



# **MicroBooNE's Recent Cross Section Results**

**April 2, 2024 2nd Short-Baseline Experiment-Theory Workshop**

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**Lee Hagaman (University of Chicago) On behalf of the MicroBooNE Collaboration**

*μ*+

Λ

*p*





*π*−

*νμ*

**MicroBooNE Data Run 5616 Subrun 14 Event 704**

## MicroBooNE

- MicroBooNE's more unique features among neutrino cross section experiments:
	- We use argon, and developing our understanding of neutrino-argon interactions is very important for DUNE oscillation searches
	- LArTPC technology allows low energy thresholds for individual particles in each event
	- We see two neutrino beams simultaneously, BNB on-axis and NuMI off-axis









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#### **Fermilab Neutrino Beams**

## Different Interaction Mechanisms

- Different neutrino energies cause different interaction mechanisms
- MicroBooNE sees many QE and RES events from the BNB and NuMI neutrino beams
- Final state interactions complicate this picture, changing the kinematics and topologies of events in complex ways

[Rev. Mod. Phys. 84, 1307 \(2012\)](https://journals.aps.org/rmp/abstract/10.1103/RevModPhys.84.1307)



**\* Meson Exchange Current (MEC) is another interaction type that often expels two nucleons**





## Outline

- In this talk, I will discuss:
	- Our latest results on inclusive  $\nu_\mu$ CC cross sections, including all these interaction types
	- Our latest results on exclusive  $\nu_\mu$ CC 0 $\pi$ topologies, giving particular insight into QE interactions
	- Latest results on rare cross sections
		- A Cabibbo-suppressed version of QE:  $\Lambda$  production
		- A heavy version of RES interactions, producing an  $N(1535)$  rather than a  $\Delta(1232)$



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#### Invisible Neutrino Energy Modeling Validation

- Modeling the  $E_{\nu}^{\text{true}} \to E_{\nu}^{\text{rec}}$  mapping is very important for oscillation analyses
- These quantities differ by *E*invis had
	- No direct measurement possible
	- Can we improve confidence in our modeling of this quantity within uncertainties (cross-section, flux, detector response, and statistical)?

Consider  $\nu_{\mu}$  CC interactions:

#### $E_{\nu}^{\rm true}$ <sup>*v*true</sup> =  $E_{\mu} + E_{\text{had}}^{\text{vis}} + E_{\text{had}}^{\text{invis}}$

#### [Phys. Rev. Lett. 128, 151801 \(2022\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.128.151801)







#### Invisible Neutrino Energy Modeling Validation

- Energy conservation: if modeling of  $E_\nu^{\rm true}, E_\mu, E_{\rm had}^{\rm vis}$  is correct, then our modeling of  $E_{\rm had}^{\rm invis}$  must be correct had
- We can't test this event-by-event, but we can test this for a distribution of many events
- A conditional constraint test shows that  $E_{\rm had}^{\rm vis}$ data matches the prediction using  $E_\nu^{\rm true}$  (from our flux model) and  $E_{\mu}$  (from our data measurement) *ν*
- So, three of these distributions tell a consistent story, so the energy conservation equation helps to validate our modeling of the *E*invis distribution had



#### Invisible Neutrino Energy Modeling Validation

- We've performed many types of these constraint tests, and expanded to study more dimensions
- In fake data tests, this procedure is sensitive to ~15% shifts between  $E_{\rm had}^{\rm VIS}$  and *E*vis had *E*invis had
	- Our resulting  $E_\nu$  cross section results are significantly less sensitive to changes in the missing energy
- We have also tested this procedure with fake data from GENIE v2 and NuWro, and in all cases, we have found that when we pass model validation, we get the correct  $E_\nu$  XS result within uncertainties

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 ${E_{\text{rec}}^{\text{had}}}, \cos \theta_{\mu}$ } constrained by  ${P_{\mu}, \cos \theta_{\mu}}$ 



[arXiv:2307.06413](https://arxiv.org/abs/2307.06413)

# $3D \nu_\mu$ CC Inclusive Cross Section Results

 $_{\mu}^{\mu}$ dcos $\theta_{\mu}$  (10 $^{36}$ cm $^2$  / GeV / Ar)

 $d^2\sigma(E_y)/dP_y$ 

 $0.8$ 

 $0.6$ 

 $0.4$ 

- With this model validation giving us confidence in our modeling of the  $E_{\nu}^{\rm true} \rightarrow E_{\nu}^{\rm reco}$  mapping within uncertainties, we can extract cross sections as a function of *Eν*
- One of our latest results does this simultaneously in 3 dimensions:

• NuWro has the best agreement with our data, and GiBUU and NEUT do better in the lower *Eν* region

• 
$$
E_{\nu}
$$
,  $P_{\mu}$ , and  $\cos \theta_{\mu}$ 





- We also expanded this  $\nu_\mu$ CC inclusive analysis to study detailed final states with and without protons
- We do a similar type of model validation for reconstructed proton kinetic energy, but it fails!
- Our data is incompatible with our cross section model when describing the distribution of proton energies
	- A low energy proton connected to a muon is the type of topology that LArTPCs can study much more precisely than some other technologies
- 
- 
- Low energy proton mis-modeling could potentially cause incorrect neutrino background estimates in searches for coherent interactions or BSM decay-in-flight events

### 3D *νμ*CC Inclusive 0p/Np: Failing Model Validation

[arXiv:2402.06413](https://arxiv.org/abs/2402.19216) [arXiv:2402.19281](https://arxiv.org/abs/2402.19281)

This decomposition test transforms the covariance matrix and  $\chi^2$  calculation to a space where the bins are uncorrelated

Lower bin indices correspond to larger eigenvalues, and typically represent broader details of the distribution (normalization, broad shape, etc.)

- We use this data-simulation difference to create a new variation in our cross section model
- Unfold this distribution (statistical uncertainty only) to get a reweighting binned in true *Kp*
- We use this reweighting function to form a new covariance matrix describing this data/MC difference, including correlated and uncorrelated terms
- When we use this to expand our cross section uncertainty, we pass all model validation tests
- So, we can extract cross sections related to protons now

## 3D *νμ*CC Inclusive 0p/Np: Passing Model Validation

20000

15000

꼽 10000

5000

value

Š





describing low energy proton energies and the 0p/Np split, perhaps due to a better treatment of FSI



#### 3D *νμ*CC Inclusive 0p/Np Cross Section Results

[arXiv:2402.06413](https://arxiv.org/abs/2402.19216) [arXiv:2402.19281](https://arxiv.org/abs/2402.19281)

# $\nu_{\mu}$ CC 1p0 $\pi$  · <sup>6 degrees of freedom .  $\vec{p}_p$  and  $\vec{p}_{\mu}$ </sup>

 $\nu_{\mu} + n \rightarrow \mu^{-} + p$ 

- If we model CCQE events as a neutrino striking a free neutron at rest, the system is very simple
- We get essentially 2 interesting degrees of freedom, which we can choose to be  $E^{}_\mu$  and  $\theta^{}_\mu$ 
	- In particular, given those, we know  $E_{\rm tot}$
	- This is how MiniBooNE and Super-K can  $\mathop{\mathsf{calculate}} E_\nu$  while only seeing the muon
- The transverse momentum of the muon and proton are exactly balanced, summing to zero
- 4 constraints/symmetries
	- Incoming neutrino direction:  $\vec{p}_{\text{tot}} \cdot \hat{x} = 0$ ,  $\vec{p}_{\text{tot}} \cdot \hat{y} = 0$  $\overline{\phantom{a}}$ ⃗
	- Incoming neutrino kinematics:  $|\vec{p}_{\text{tot}}|$   $c = E_{\text{tot}}$ ⃗
	- Azimuthal symmetry
- $6 4 = 2$ -dimensional resulting phase space



- - $\vec{p}_p$  and  $\vec{p}_\mu$ ⃗ ⃗

Free

neutron

at rest

[Phys. Rev. C 94, 015503 \(2016\)](https://journals.aps.org/prc/abstract/10.1103/PhysRevC.94.015503)



- But in reality, our CCQE events do not involve a free neutron at rest, they involve a complex heavy nucleus
	- The struck nucleon can have nonzero initial momentum
	- The outgoing proton can undergo final state interactions
	- Increasing our understanding of initial-nucleon states and final state interactions are very important for a wide variety of neutrino interactions beyond just  $\nu_\mu$ CC 1p0 $\pi$  (for oscillation and other BSM searches)
- So, the total momentum of the muon-proton system can have a nonzero transverse component  $\delta p_{T}$ (Transverse Kinematic Imbalance, TKI)

### $\nu_{\mu}$ CC 1 p0 $\pi$  TKI





[Phys. Rev. C 94, 015503 \(2016\)](https://journals.aps.org/prc/abstract/10.1103/PhysRevC.94.015503)

### $\nu_{\mu}$ CC 1 p0 $\pi$  TKI

![](_page_17_Figure_4.jpeg)

![](_page_17_Picture_0.jpeg)

• We measure a cross section in this  $\delta p_T$  value, which has significant sensitivity to final state interactions

[Phys. Rev. Lett. 131, 101802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.131.101802) [Phys. Rev. D 108, 053002 \(2023\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.108.053002)

![](_page_17_Picture_7.jpeg)

![](_page_17_Picture_8.jpeg)

![](_page_17_Picture_9.jpeg)

![](_page_18_Picture_0.jpeg)

- We can expand this to multiple dimensions, looking at the angle between these transverse momentum vectors
- We get even more model discrimination power

Lee Hagaman on behalf of the MicroBooNE Collaboration 19 [Phys. Rev. Lett. 131, 101802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.131.101802) [Phys. Rev. D 108, 053002 \(2023\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.108.053002)

![](_page_18_Picture_5.jpeg)

![](_page_18_Figure_3.jpeg)

- That was considering the momentum in the transverse plane, where we would naively expect the momentum to be balanced with  $\delta p_T = 0$
- However, we measure  $E_\mu$  and  $E_p$ , so we know  $E_{\nu}^{\;\star}$ , so we know the longitudinal momentum as well and can compare with a measured value
- We expand to 3D, out of the transverse plane, to consider the total momentum imbalance,  $\boldsymbol{p}_n$  (Generalized Kinematic Imbalance, GKI)

### $\nu_{\mu}$ CC 1 p0 $\pi$  GKI

 $^{\star}$ (assuming not much  $E_{\rm had}^{\rm invis}$  on average for this topology) had

[arXiv:2310.06082](https://arxiv.org/abs/2310.06082)

![](_page_19_Picture_132.jpeg)

![](_page_19_Picture_16.jpeg)

q **: momentum transfer to the hadronic system**

![](_page_19_Figure_10.jpeg)

- 
- GENIE performs best in QE-dominated regions, while GiBUU performs best in FSI-dominated regions

![](_page_20_Figure_3.jpeg)

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#### $\nu_{\mu}$ CC 1 p0 $\pi$  GKI

• We measure this 2D cross section, and can look at slices in  $p_n$  or  $\alpha_{\rm 3D}$ , with large model discrimination power

Recall that there were also indications of better GiBUU FSI from the  $\nu_\mu$ CC inclusive  $K_p$  cross section!

![](_page_20_Figure_9.jpeg)

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# $\nu_\mu$ CC Np0 $\pi$ <br>  $\int_{\theta \deg \leq \delta \alpha_T < 45 \deg}$

45 deg  $\leq \delta \alpha_T < 90$  deg

- Studied TKI and GKI variables for this topology as well, using the highest energy proton
- We report correlations between a large set of extracted cross sections

![](_page_21_Figure_2.jpeg)

![](_page_21_Figure_3.jpeg)

# Rare Channels

- Neutrino interactions are famously rare in the first place
- Interactions producing these new final state particles have cross sections ~100-1000 times smaller than the inclusive cross section

![](_page_22_Figure_4.jpeg)

• Cabibbo-suppressed counterpart of CCQE interactions:  $\nu_{\mu} + Ar \rightarrow \mu^{+} + \Lambda + X$ 

#### Λ Production

- "Hyperon puzzle", studying these particles could have consequences for neutron star populations
- Only a handful of old bubble chamber observations of this process
- Secondary  $\Lambda + Ar \rightarrow K^+ + X$  is a potential background to  $p \to K + \nu$  proton decay searches
- Sensitive to nucleon form factors, hyperonnucleus potentials, and final state interactions
- Exclusively due to  $\overline{\nu}$ , can constrain antineutrino content in a neutrino beam

• Then 
$$
\Lambda \rightarrow p + \pi^-
$$

[Phys. Rev. Lett. 130, 231802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.130.231802)

![](_page_23_Picture_9.jpeg)

### Λ Production

- We select five data events
- Invariant mass is consistent with the  $\Lambda$  mass of 1116 MeV
- Relatively low statistics, used about 1/4 of MicroBooNE NuMI data
- We report a measurement rather than an exclusion

Lee Hagaman on behalf of the MicroBooNE Collaboration 25 [Phys. Rev. Lett. 130, 231802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.130.231802)

![](_page_24_Figure_6.jpeg)

## *η* Production

- By studying rarely produced  $η$  mesons which behave like a heavier  $\pi^0$ , we can get a unique handle on higher mass resonances and their decays *π*0
- $p \rightarrow e^+ + \eta$  is an important potential proton decay channel, which has already been studied in Super-K
- New shower energy calibration scale, with an invariant mass of 548 MeV (compared to 135 MeV  $\pi^0$ ) *π*0

[arXiv:2305.16249](https://arxiv.org/abs/2305.16249)

$$
\nu + p \to \Delta(1232) \to p + \pi^0 \to p + \gamma + \gamma
$$

$$
\nu + p \rightarrow N(1535) \rightarrow p + \eta \rightarrow p + \gamma
$$

**Typical resonant neutrino interaction:**

![](_page_25_Figure_13.jpeg)

- The two photon invariant  ${\sf mass}\ M_{\gamma\gamma}$  is consistent with the  $\eta$  mass, 548 MeV
- The hadronic system invariant mass  $W$  is consistent with the *N*(1535) mass
- We report a measurement rather than an exclusion

![](_page_26_Figure_4.jpeg)

# *η* Production

## Conclusions

- MicroBooNE's recent cross section results have explored a lot of different directions
	- New ways to validate the  $E_{\nu}^{\rm true} \rightarrow E_{\nu}^{\rm rec}$ mapping for oscillation experiments
	- Important generator deficiencies for low energy protons
	- New ways to explore initial nucleon momentum and final state interactions with simple topologies
	- Two first-time observations of rare particles in neutrino-argon interactions
- Looking to the future, we are actively working on lots of cross section analyses, including:
	- Studying more new final state particles
		- $K^{+/-}$ ,  $\pi^{+/-}$ , and neutron production
	- New methods to extract more information from our data
		- Separating neutrino and antineutrino cross sections
		- Reporting more correlations between different cross section measurements
		- Joint BNB/NuMI cross sections, reducing flux uncertainties

![](_page_27_Figure_14.jpeg)

![](_page_27_Figure_15.jpeg)

![](_page_27_Figure_16.jpeg)

![](_page_27_Figure_17.jpeg)

## Thanks for your attention!

![](_page_28_Picture_1.jpeg)

# Backup Slides

#### All Public MicroBooNE XS Measurements

- Rare channels
	- *η* production, BNB, [arXiv:2305.16249](https://arxiv.org/abs/2305.16249)
	- A production, NuMI, *[Phys. Rev. Lett. 130, 231802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.130.231802)*
	- NC  $\Delta \rightarrow N\gamma$  (interpreted as a limit on the XS), BNB, [Phys. Rev. Lett. 128, 111801 \(2022\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.128.111801)
- CC 0 *π*
	- 2D  $\nu_{\mu}$  CC Np0π, BNB, <u>[arXiv:2403.19574](https://arxiv.org/abs/2403.19574)</u>
	- 1D & 2D  $\nu_{\mu}$  CC 1p0 $\pi$  Generalized Imbalance [arXiv:2310.06082](https://arxiv.org/abs/2310.06082), BNB, accepted by PRD
	- 1D & 2D  $\nu_\mu$ CC 1p0 $\pi$  Transverse Imbalance, BNB, *Phys.* [Rev. Lett. 131, 101802 \(2023\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.131.101802), [Phys. Rev. D 108, 053002](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.108.053002)  [\(2023\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.108.053002)
	- 1D  $\nu_e$ CC Np0π, BNB, <u>Phys. Rev. D 106, L051102 (2022)</u>
	- 1D  $\nu_{\mu}$  CC 2p0π, BNB, [arXiv:2211.03734](https://arxiv.org/abs/2211.03734)
	- 1D  $\nu_{\mu}$  CC Np0 $\pi$ , BNB, <u>[Phys. Rev. D102, 112013 \(2020\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.102.112013)</u>
	- 1D  $\nu_{\mu}$  CC 1p0π, BNB, <u>Phys. Rev. Lett. 125, 201803 (2020)</u>

![](_page_30_Picture_25.jpeg)

![](_page_30_Picture_26.jpeg)

![](_page_30_Picture_27.jpeg)

- CC inclusive
	- 3D  $\nu_\mu$ CC inclusive 0p/Np, BNB, [arXiv:2402.19281](https://arxiv.org/abs/2402.19281), [arXiv:2402.19216](https://arxiv.org/abs/2402.19216)
	- 3D  $\nu_\mu$ CC inclusive, BNB, [arXiv:2307.06413](https://arxiv.org/abs/2307.06413)
	- 1D  $\nu_\mu$ CC inclusive  $E_\nu$ , BNB, *Phys. Rev. Lett.* 128, [151801 \(2022\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.128.151801)
	- 1D  $\nu_e$ CC inclusive, NuMI, *Phys. Rev. D105,* [L051102 \(2022\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.105.L051102)
	- $ν_e$ CC inclusive, NuMI, *Phys. Rev. D104, 052002* [\(2021\)](https://journals.aps.org/prd/abstract/10.1103/PhysRevD.104.052002)
	- 2D  $ν_{μ}$ CC inclusive, BNB, *Phys. Rev. Lett. 123,* [131801 \(2019\)](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.123.131801)
- Pion production
	- NC  $\pi^0$ , BNB, <u>Phys. Rev. D 107, 012004 (2023)</u>
	- CC  $\pi^{0}$ , BNB, <u>Phys. Rev. D 99, 091102(R) (2019)</u>

#### Conditional Constraint

$$
\Sigma = \begin{pmatrix} \Sigma^{XX} & \Sigma^{XY} \\ \Sigma^{YX} & \Sigma^{YY} \end{pmatrix}, \ \ n: measurement, \ \ \mu: predicate
$$

$$
\mu^{X, \text{const.}} = \mu^X + \Sigma^{XY} \cdot (\Sigma^{YY})^{-1} \cdot (n^Y - \mu^Y)
$$

 $\Sigma^{XX,\text{const.}} = \Sigma^{XX} - \Sigma^{XY} \cdot (\Sigma^{YY})^{-1} \cdot \Sigma^{YX}$ 

![](_page_31_Figure_6.jpeg)

![](_page_31_Picture_7.jpeg)

We use a regularization technique to avoid large fluctuations after inversion

# Unfolding  $M_i = \sum_j R_{ij} S_j + B_i$

We solve for S by inverting *Rij*

![](_page_32_Picture_3.jpeg)

![](_page_32_Picture_7.jpeg)

![](_page_33_Figure_1.jpeg)

All of these quantities must consider full flux, cross-section, detector, and statistical uncertainties!

$$
M(E_{rec}) = \frac{POT \cdot T \cdot \int_{j} F(E_{\nu j}) \cdot \sigma(E_{\nu j}) \cdot D(E_{\nu j} \rightarrow E_{rec i}) \cdot \varepsilon(E_{\nu j}, E_{rec i}) \cdot dE_{\nu j}}{POT \cdot T \cdot \int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}} \cdot \frac{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j} \cdot dE_{\nu j}}{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}} + B \cdot \frac{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}}{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}} + B \cdot \frac{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}}{\int_{j} \overline{F}(E_{\nu j}) \cdot dE_{\nu j}} + B \cdot \frac{\sigma}{\sigma}
$$

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![](_page_33_Picture_7.jpeg)

Re-writing this same equation to be useful later (adding more terms that cancel each other out):

#### How We Unfold To Nominal Flux Using Data From The Real Flux

$$
\tilde{\Delta}_{ij} = \frac{POT \cdot T \cdot \int_j F(E_{\nu j}) \cdot \sigma(E_{\nu j}) \cdot D(E_{\nu j}, E_{rec i}) \cdot POT \cdot T \cdot \int_j \overline{F}(E_{\nu j}) \cdot \sigma(E_{\nu j}) \cdot G \cdot E_{\nu j}}{POT \cdot T \cdot \int_j \overline{F}(E_{\nu j}) \cdot \sigma(E_{\nu j}) \cdot G \cdot E \cdot F}.
$$

$$
S_j = \frac{\int_j \overline{F}\left(E_{\nu j}\right) \cdot \sigma\left(E_{\nu j}\right) \cdot dE_{\nu j}}{\int_j \overline{F}\left(E_{\nu j}\right) \cdot dE_{\nu j}}
$$

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$$
\tilde{F}_j = POT \cdot T \cdot \int_j \overline{F}\left(E_{\nu j}\right) \cdot dE_{\nu j}
$$

*ij* ⋅ *F*  $\left(f_j \cdot S_j + B\left(E_{rec}\right)\right)_i$ 

 $\{E_{rec~i}\}\cdot \varepsilon\left(E_{\nu~j}, E_{rec~i}\right)\cdot dE_{\nu~j}$ 

 $dE_{\nu}$ <sup>*j*</sup>

#### $M(E_{rec})_i = \Delta$  $\widetilde{\Delta}$  $\widetilde{\mathsf{F}}$ How We Unfold To Nominal Flux Using Data From The Real Flux

**Nominal flux-binned crosssection signal** 

**This is what we want to measure!**

**Cross-section uncertainty largely (but not entirely) cancels**

*E* **E***h E nominal* **<b>flux**