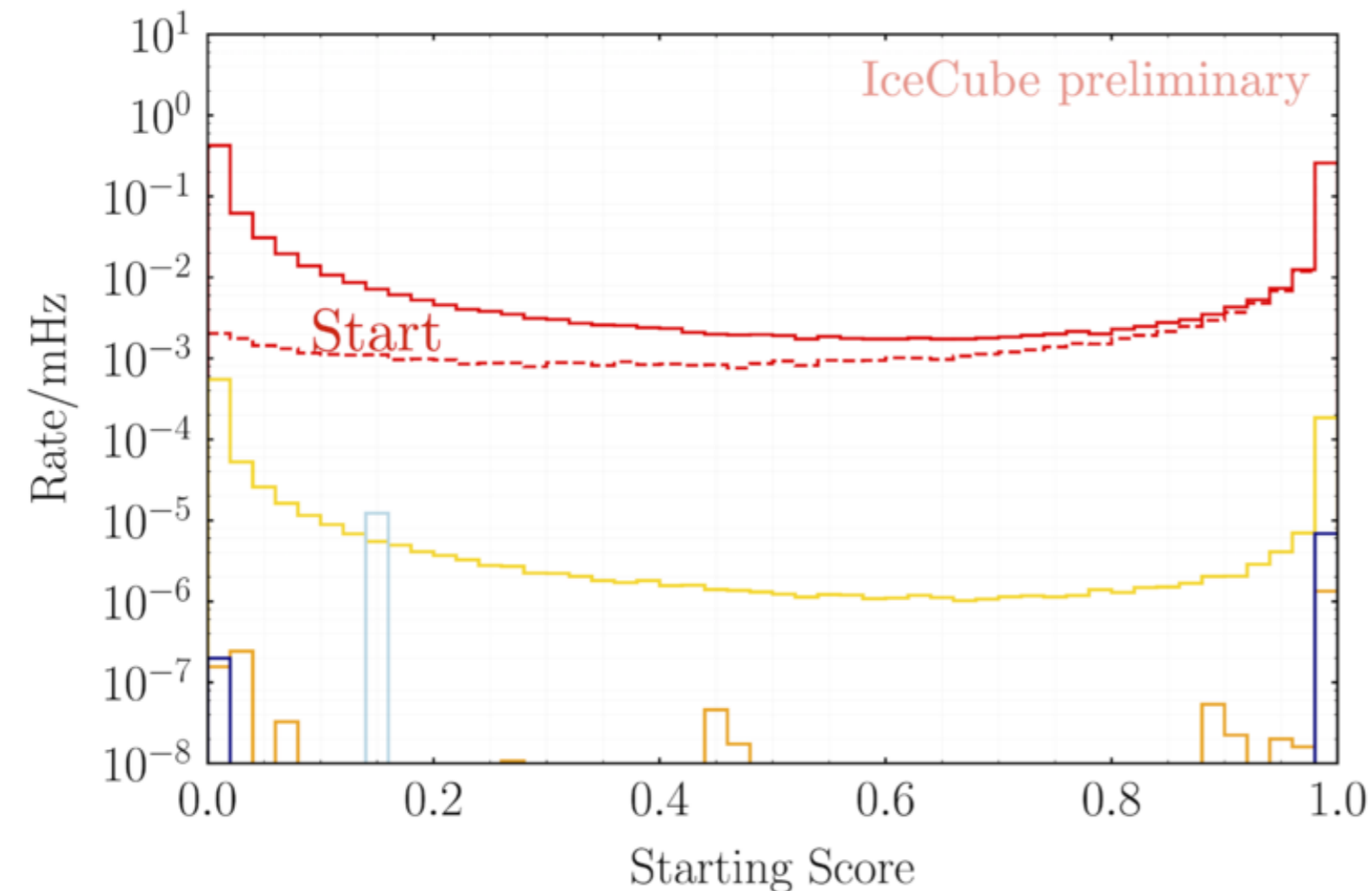
# Analysis Strategy

- BDT to isolate a pure sample of up-going tracks



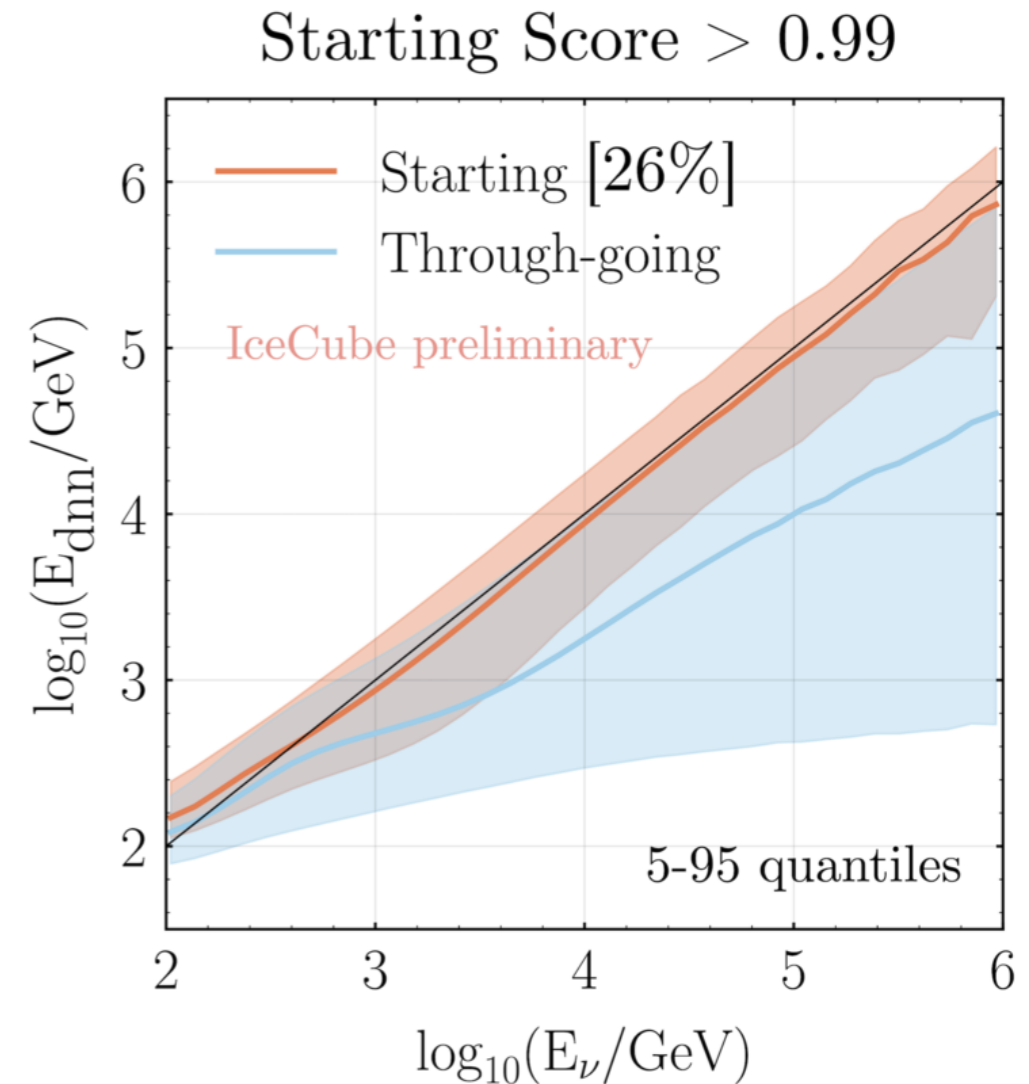
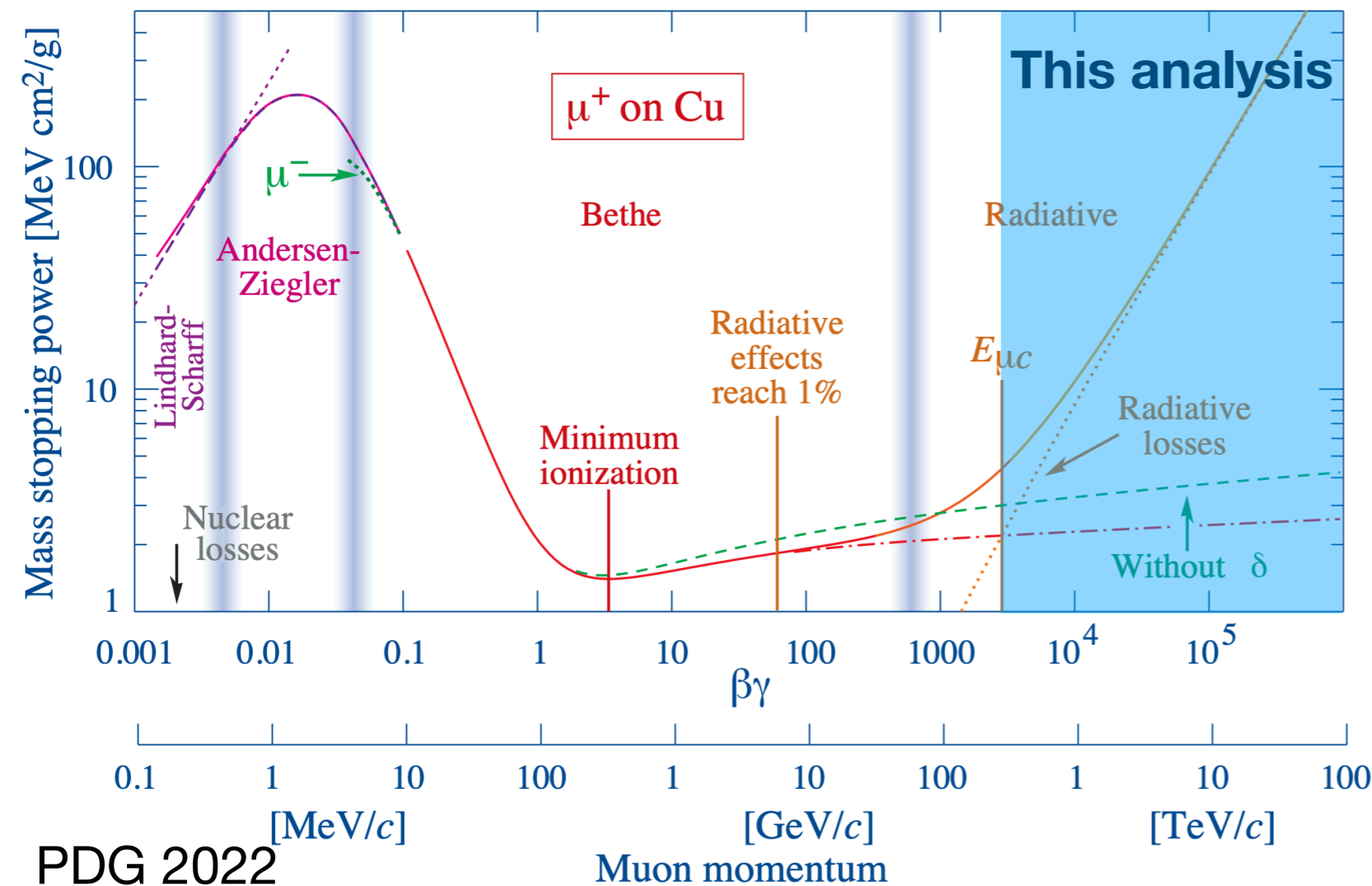
# Analysis Strategy

- BDT to isolate a pure sample of up-going tracks
- DNN to separate starting and through-going tracks



# Analysis Strategy

- BDT to isolate a pure sample of up-going tracks
- DNN to separate starting and through-going tracks
- Another DNN to reconstruct the original neutrino energy



# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. Bulk ice properties
4. Local DOM response
5. Neutrino attenuation
6. Overall normalization



# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. Bulk ice properties
4. Local DOM response
5. Neutrino attenuation
6. Overall normalization

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range	
Conventional flux (Sec. III A)				
Atm. density ( $\rho_{\text{atm}}$ )	0.00	1.00	-3.00,3.00	
Kaon energy loss ( $\sigma_{\text{K-Air}}$ )	0.00	1.00	-3.00,3.00	
Hadronic production	$K_{158G}^+$	0.00	1.00	-2.00,2.00
	$K_{158G}^-$	0.00	1.00	-2.00,2.00
	$\pi_{20T}^+$	0.00	1.00	-2.00,2.00
	$\pi_{20T}^-$	0.00	1.00	-2.00,2.00
	$K_{2P}^+$	0.00	1.00	-1.00,2.00
	$K_{2P}^-$	0.00	1.00	-1.50,2.00
	$\pi_{2P}^+$	0.00	1.00	-2.00,2.00
	$\pi_{2P}^-$	0.00	1.00	-2.00,2.00
	$p_{2P}$	0.00	1.00	-2.00,2.00
	$n_{2P}$	0.00	1.00	-2.00,2.00
CR spectrum	GSF <sub>1</sub>	0.00	1.00	-4.00,4.00
	GSF <sub>2</sub>	0.00	1.00	-4.00,4.00
	GSF <sub>3</sub>	0.00	1.00	-4.00,4.00
	GSF <sub>4</sub>	0.00	1.00	-4.00,4.00
	GSF <sub>5</sub>	0.00	1.00	-4.00,4.00
	GSF <sub>6</sub>	0.00	1.00	-4.00,4.00

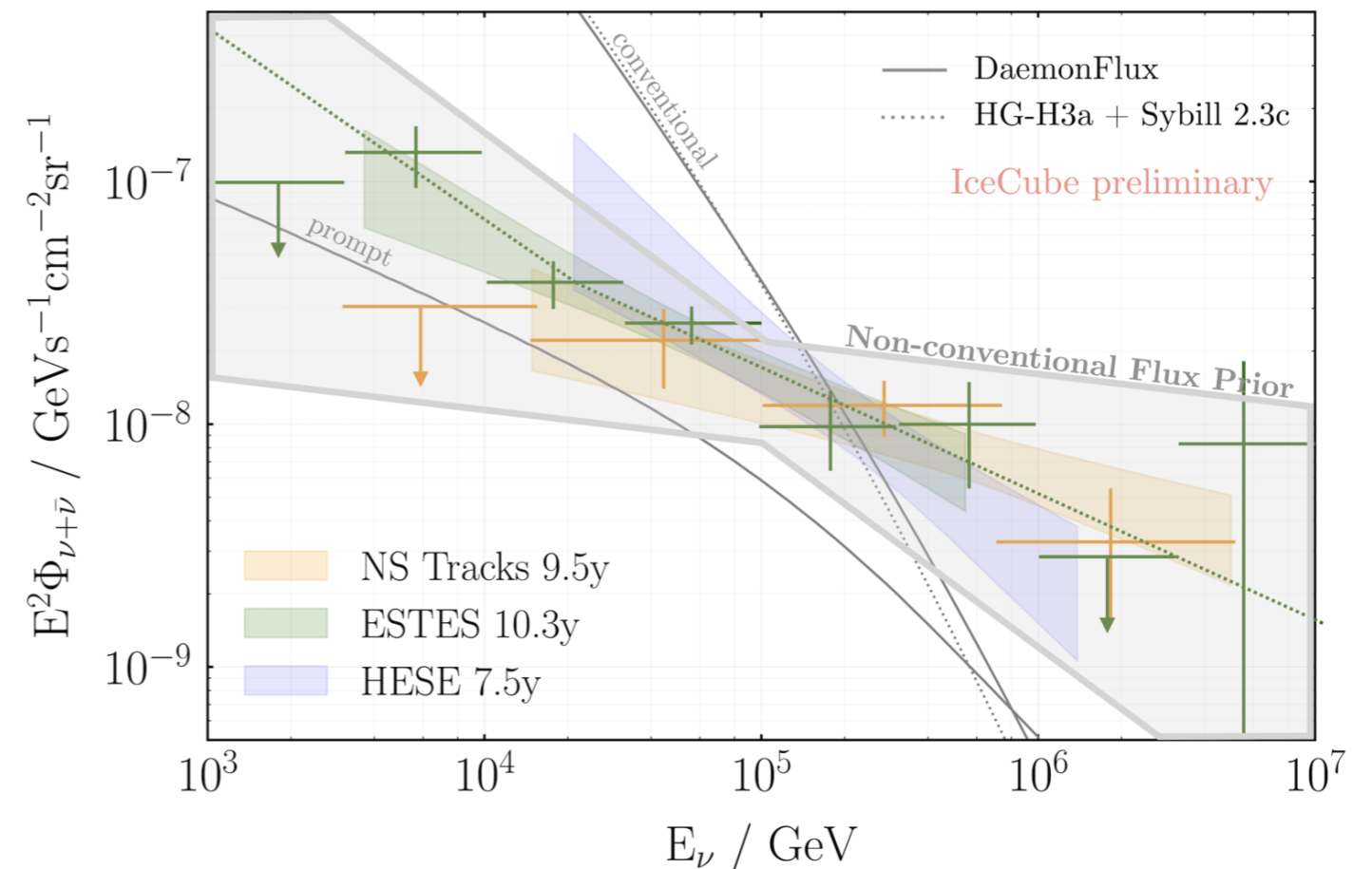
**DAEMONFLUX uncertainties + atmospheric density and meson energy losses in atmosphere**

# Systematic Uncertainties

## 6 major categories

1. Conventional flux
- 2. Non-conventional flux**
3. Bulk ice properties
4. Local DOM response
5. Neutrino attenuation
6. Overall normalization

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range
Non-conventional flux (Sec. III B)			
$\Phi^{\text{HE}}/10^{-18}\text{GeV}^{-1}\text{sr}^{-1}\text{s}^{-1}\text{cm}^{-2}$	0.787	0.36	0.00,3.00
$\log_{10}$ of pivot energy, $E_{\text{break}}^{\text{HE}}/\text{GeV}$	-	-	4.00,6.00
$\Delta\gamma_1^{\text{HE}}$ , tilt from -2.5	0.00	0.36	-2.00,2.00
$\Delta\gamma_2^{\text{HE}}$ , tilt from -2.5	0.00	0.36	-2.00,2.00



**Broken power law to describe the prompt atmospheric + astrophysical flux**

# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. **Bulk ice properties**
4. Local DOM response
5. Neutrino attenuation
6. Overall normalization

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range
<b>Bulk ice (Sec. III E)</b>			
Amplitude 0	0.00	1.00	-3.00,3.00
Amplitude 1	0.00	1.00	-3.00,3.00
Amplitude 2	0.00	1.00	-3.00,3.00
Amplitude 3	0.00	1.00	-3.00,3.00
Amplitude 4	0.00	1.00	-3.00,3.00
Phase 1	0.00	1.00	-3.00,3.00
Phase 2	0.00	1.00	-3.00,3.00
Phase 3	0.00	1.00	-3.00,3.00
Phase 4	0.00	1.00	-3.00,3.00

**Variations in ice model characterized by correlated Fourier modes in energy and zenith space via the SnowStorm method (IceCube 2019). Ice properties are constrained by LED flasher data (IceCube 2013)**

# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. Bulk ice properties
4. **Local DOM response**
5. Neutrino attenuation
6. Overall normalization

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range
<u>Local response of DOMs (Sec. IIID)</u>			
DOM efficiency	1.00	0.10	0.97,1.06
Forward hole ice	-1.00	10.00	-5.35,1.85

**Captures photon detection efficiency of the DOMs as well as behavior of refrozen ice along strings**



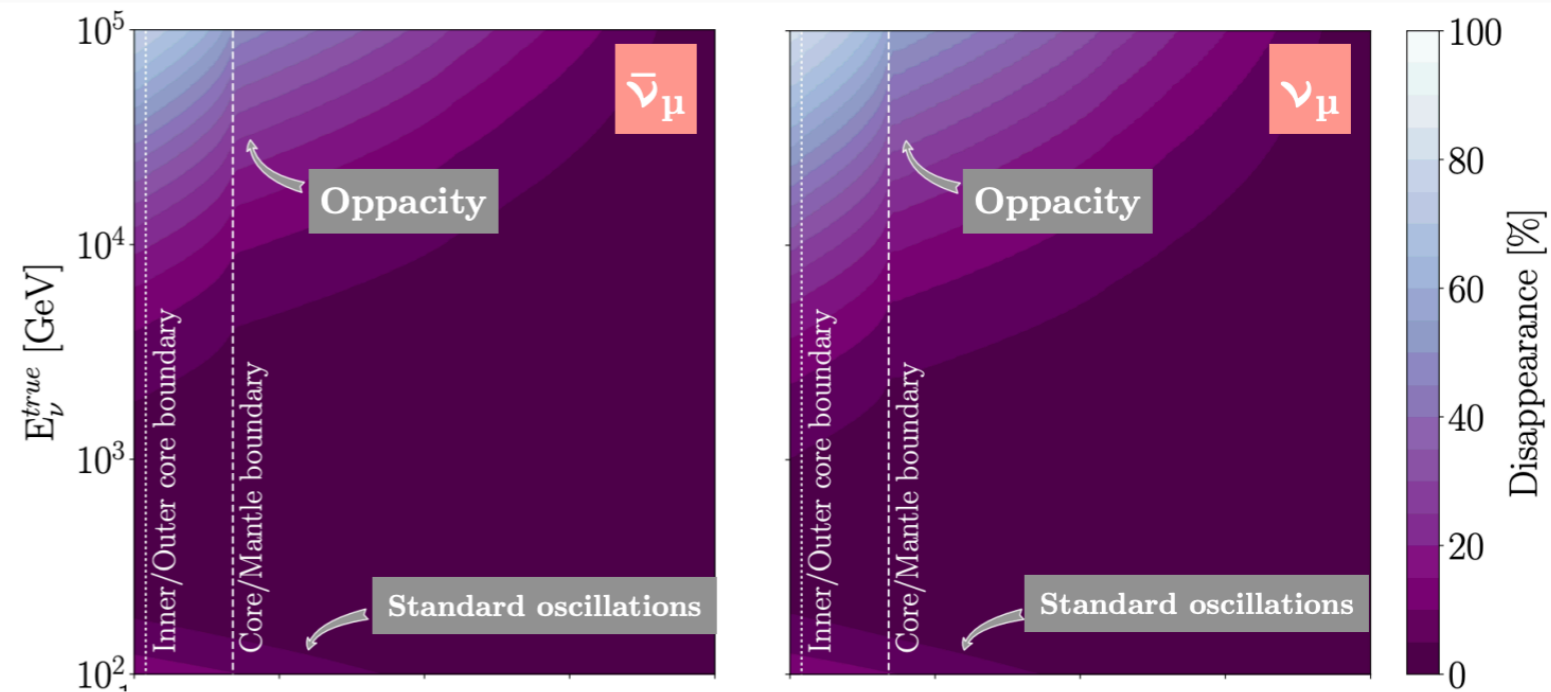
# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. Bulk ice properties
4. Local DOM response
5. **Neutrino attenuation**
6. Overall normalization

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range
Neutrino attenuation (Sec. III F)			
$\nu$ attenuation	1.00	0.10	0.82, 1.18
$\bar{\nu}$ attenuation	1.00	0.10	0.82, 1.18

**Captures the attenuation of high-energy ( $E_\nu \gtrsim 40$  TeV) neutrinos as they pass through the Earth**



# Systematic Uncertainties

## 6 major categories

1. Conventional flux
2. Non-conventional flux
3. Bulk ice properties
4. Local DOM response
5. Neutrino attenuation
6. **Overall normalization**

Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range
Overall normalization (Sec. III C)			
Norm	1.00	0.2	0.10,3.00

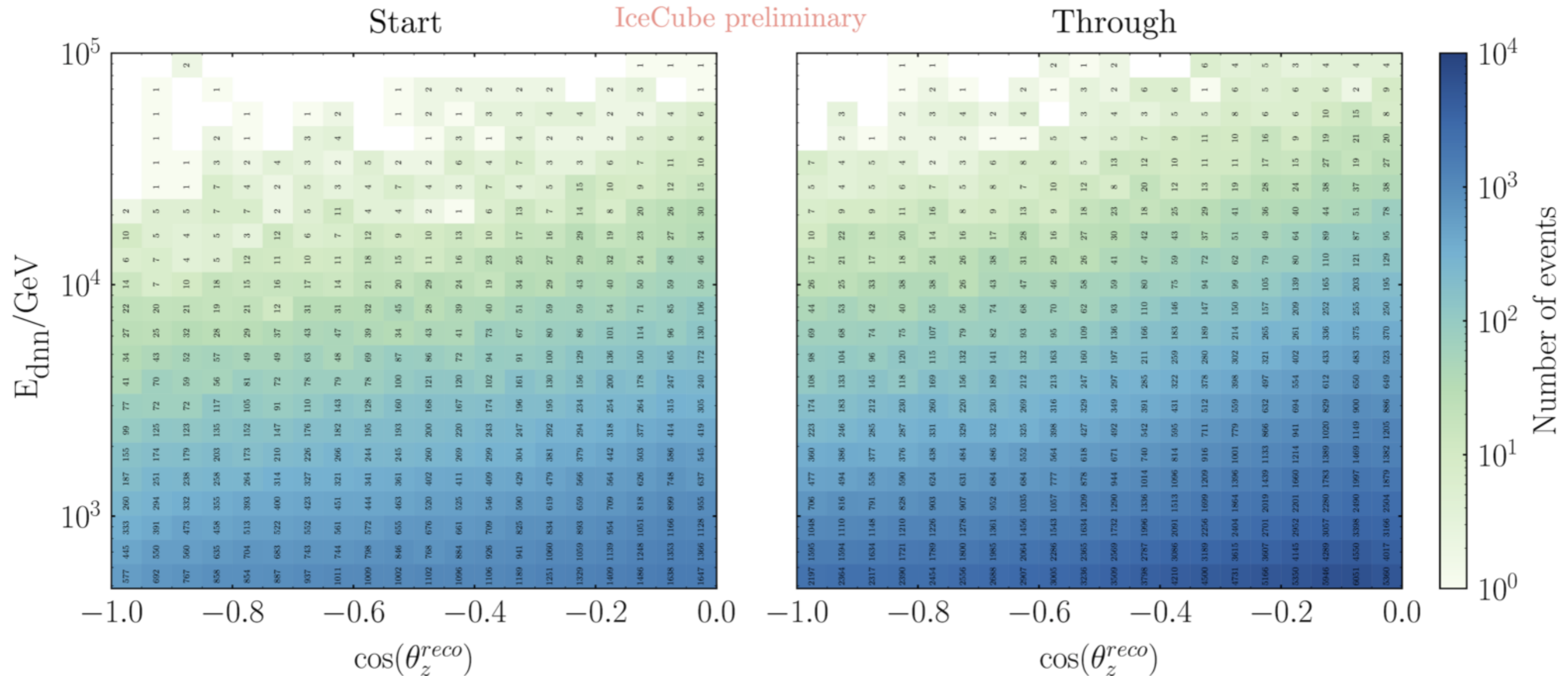
**Captures uncertainties in overall flux normalization, total cross section, and muon energy loss in matter**

# Fit Strategy

- Binned likelihood in  $\{E_\nu^{\text{reco}}, \cos \theta_z^{\text{reco}}\}$
- Log-likelihood ratio test statistic marginalizing over the nuisance parameters with Gaussian priors
- Main result is a frequentist analysis with p-values computed assuming Wilks' theorem for two degrees of freedom
- Cross-checked with a Bayesian analysis
  - Not presented here, though results are consistent with the frequentist analysis

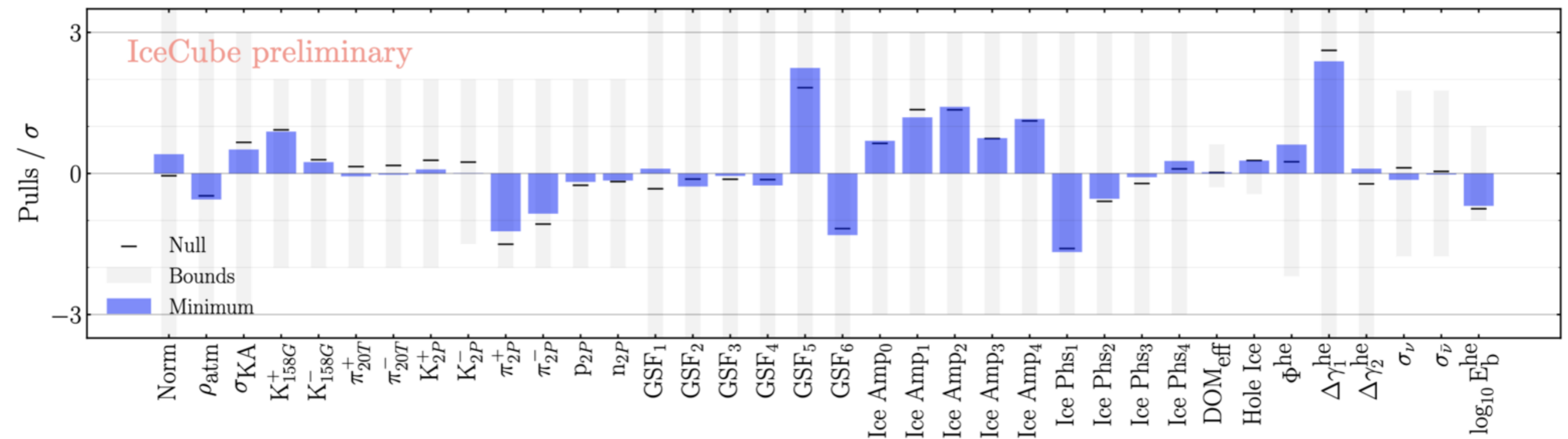
# Data Sample

- Around 93K/270K starting/through-going  $\nu_\mu$  candidate events in 10.7 years



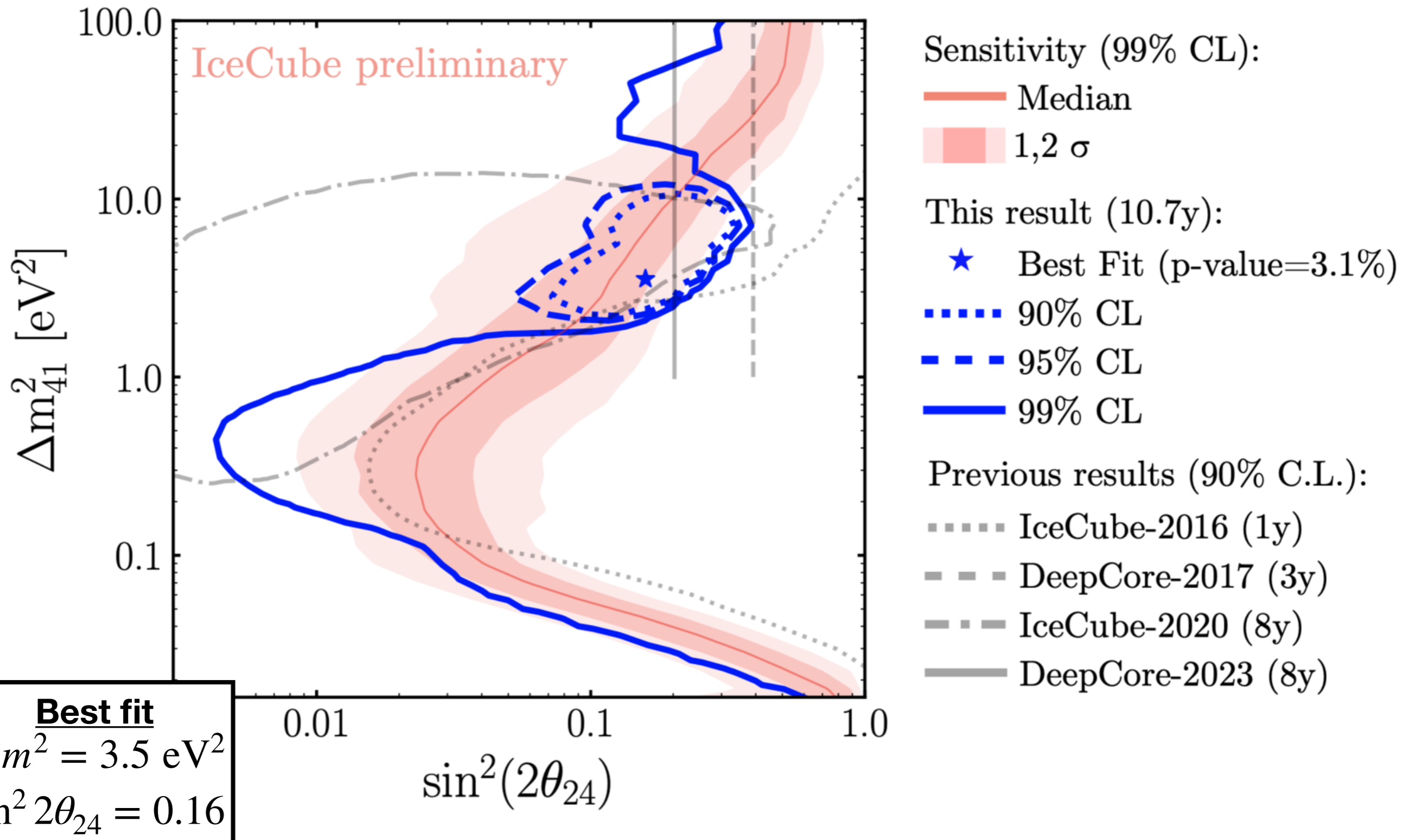


# Post-fit systematics



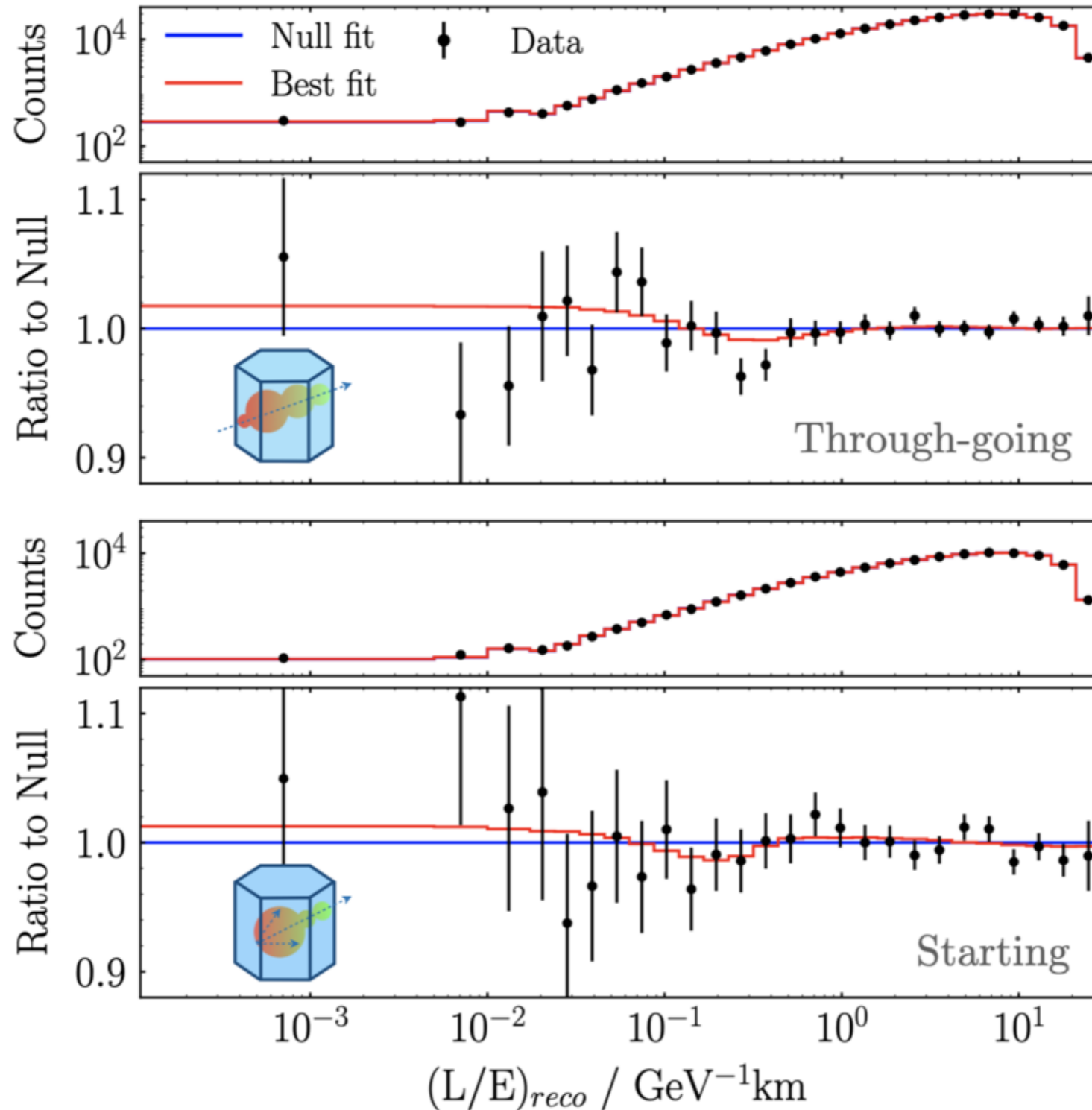
**Similar systematic pulls between best fit and null**

# Oscillation Fit Result



# Oscillation Fit Result

IceCube preliminary



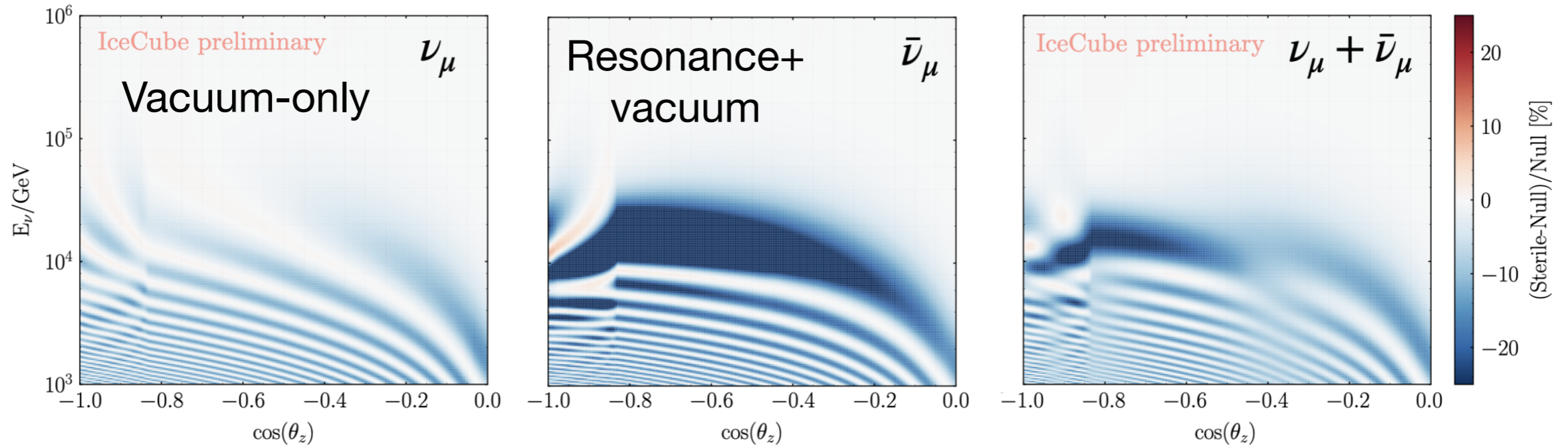
**Best fit**

$$\Delta m^2 = 3.5 \text{ eV}^2$$

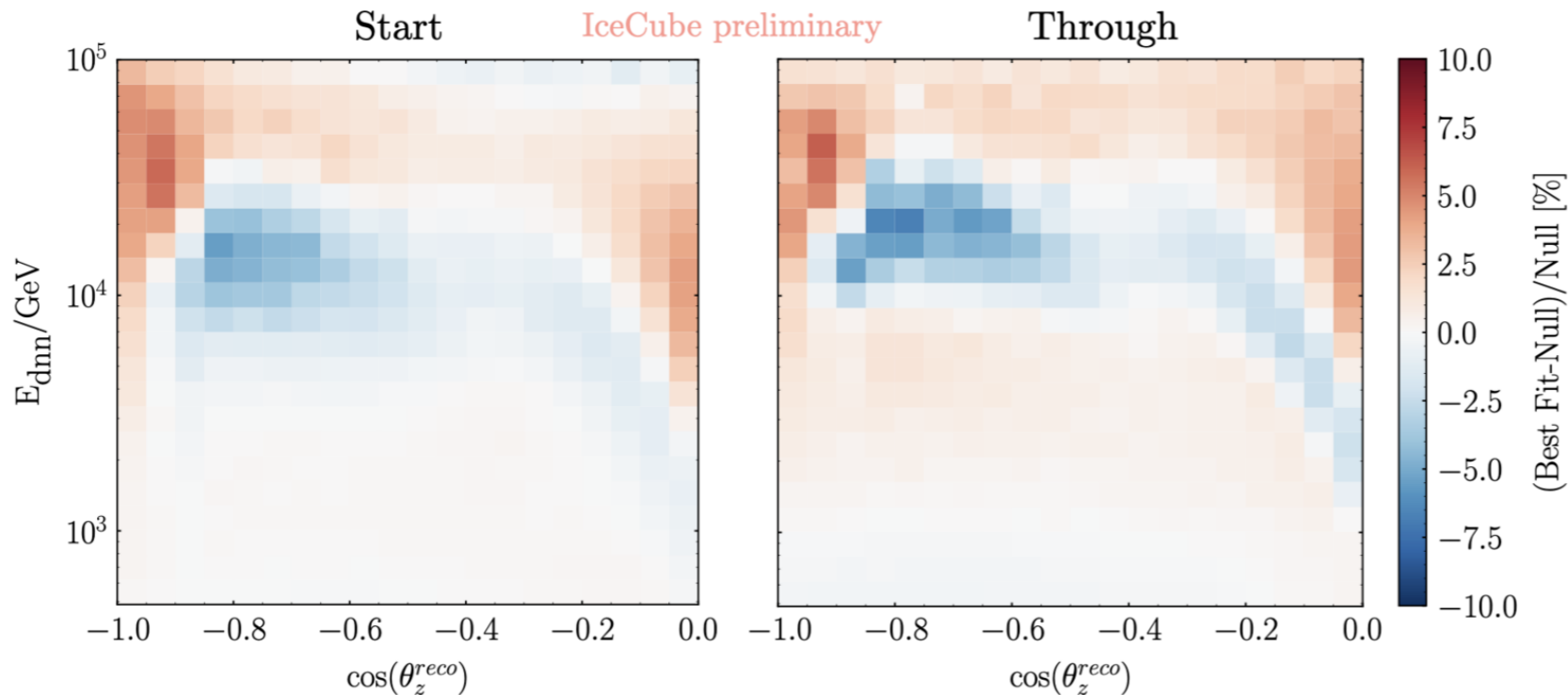
$$\sin^2 2\theta_{24} = 0.16$$

# Where does our significance come from?

Without detector effects



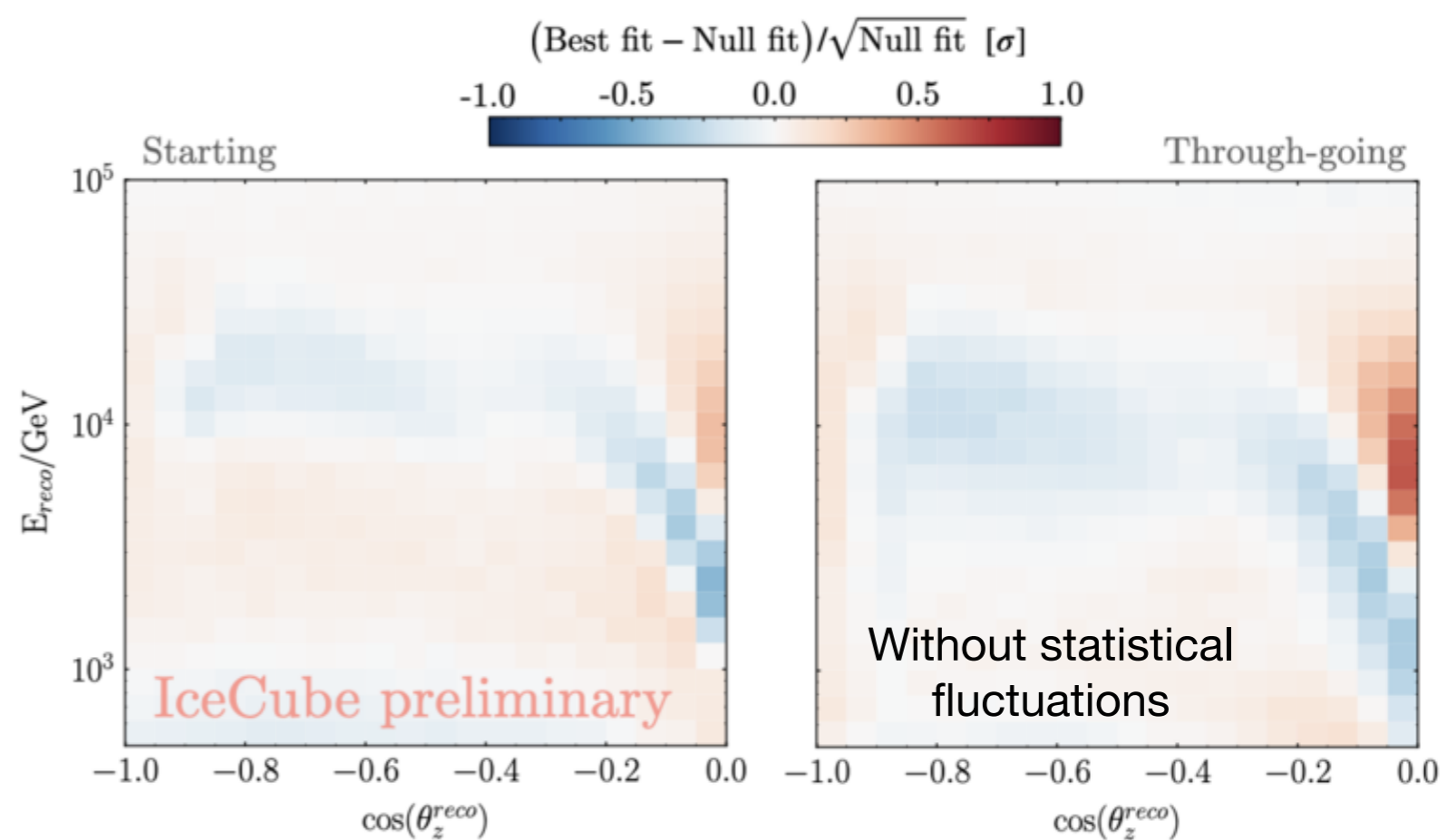
With detector effects, without statistical fluctuations





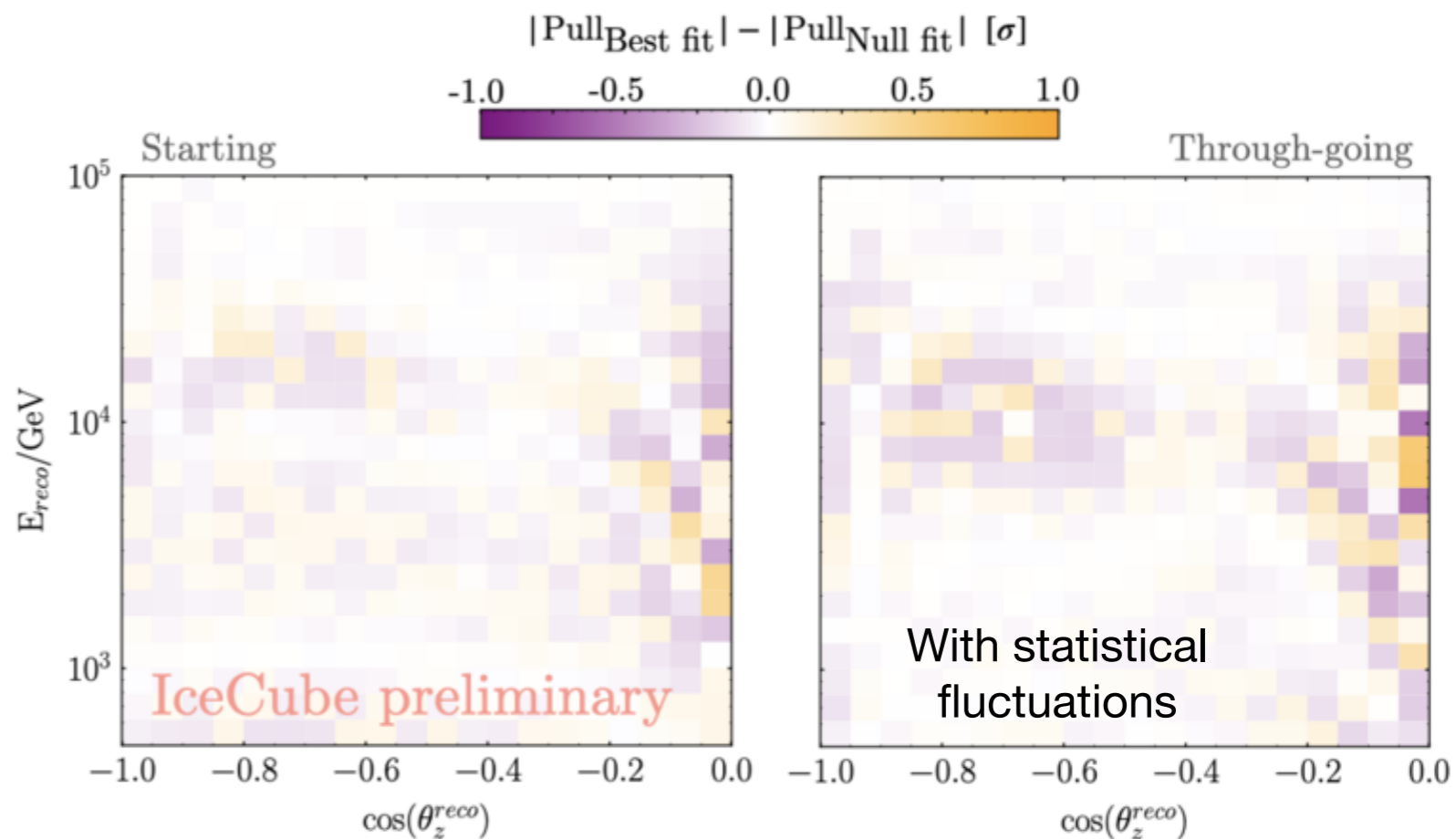
$$\text{Pull} \equiv \frac{\text{Best fit} - \text{Null fit}}{\sqrt{\text{Null fit}}}$$

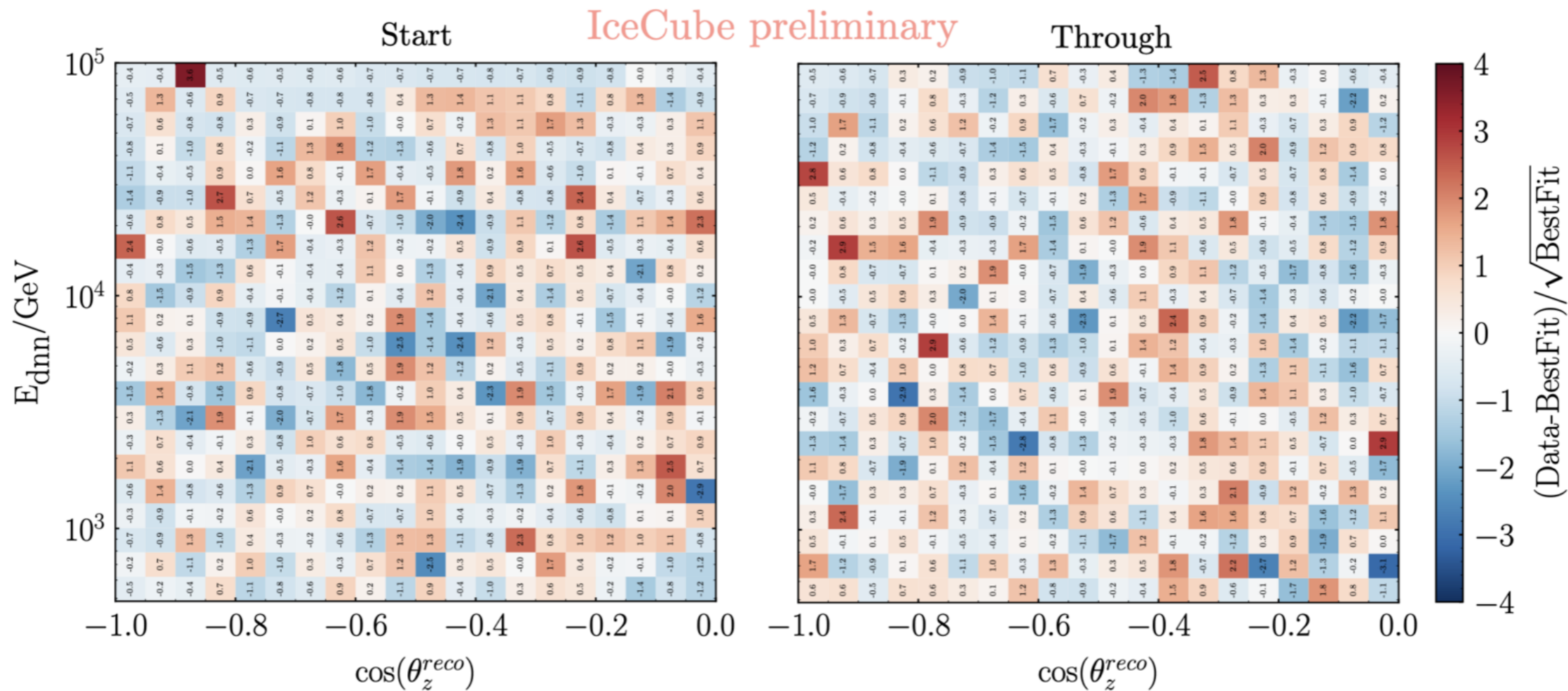
**Red: excess in best fit v.s. null**  
**Blue: deficit in best fit v.s. null**



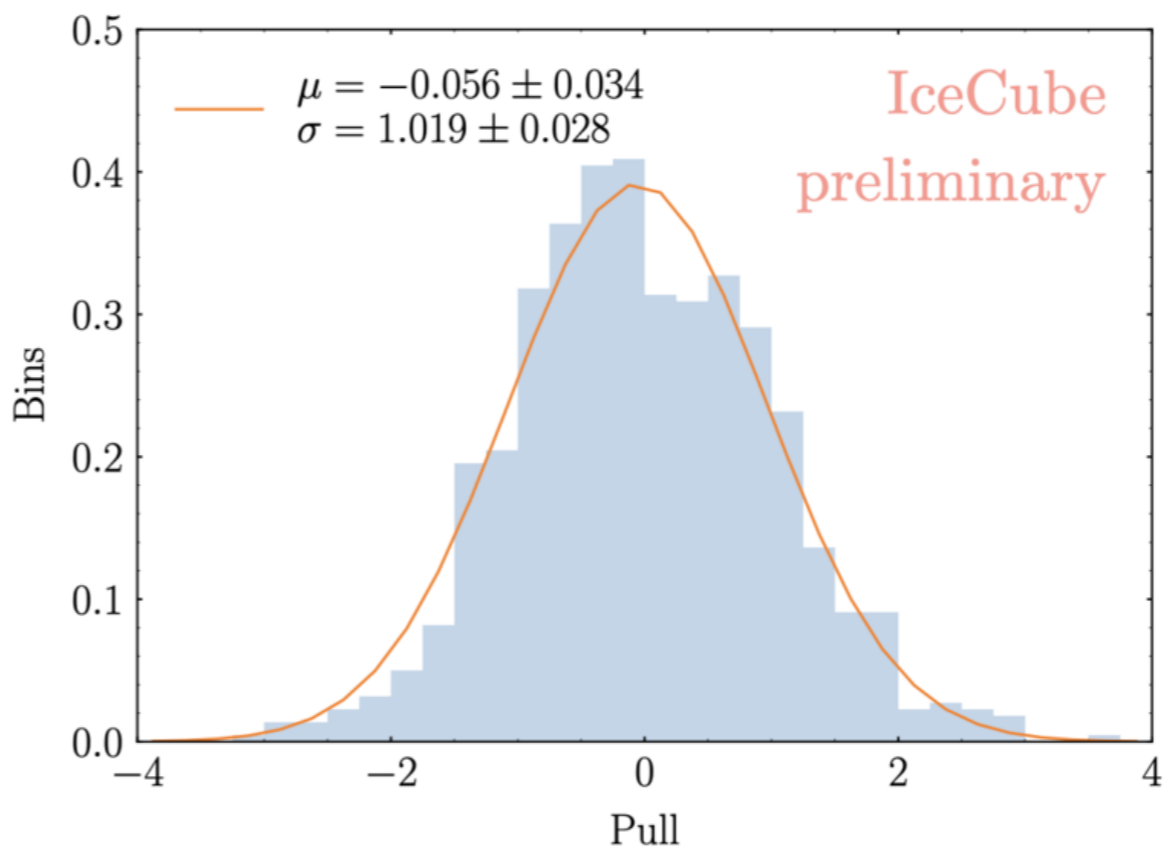
$$\text{Pull} \equiv \frac{\text{Data} - \text{Fit}}{\sqrt{\text{Fit}}}$$

**Yellow: data prefers null fit**  
**Purple: data prefers oscillation fit**

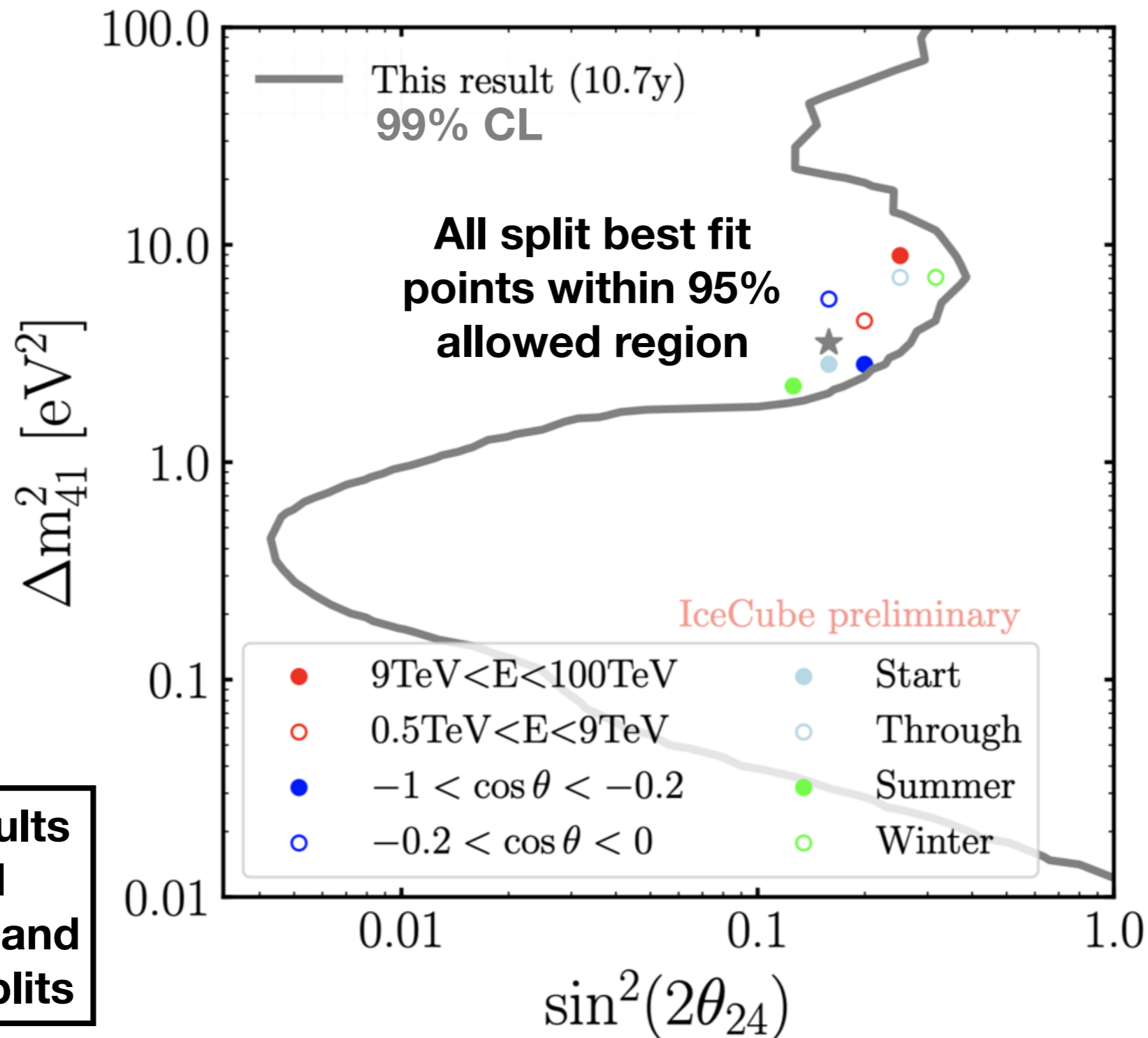




**Good agreement  
between data and MC  
at best fit (goodness of  
fit p-value ~12%)**



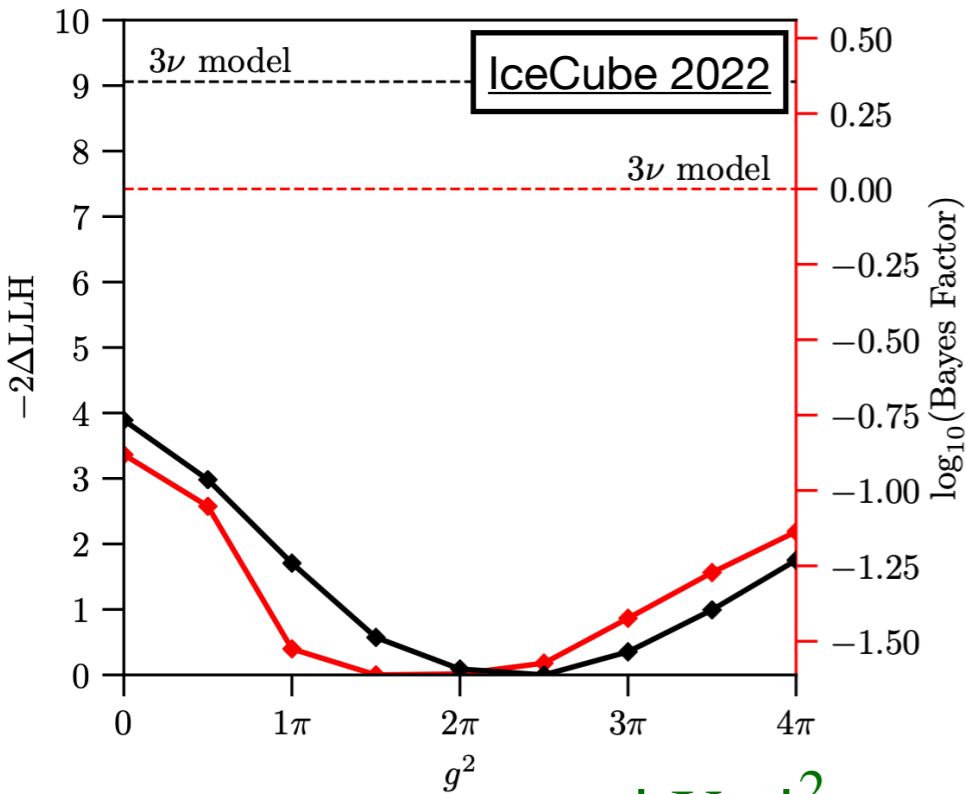
# Post-unblinding checks



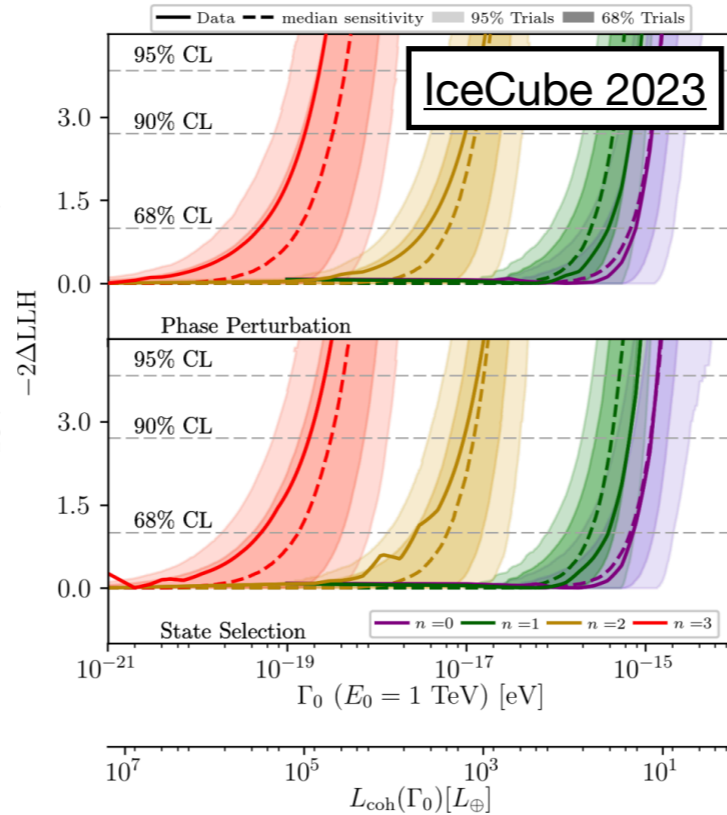
**Consistent results  
in azimuthal  
direction splits and  
year-by-year splits**

# Related Work in IceCube

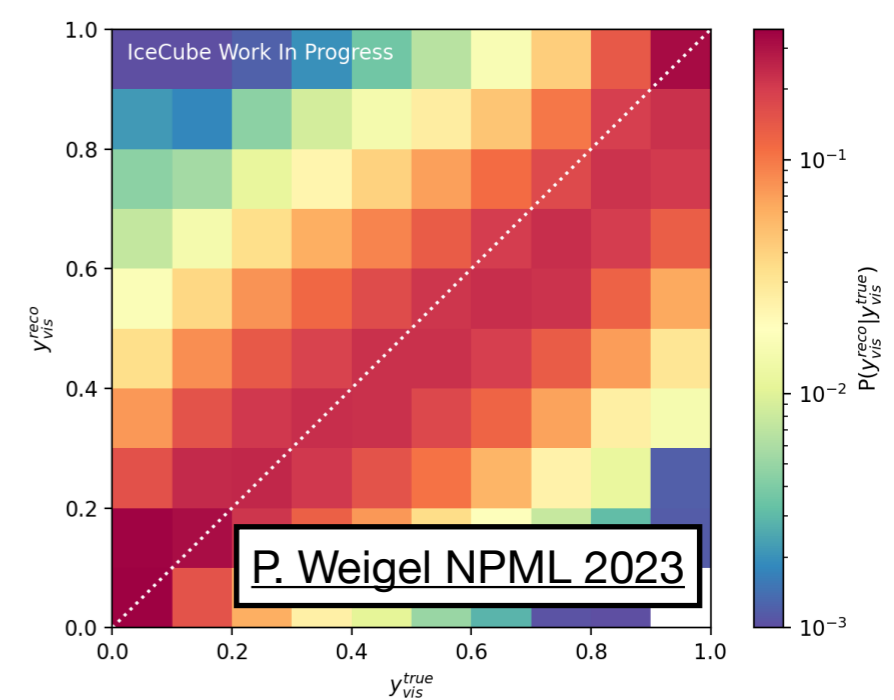
## 3+1 with decay



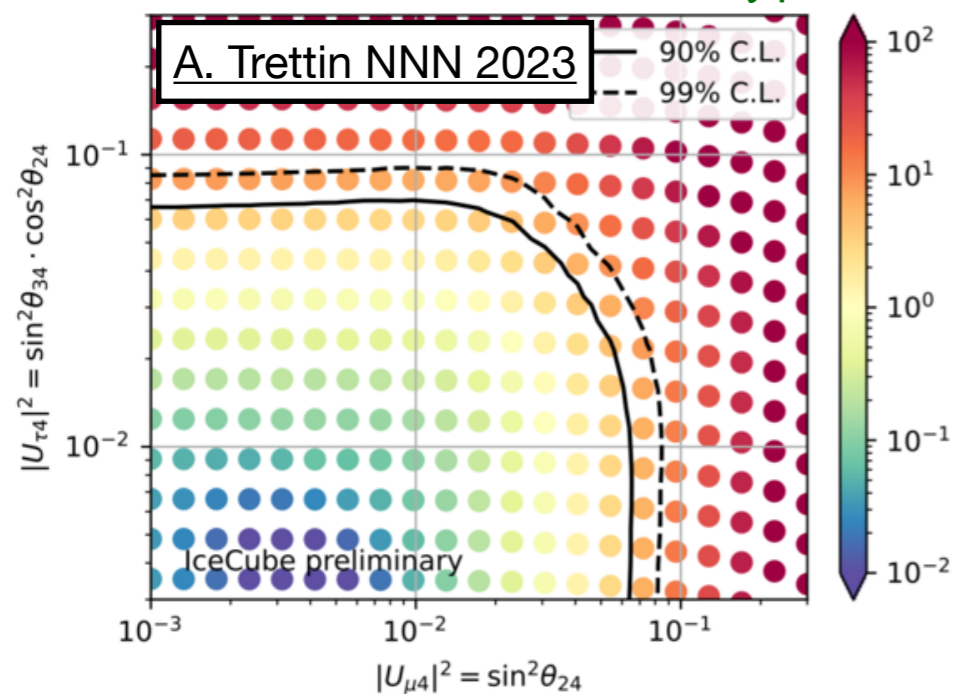
## Decoherence



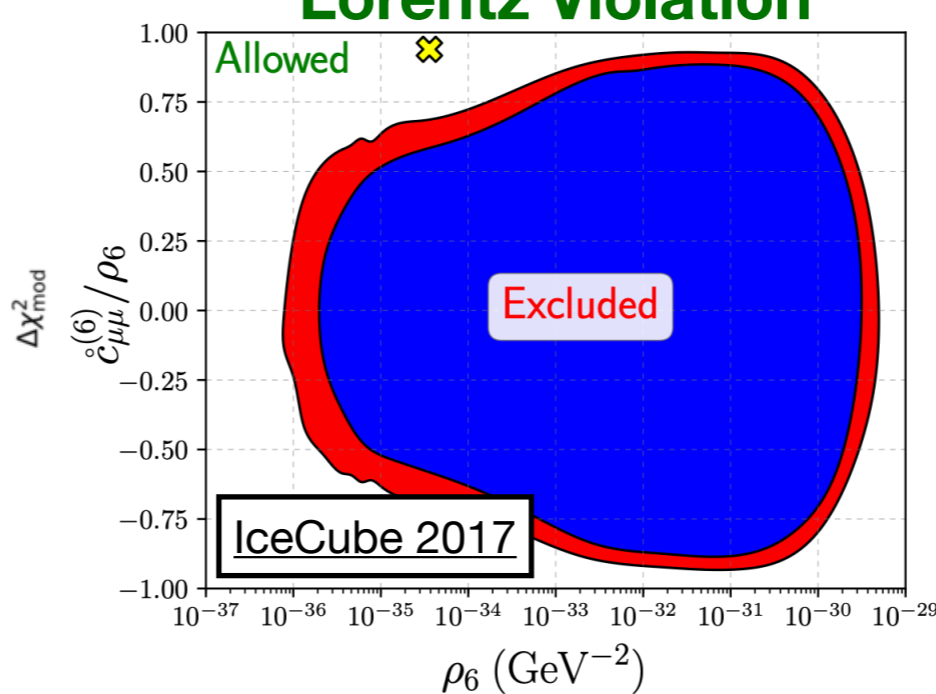
## 3+1 w/ Inelasticity



## 3+1 w/ nonzero $|U_{\tau 4}|^2$



## Lorentz Violation



Updated analyses coming soon!

# Conclusion

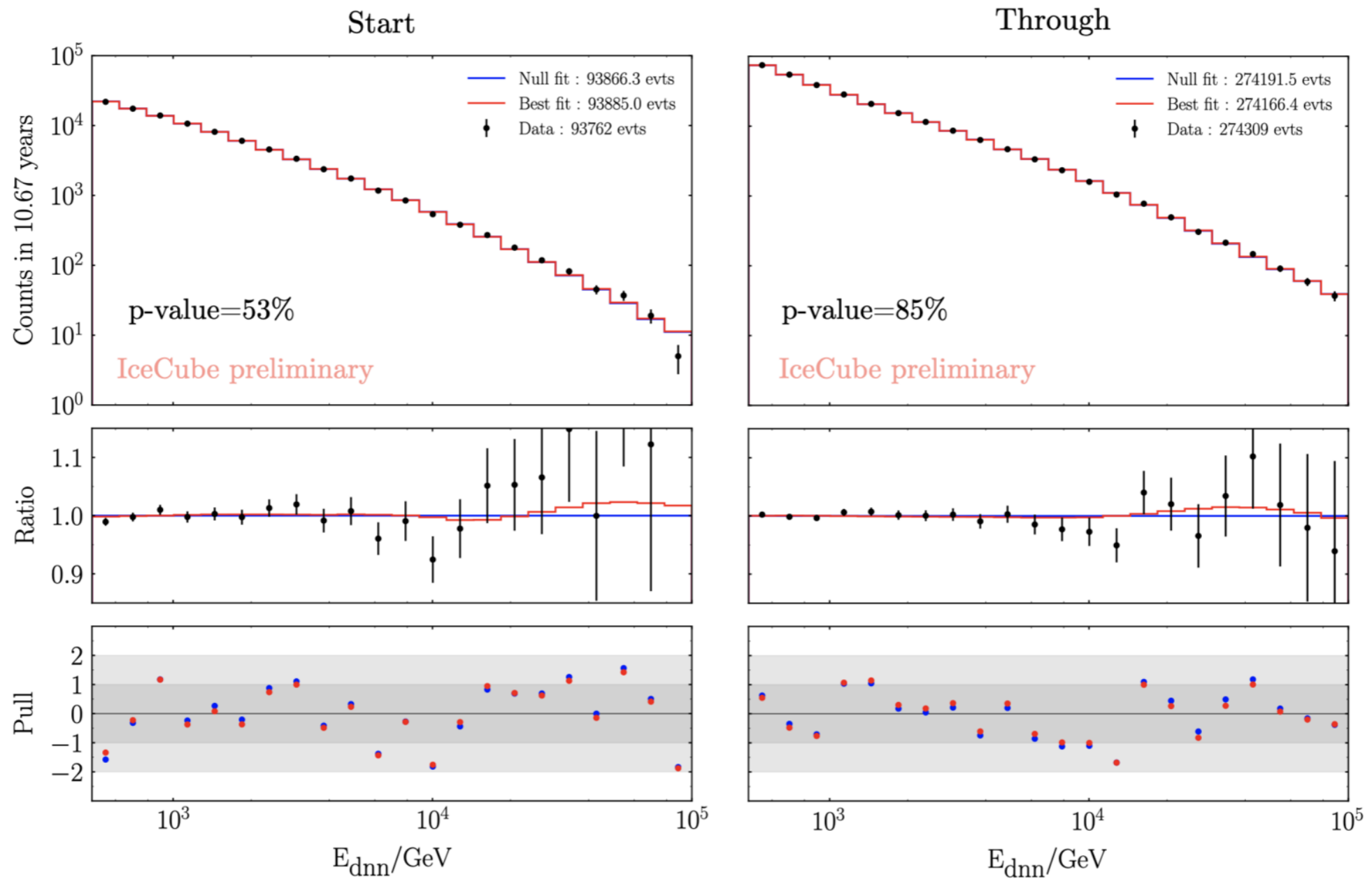
- IceCube has performed a search for sterile neutrino oscillation imprints in 10.7 years of atmospheric muon neutrino data
  - Sensitivity from matter-enhanced resonance
  - Improvements to event selection, reconstruction, and systematic treatment
- Best fit at  $\Delta m^2 = 3.5 \text{ eV}^2$ ,  $\sin^2 2\theta_{24} = 0.16$ 
  - Consistent with best fit (null) at 12% (3.1%)
- Results from related analyses on the way
- **Data release for the 8-year version of this analysis available here: <https://dataverse.harvard.edu>**



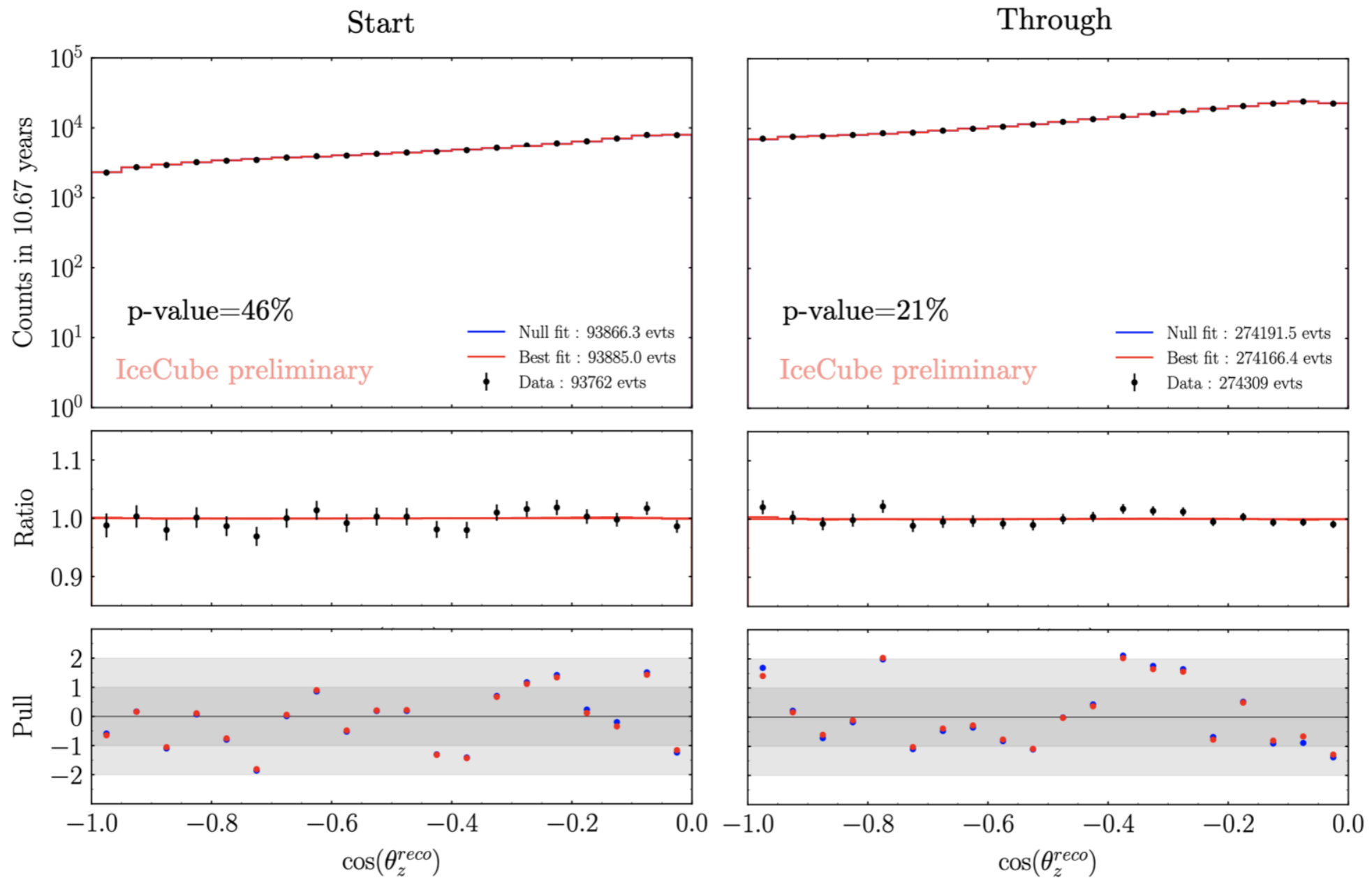
**Thank you!**

# Backups

# 1D Distributions



# 1D Distributions



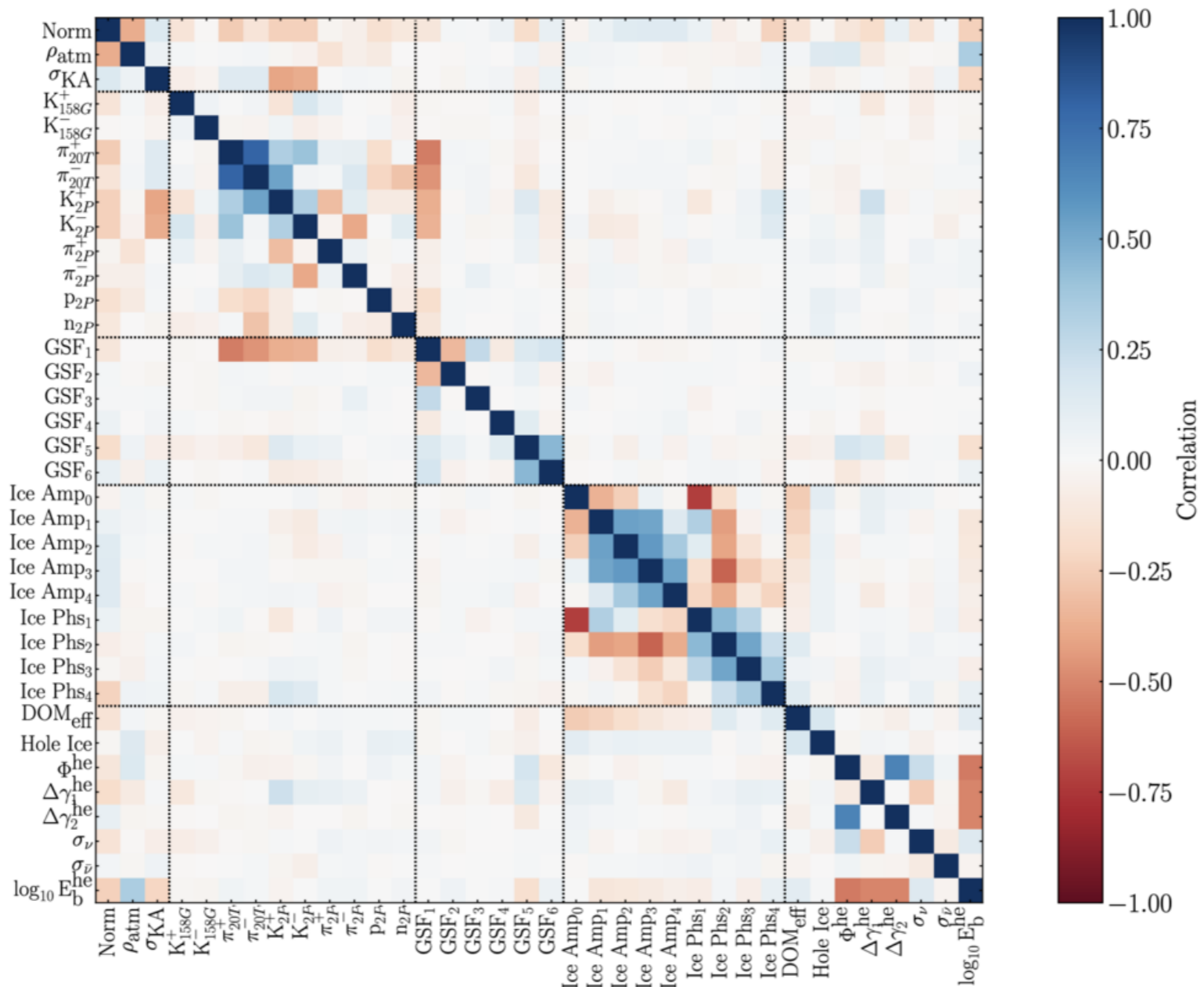
# Data Rates

Component	Starting	Through-going
Conv. $\nu_\mu$	90848.2	260339.6
Non-conv. $\nu_\mu$	765.6	4253.6
All $\nu_e$	0.5	0.2
All $\nu_\tau$	60.0	258.0
Atmospheric $\mu$	2.3	4.2
Data	93762	274309

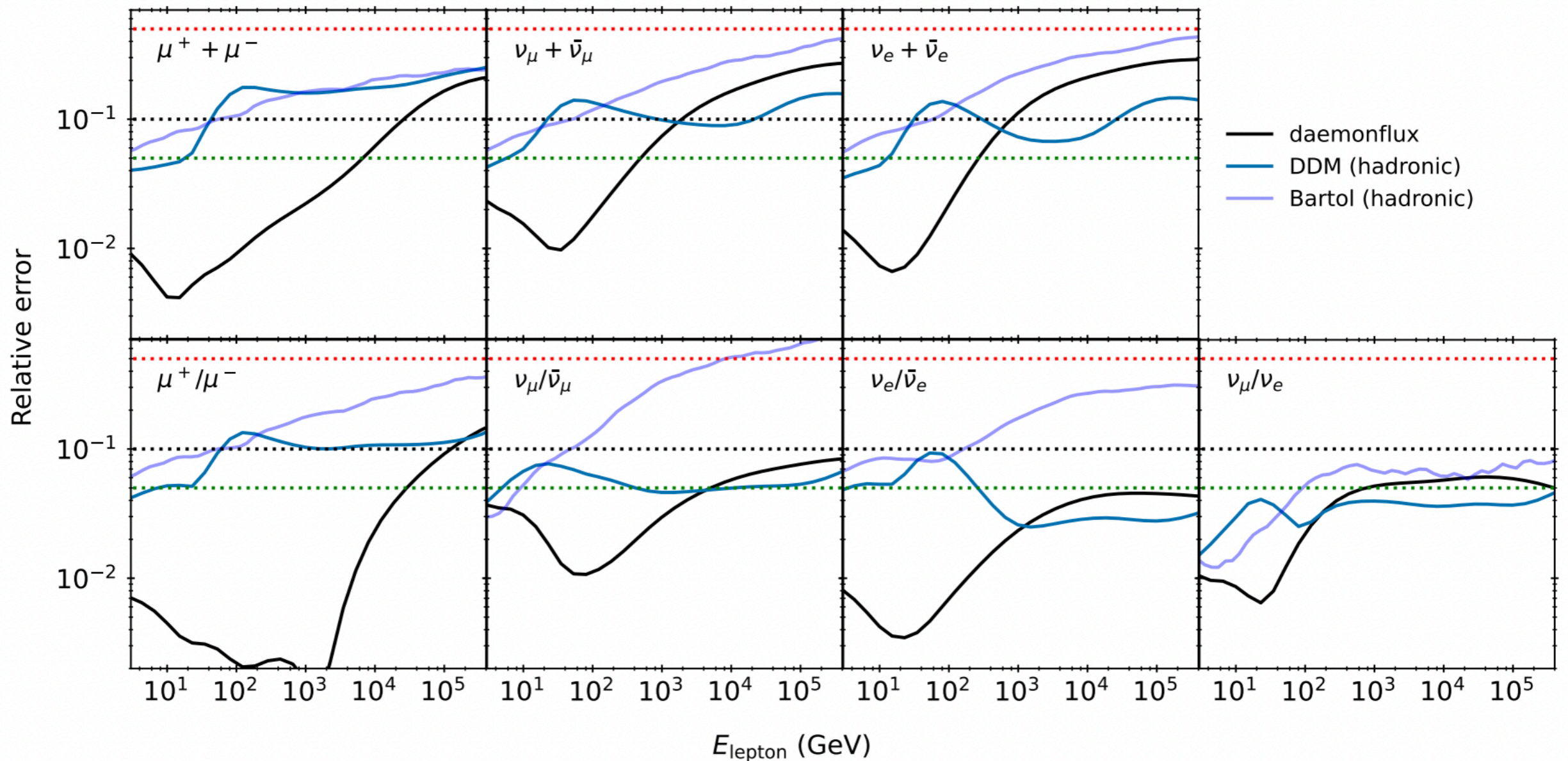


# Best-fit systematic correlations

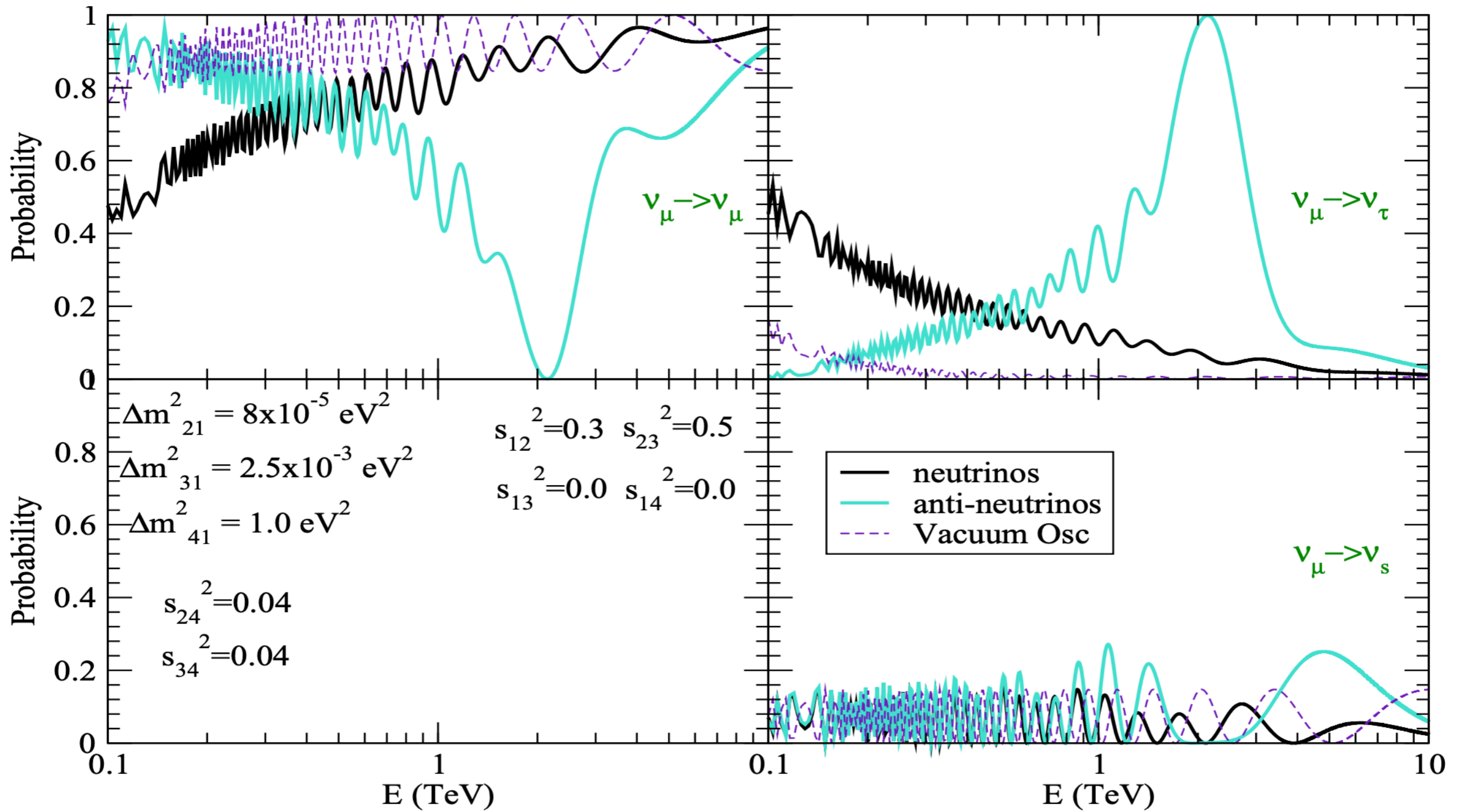
IceCube preliminary



# Daemonflux high energy uncertainties

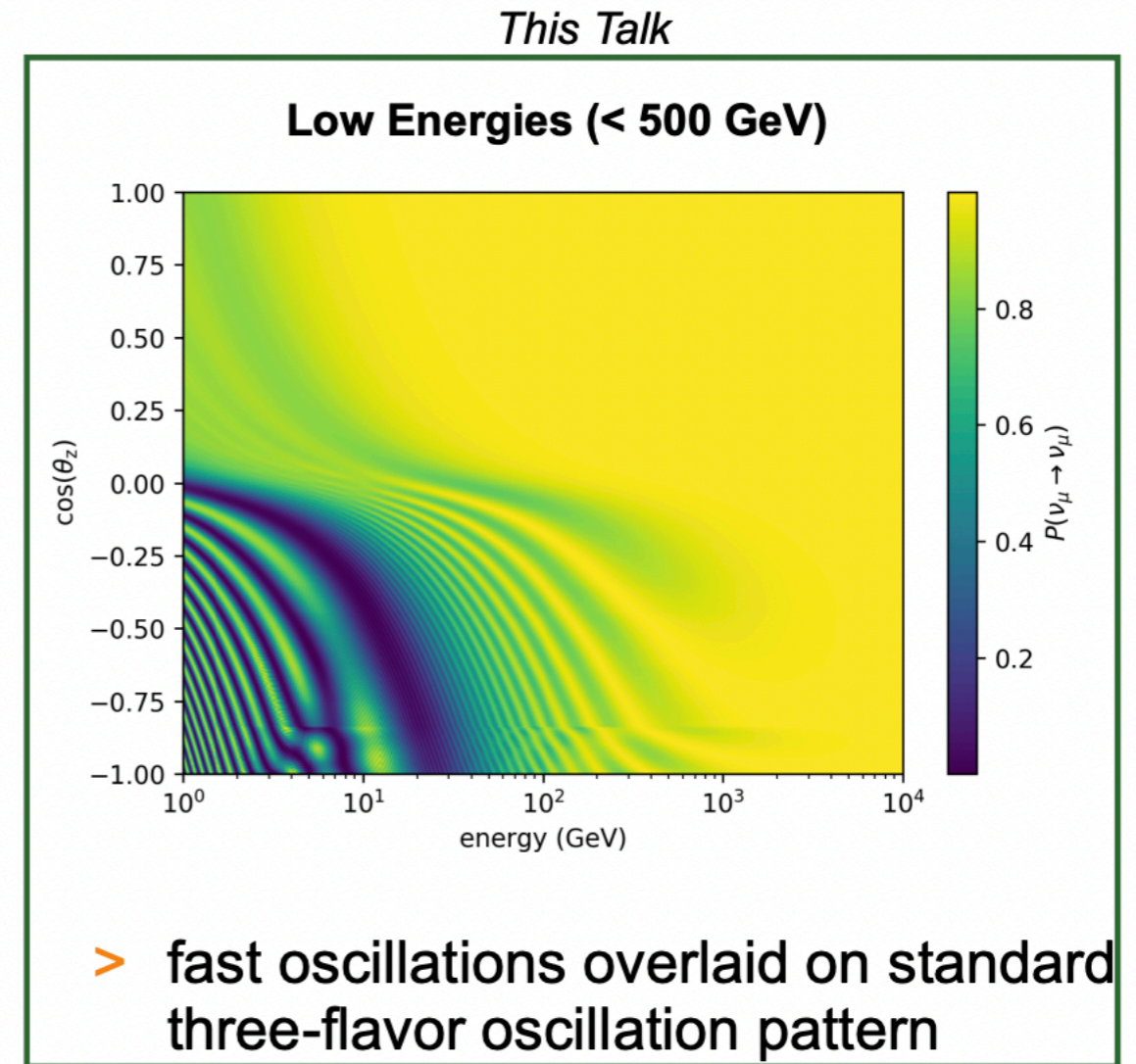
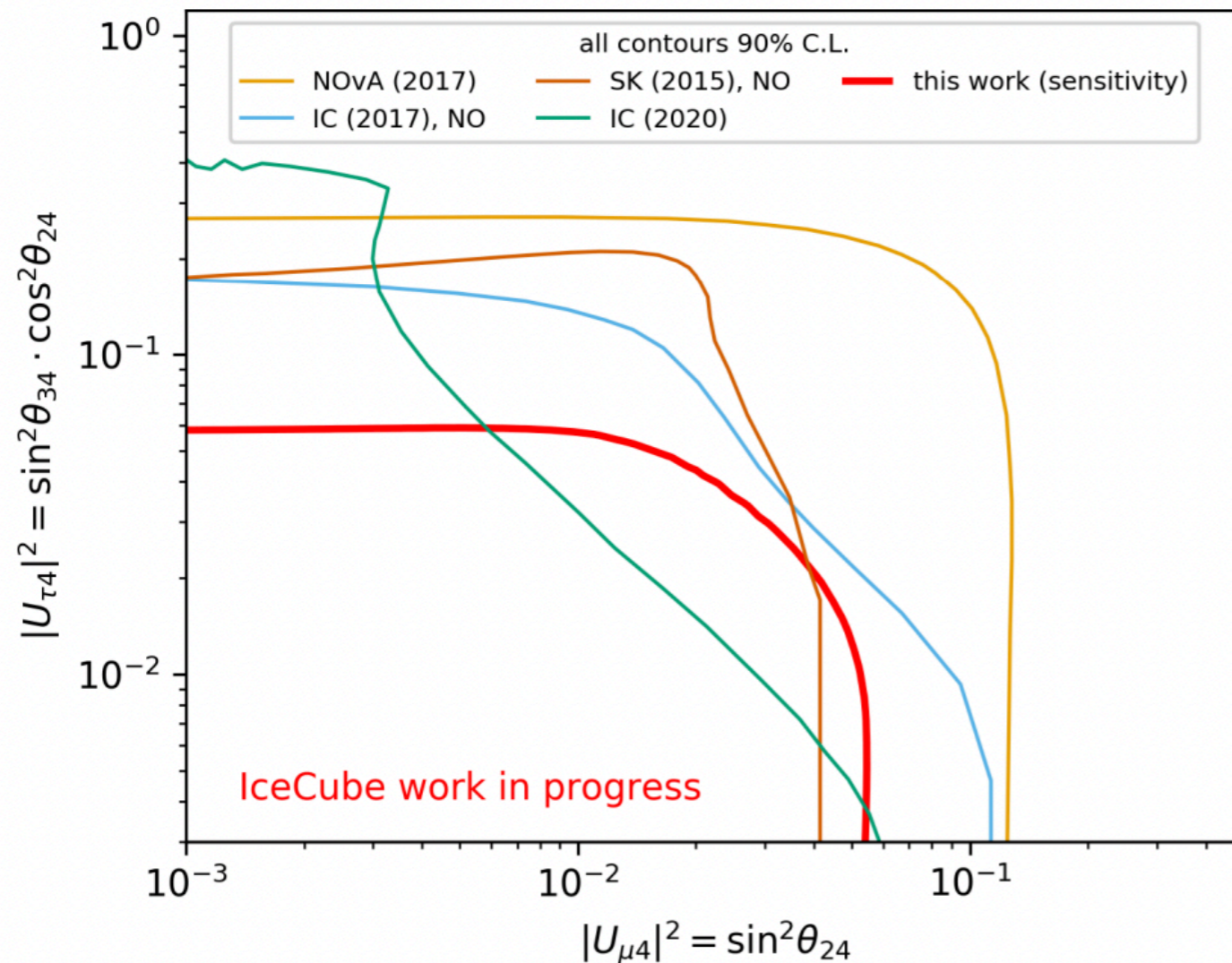


Nuisance parameter	Central value	$1\sigma$ width of prior	Allowed range	Pull Null Fit	Pull Best Fit	Pull Difference abs(Null-Best Fit)	
Overall normalization (Sec. III C)							
Norm	1.00	0.2	0.10,3.00	-0.05	0.41	0.46	
Local response of DOMs (Sec. III D)							
DOM efficiency	1.00	0.10	0.97,1.06	0.02	0.03	0.01	
Forward hole ice	-1.00	10.00	-5.35,1.85	0.28	0.27	0.01	
Bulk ice (Sec. III E)							
Amplitude 0	0.00	1.00	-3.00,3.00	0.64	0.69	0.05	
Amplitude 1	0.00	1.00	-3.00,3.00	1.36	1.19	0.17	
Amplitude 2	0.00	1.00	-3.00,3.00	1.35	1.42	0.07	
Amplitude 3	0.00	1.00	-3.00,3.00	0.74	0.75	0.01	
Amplitude 4	0.00	1.00	-3.00,3.00	1.12	1.16	0.04	
Phase 1	0.00	1.00	-3.00,3.00	-1.60	-1.67	0.07	
Phase 2	0.00	1.00	-3.00,3.00	-0.59	-0.54	0.05	
Phase 3	0.00	1.00	-3.00,3.00	-0.21	-0.08	0.13	
Phase 4	0.00	1.00	-3.00,3.00	0.10	0.27	0.17	
Conventional flux (Sec. III A)							
Atm. density ( $\rho_{\text{atm}}$ )	0.00	1.00	-3.00,3.00	-0.48	-0.55	0.07	
Kaon energy loss ( $\sigma_{\text{K-Air}}$ )	0.00	1.00	-3.00,3.00	0.66	0.51	0.15	
Hadronic production	$\text{K}_{158G}^+$	0.00	1.00	-2.00,2.00	0.93	0.89	0.04
	$\text{K}_{158G}^-$	0.00	1.00	-2.00,2.00	0.29	0.24	0.05
	$\pi_{20T}^+$	0.00	1.00	-2.00,2.00	0.15	-0.06	0.21
	$\pi_{20T}^-$	0.00	1.00	-2.00,2.00	0.17	-0.03	0.20
	$\text{K}_{2P}^+$	0.00	1.00	-1.00,2.00	0.28	0.09	0.19
	$\text{K}_{2P}^-$	0.00	1.00	-1.50,2.00	0.24	0.01	0.23
	$\pi_{2P}^+$	0.00	1.00	-2.00,2.00	-1.50	-1.23	0.27
	$\pi_{2P}^-$	0.00	1.00	-2.00,2.00	-1.08	-0.85	0.23
	$\text{p}_{2P}$	0.00	1.00	-2.00,2.00	-0.25	-0.18	0.07
	$\text{n}_{2P}$	0.00	1.00	-2.00,2.00	-0.17	-0.15	0.02
CR spectrum	GSF <sub>1</sub>	0.00	1.00	-4.00,4.00	-0.33	0.10	0.43
	GSF <sub>2</sub>	0.00	1.00	-4.00,4.00	-0.12	-0.28	0.16
	GSF <sub>3</sub>	0.00	1.00	-4.00,4.00	-0.12	-0.05	0.07
	GSF <sub>4</sub>	0.00	1.00	-4.00,4.00	-0.13	-0.25	0.12
	GSF <sub>5</sub>	0.00	1.00	-4.00,4.00	1.82	2.24	0.42
	GSF <sub>6</sub>	0.00	1.00	-4.00,4.00	-1.17	-1.31	0.14
Non-conventional flux (Sec. III B)							
$\Phi^{\text{HE}}/10^{-18}\text{GeV}^{-1}\text{sr}^{-1}\text{s}^{-1}\text{cm}^{-2}$	0.787	0.36	0.00,3.00	0.25	0.61	0.36	
$\log_{10}$ of pivot energy, $E_{\text{break}}^{\text{HE}}/\text{GeV}$	-	-	4.00,6.00	*4.25	*4.31	N/A, see caption	
$\Delta\gamma_1^{\text{HE}}$ , tilt from -2.5	0.00	0.36	-2.00,2.00	2.62	2.39	0.23	
$\Delta\gamma_2^{\text{HE}}$ , tilt from -2.5	0.00	0.36	-2.00,2.00	-0.22	0.10	0.21	
Neutrino attenuation (Sec. III F)							
$\nu$ attenuation	1.00	0.10	0.82, 1.18	0.12	-0.14	0.26	
$\bar{\nu}$ attenuation	1.00	0.10	0.82, 1.18	0.04	-0.02	0.06	





# DeepCore Sterile Analysis



Credit: [A. Trettin VLVnT 2021](#)

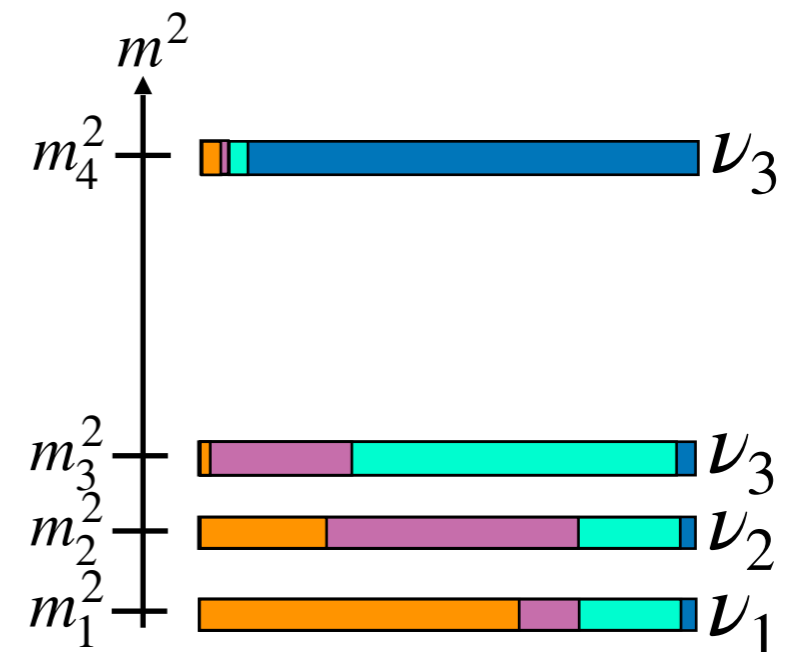


# The 3+1 Model

- Most common explanation: new eV-scale mass eigenstate
- Invisible Z width measurements mean this state must be mostly sterile
- Facilitates oscillations at shorter baseline than those involving active neutrinos



$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{\mu1} & U_{\tau1} & U_{s1} \\ U_{e2} & U_{\mu2} & U_{\tau2} & U_{s2} \\ U_{e3} & U_{\mu3} & U_{\tau3} & U_{s3} \\ U_{e4} & U_{\mu4} & U_{\tau4} & U_{s4} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \end{bmatrix}$$



(Normal Ordering)

# Tension in Global Fits

$$P(\nu_\mu \rightarrow \nu_e) = 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**SBL Accelerator**

$$P(\nu_e \rightarrow \nu_e) = 1 - 4 |U_{e4}|^2 (1 - |U_{e4}|^2) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**SBL Gallium/Reactor**

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4 |U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**LBL Accelerator/Atmospheric**

Hardin+ 2022

	$\nu_\mu \rightarrow \nu_e$	$\nu_\mu \rightarrow \nu_\mu$	$\nu_e \rightarrow \nu_e$
$\nu$	MiniBooNE NUMI-MB NOMAD MicroBooNE	SciBooNE-MB CCFR CDHS MINOS MicroBooNE	KARMEN-LSND-xsec SAGE+GALLEX BEST MicroBooNE MiniBooNE
$\bar{\nu}$	LSND KARMEN MiniBooNE	SciBooNE-MB CCFR MINOS IceCube	Bugey NEOS DANSS PROSPECT STEREO MiniBooNE

# Tension in Global Fits

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2(2\theta_{\mu e}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**SBL Accelerator**

$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2(2\theta_{ee}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**SBL Gallium/Reactor**

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta_{\mu\mu}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

**LBL Accelerator/Atmospheric**

Hardin+ 2022

	$\nu_\mu \rightarrow \nu_e$	$\nu_\mu \rightarrow \nu_\mu$	$\nu_e \rightarrow \nu_e$
$\nu$	MiniBooNE NUMI-MB NOMAD MicroBooNE	SciBooNE-MB CCFR CDHS MINOS MicroBooNE	KARMEN-LSND-xsec SAGE+GALLEX BEST MicroBooNE MiniBooNE
$\bar{\nu}$	LSND KARMEN MiniBooNE	SciBooNE-MB CCFR MINOS IceCube	Bugey NEOS DANSS PROSPECT STEREO MiniBooNE

# Tension in Global Fits

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2(2\theta_{\mu e}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2(2\theta_{ee}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

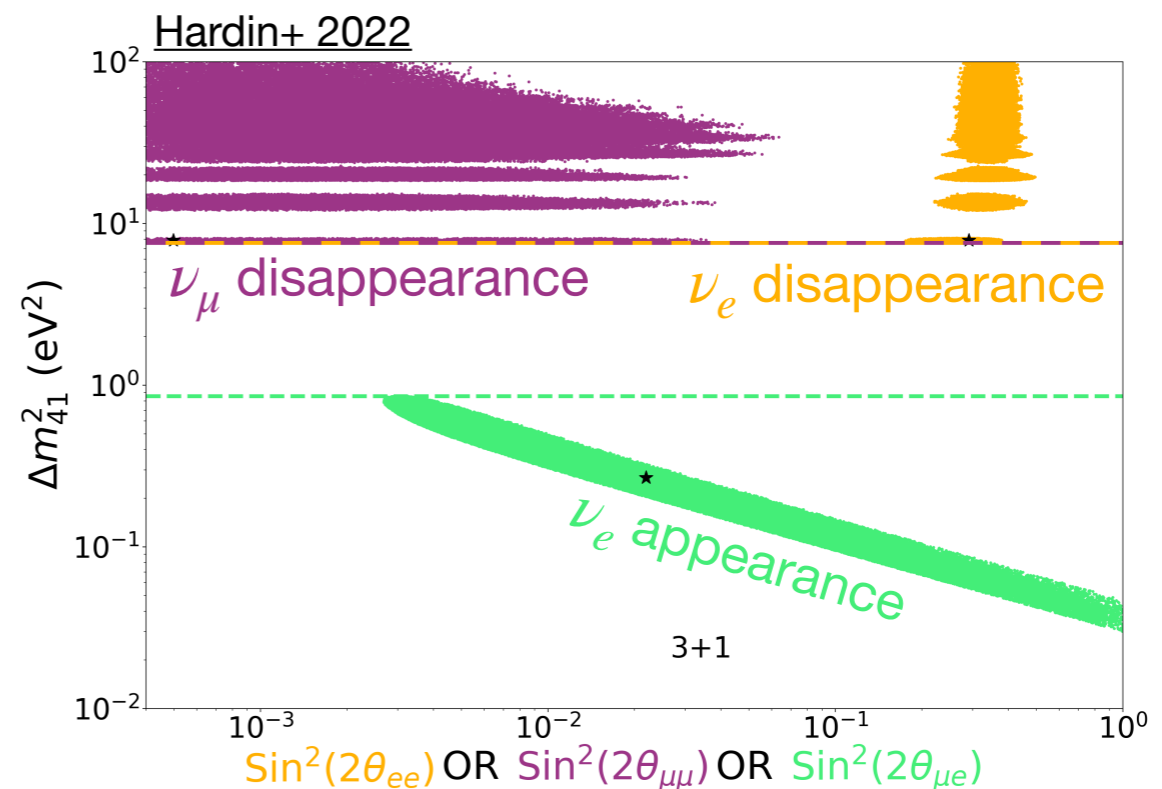
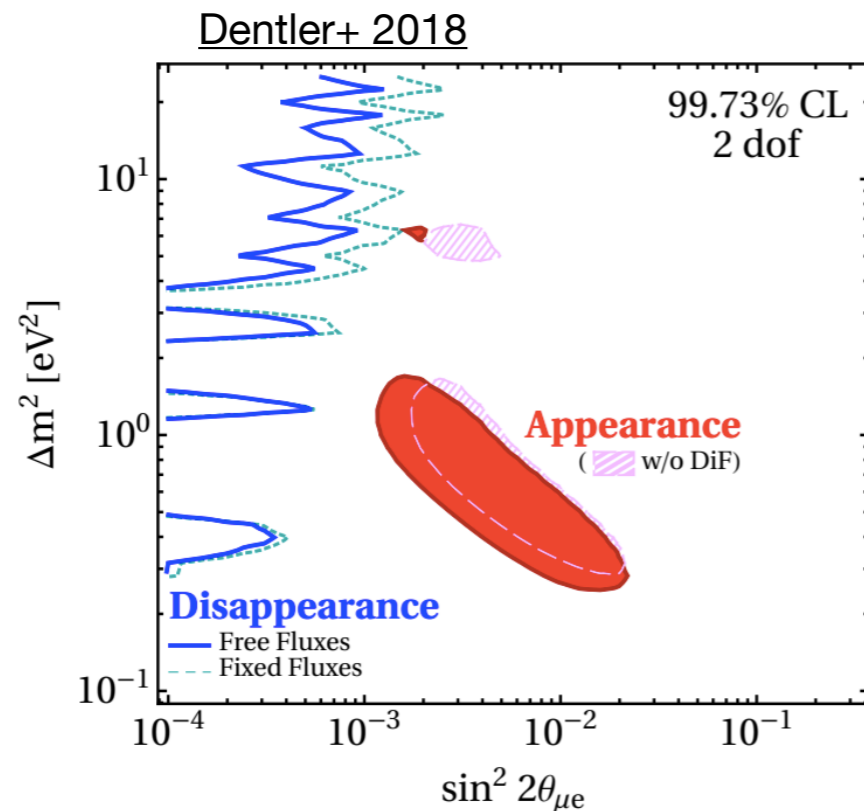
$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta_{\mu\mu}) \sin^2\left(1.27 \Delta m^2 \frac{L}{E}\right)$$

SBL Accelerator

SBL Gallium/Reactor

LBL Accelerator/Atmospheric

Lack of clear muon neutrino disappearance in tension with electron neutrino appearance/disappearance anomalies at the  $4.9\sigma$  level (Hardin+ 2022)



# Muon Neutrino Disappearance

- Strongest constraints on  $\nu_\mu$  disappearance at  $\Delta m^2 \sim 1 \text{ eV}^2$  typically come from long baseline accelerator experiments
- **Can we explore this channel in a complementary way?**

